

# Probing the Standard Model Frontier with B Physics at CDF

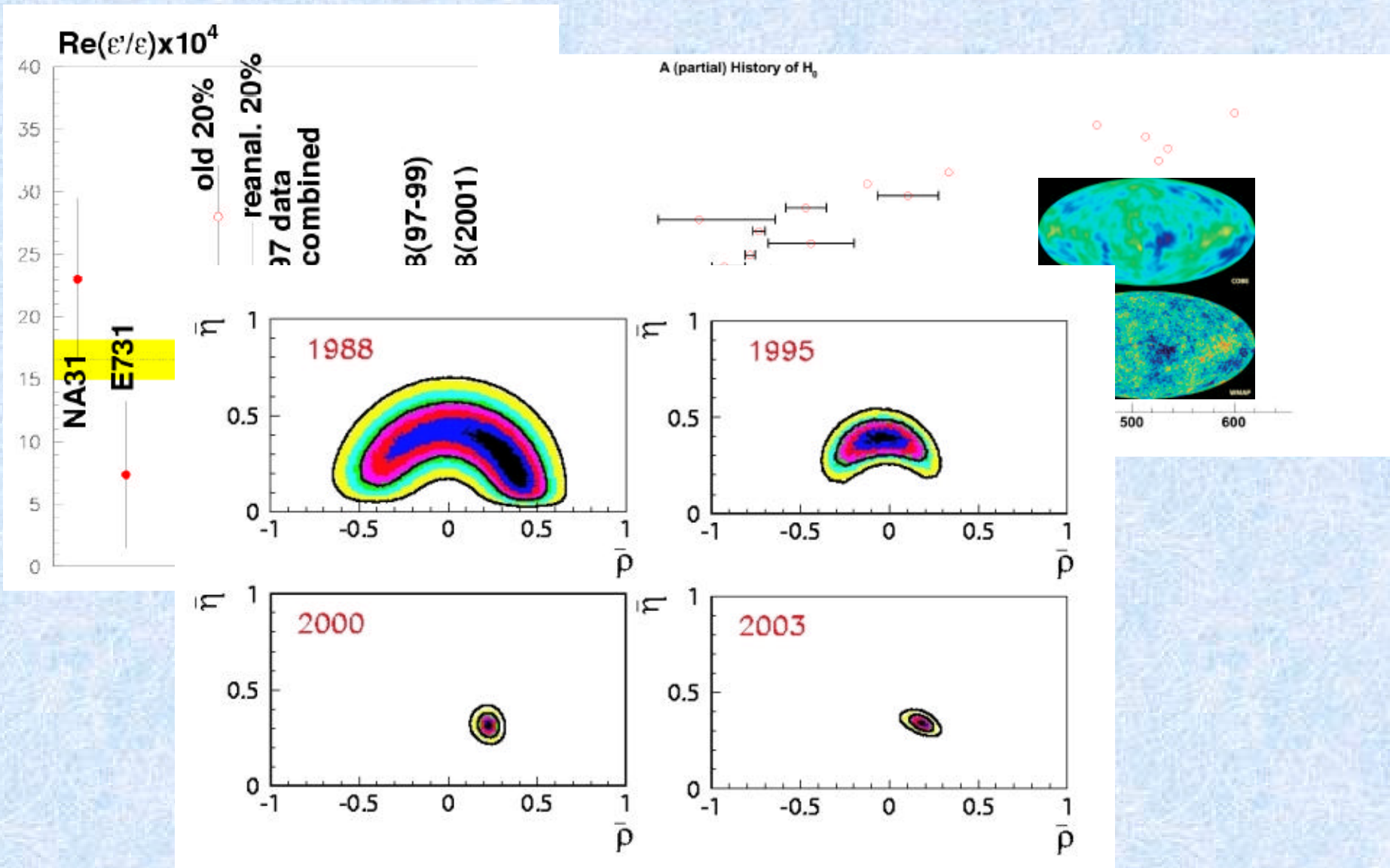
Alessandro Cerri



# Synopsis

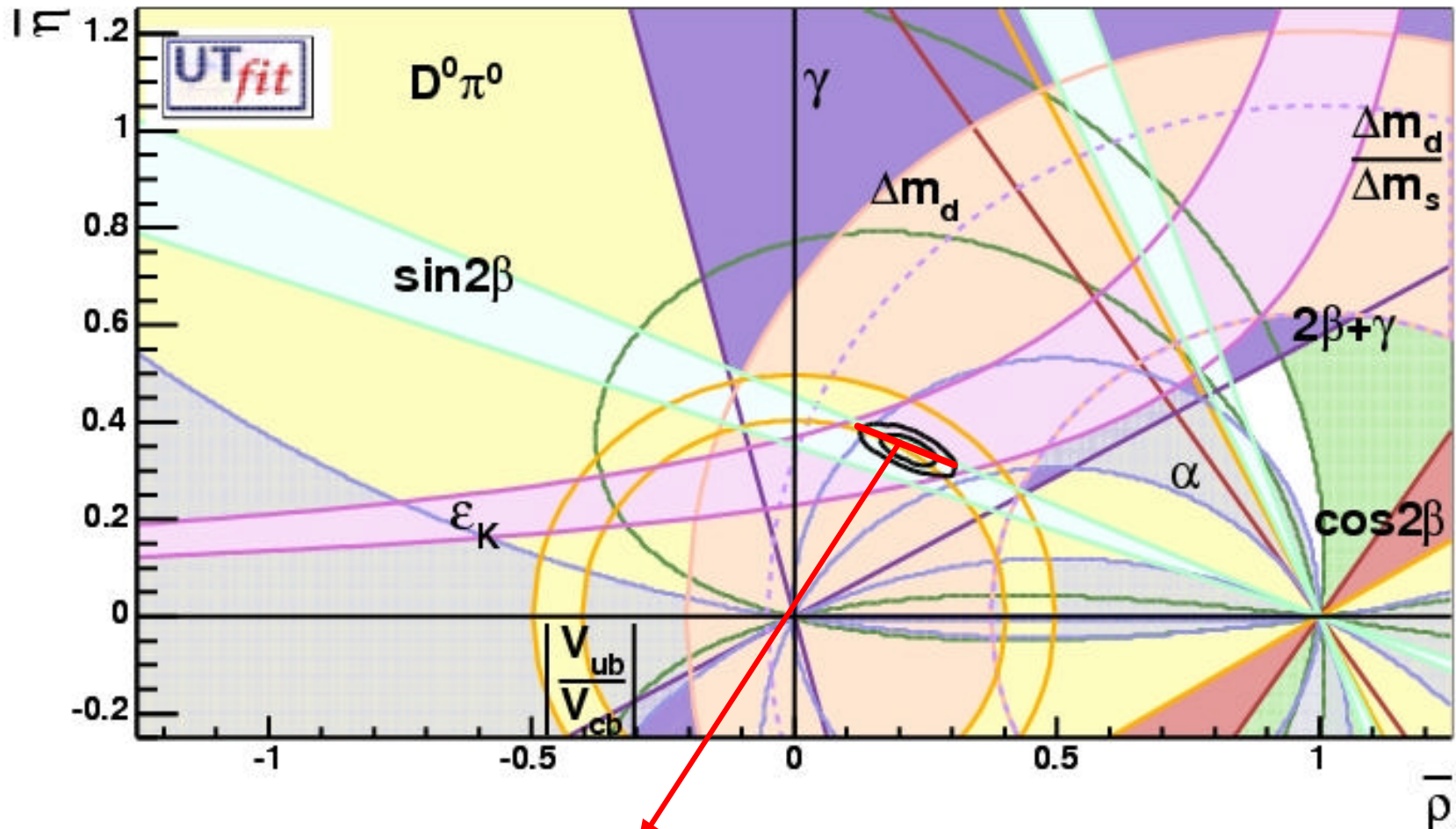
- The Big Picture
- Why B physics at the TeVatron is a good bet
- Tools of the trade
  - CDF: detector and DAQ
  - SVT: the CDF key to B physics
- Selected examples
  - Hadronic Moments in  $b \rightarrow cl\nu$  ( $V_{cb}$ )
  - $B_s$  Mixing ( $V_{td}$  and new physics)
- Perspectives
- Conclusions

# Qualitative to Quantitative



Like other areas, CKM physics can now precisely probe the Standard Model

# B physics: precision probe of SM and beyond!



TeVatron contribution is critical!



# The Tevatron as a **b** factory

- B factories program extensive and very successful **BUT** limited to  $B_u, B_d$
- Tevatron experiments can produce all b species:  
 $B_u, B_d, B_s, B_c, B^{**}, \Lambda_b, \Xi_b$

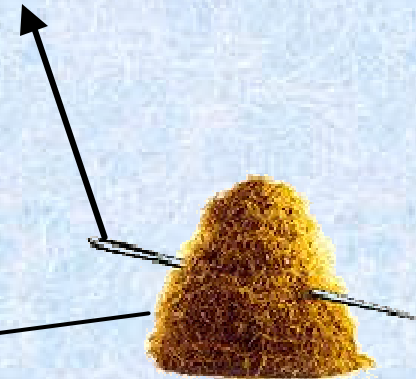
$$\sigma_{B^0} = 3.51 \pm 0.42 \pm 0.53 \text{ mb} @ |y| < 1 \quad p_t > 6$$

Compare to:

- $\Upsilon(4S) \approx 1 \text{ nb}$  (only  $B^0, B^+$ )
- $Z^0 \approx 7 \text{ nb}$

Unfortunately

- $p\bar{p} \approx 100 \text{ mb}$



- b production in pp collisions is so large ( $\sim 300 \text{ Hz}$  @  $10^{32} \text{ cm}^{-2} \text{ Hz}$ ) that we could not even cope with writing it to tape!

# Path to New Physics

CKM measurements could hint to new physics through discrepancies with SM predictions. How do we get there?

- **Design/improve** the “**tools** of the trade”
  - Experimental (detector & techniques)
  - Theoretical (phenomenological devices)
- **Measure** uncharted properties at the boundaries of our knowledge
  - Masses
  - Lifetimes
  - Branching ratios
- **Press** further ahead and investigate **beyond the boundaries**:
  - Mixing
  - CP asymmetries

# CDF and the Tevatron

•Renewed detector & Accelerator chain:

→ Higher Luminosity → higher event rate

→ Detector changes/improvements:

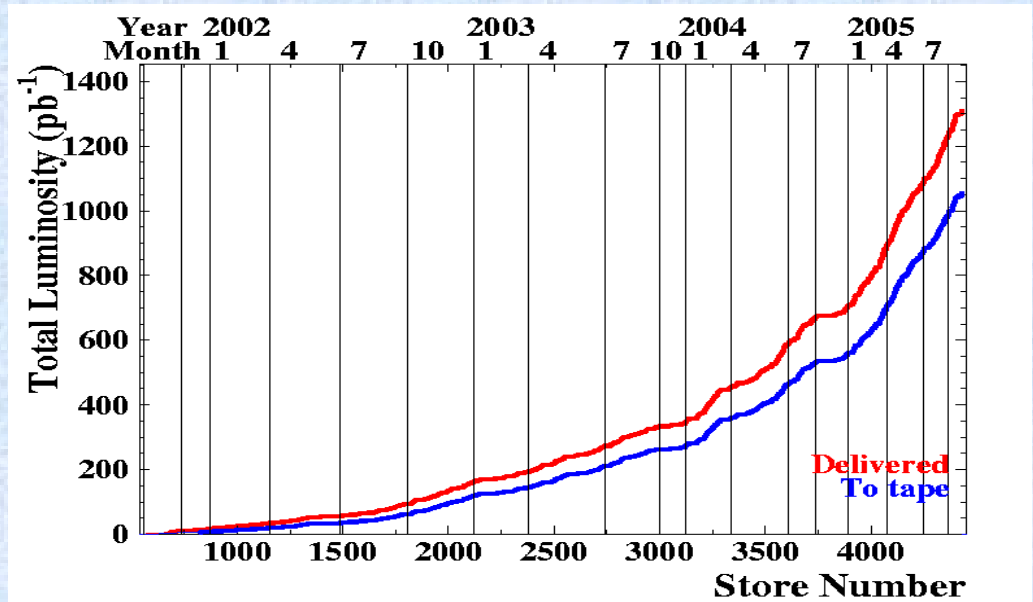
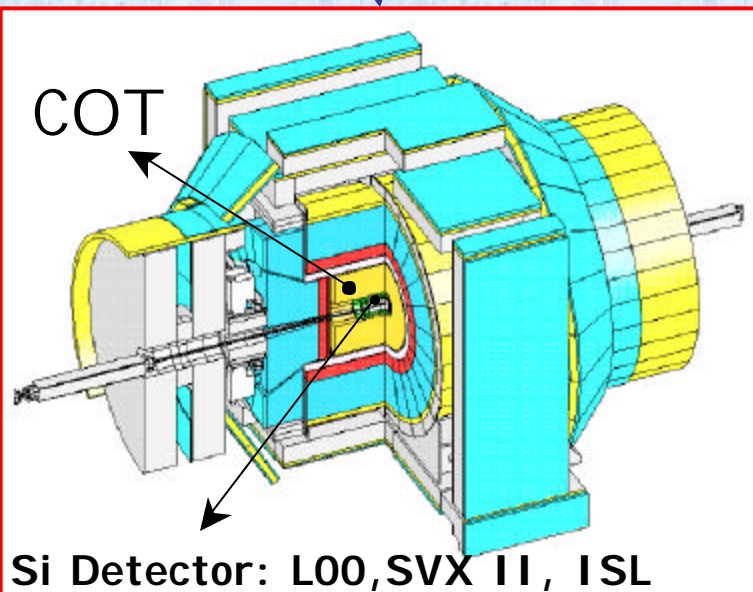
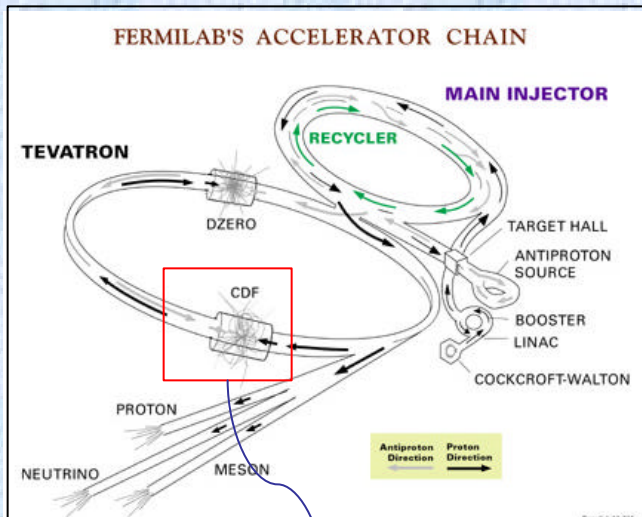
→ DAQ redesign

→ Improved performance:

➤ Detector Coverage

➤ Tracking Quality

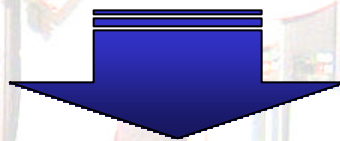
➤ New Trigger strategies for heavy flavors: displaced vertex trigger



# SVT: a specialized B physics trigger

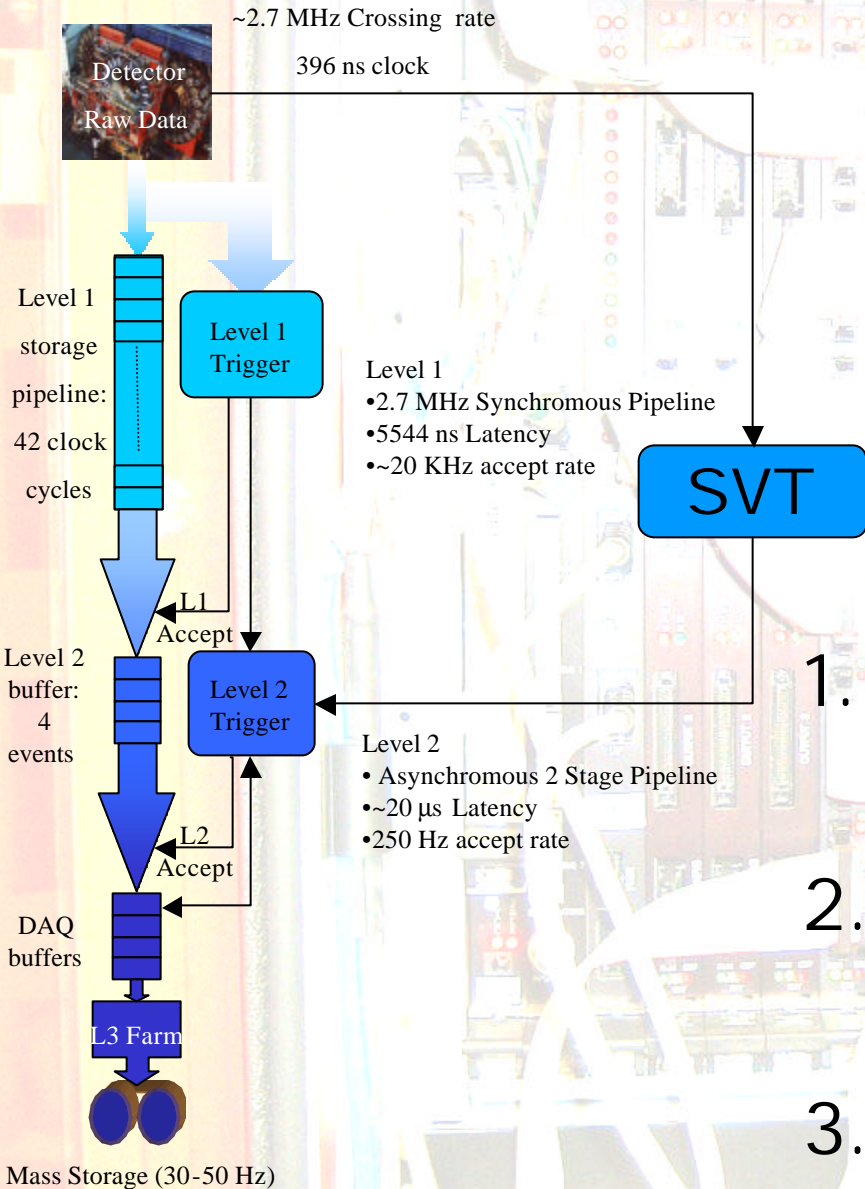
requirements

- Good IP resolution
- ASAP ( $\approx 10 \mu\text{sec}$ )
- No Dead Time



1. @ earliest L2 where silicon data starts flowing
2. Drop stereo info: 2D tracking
3. Extensive custom design

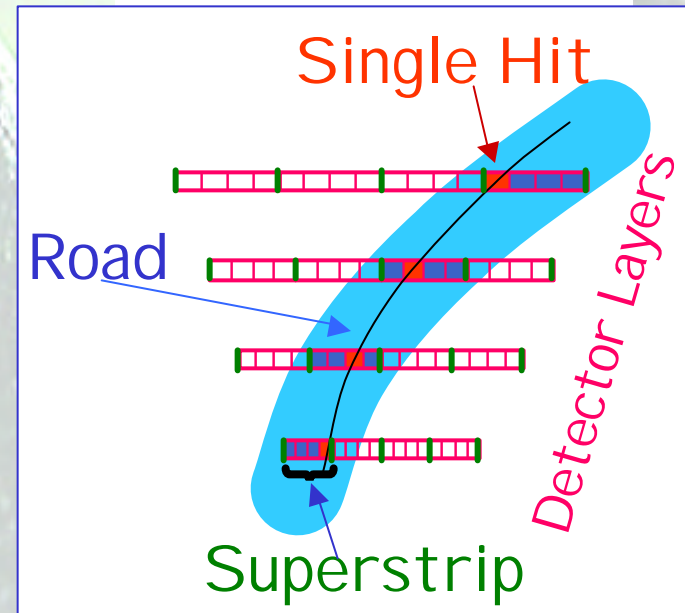
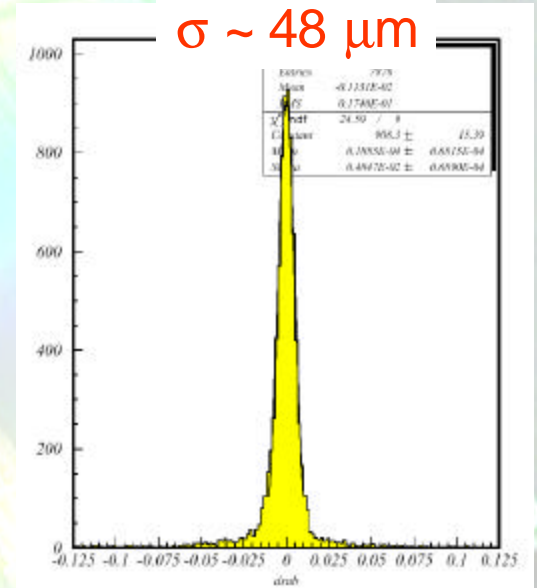
## The CDF 3 level trigger





# ...and a successful endeavor!

- SVT is capable of digesting **>20000 evts/second** to **identifying tracks in the silicon**
- CDF II has been running it **since day -1**
- The recipe uses **specialized hardware**:
  - 1)Clustering  
Find clusters (**hits**) from detector 'strips' at full detector resolution
  - 2)Template matching  
Identify **roads**: pre-defined track templates with coarser detector bins (**superstrips**)
  - 3)Linearized track fitting  
Fit tracks, with combinatorial limited to **clusters** within roads



# Benchmarks

# What was known about non- $\Upsilon$ -produced $b$ (PDG'04)

$\Lambda_b^0$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$\rho$ (MeV/c)
$J/\psi(1S)\Lambda$	$(4.7 \pm 2.8) \times 10^{-4}$		1744
$\Lambda_c^+ \pi^-$	seen		2345
$\Lambda_c^+ a_1(1260)^-$	seen		
$\Lambda_c^+ \ell^- \bar{\nu}_\ell$ anything	[t] $(9.2 \pm 2.1) \%$		
$p \pi^-$	$< 5.0 \times 10^{-5}$		
$p K^-$	$< 5.0 \times 10^{-5}$		
$\Lambda \gamma$	$< 1.3 \times 10^{-3}$		

$B_s^0$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$\rho$ (MeV/c)
$D_s^-$ anything	$(94 \pm 30) \%$		-
$D_s^- \ell^+ \nu_\ell$ anything	[kkk] $(7.9 \pm 2.4) \%$		-
$D_s^- \pi^+$	$< 13 \%$		2322
$D_s^{(*)-} + D_s^{*-}$	$(23 \pm_{-13}^{+21}) \%$		-
$J/\psi(1S)\phi$	$(9.3 \pm 3.3) \times 10^{-4}$		1590
$J/\psi(1S)\pi^0$	$< 1.2 \times 10^{-3}$	90%	1788
$J/\psi(1S)\eta$	$< 3.8 \times 10^{-3}$	90%	1735
$\psi(2S)\phi$	seen		1123
$\pi^+ \pi^-$	$< 1.7 \times 10^{-4}$	90%	2681
$\pi^0 \pi^0$	$< 2.1 \times 10^{-4}$	90%	2681
$\eta \pi^0$	$< 1.0 \times 10^{-3}$	90%	2655
$\eta \eta$	$< 1.5 \times 10^{-3}$	90%	2628
$\rho^0 \rho^0$	$< 3.20 \times 10^{-4}$	90%	2570
$\phi \rho^0$	$< 6.17 \times 10^{-4}$	90%	2528
$\phi \phi$	$< 1.183 \times 10^{-3}$	90%	2484
$\pi^+ K^-$	$< 2.1 \times 10^{-4}$	90%	2660
$K^+ K^-$	$< 5.9 \times 10^{-5}$	90%	2639
$\bar{K}^*(892)^0 \rho^0$	$< 7.67 \times 10^{-4}$	90%	2551
$\bar{K}^*(892)^0 K^*(892)^0$	$< 1.681 \times 10^{-3}$	90%	2532
$\phi K^*(892)^0$	$< 1.013 \times 10^{-3}$	90%	2508
$\rho \bar{p}$	$< 5.9 \times 10^{-5}$	90%	2516
$\gamma \gamma$	$< 1.48 \times 10^{-4}$	90%	2685
$\phi \gamma$	$< 1.2 \times 10^{-4}$	90%	2588

**$B_c^+$  DECAY MODES  $\times B(\bar{b} \rightarrow B_c)$**       Fraction ( $\Gamma_i/\Gamma$ )      Con

The following quantities are not pure branching ratios; rather  $\Gamma_i/\Gamma \times B(\bar{b} \rightarrow B_c)$ .

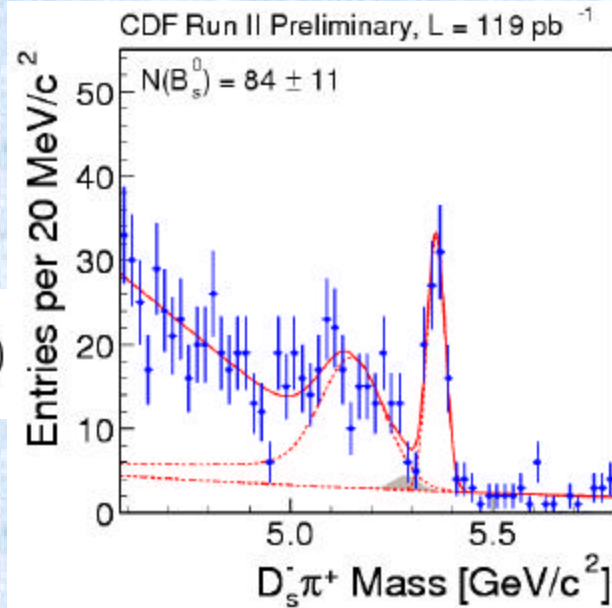
$J/\psi(1S)\ell^+ \nu_\ell$ anything	$(5.2 \pm_{-2.1}^{+2.4}) \times 10^{-5}$	
$J/\psi(1S)\pi^+$	$< 8.2 \times 10^{-5}$	
$J/\psi(1S)\pi^+ \pi^+ \pi^-$	$< 5.7 \times 10^{-4}$	
$J/\psi(1S)a_1(1260)$	$< 1.2 \times 10^{-3}$	
$D^*(2010)^+ \bar{D}^0$	$< 6.2 \times 10^{-3}$	

# Measure: Branching Ratios

First-time measurement of many  $B_s$  and  $\Lambda_b$  Branching Fractions

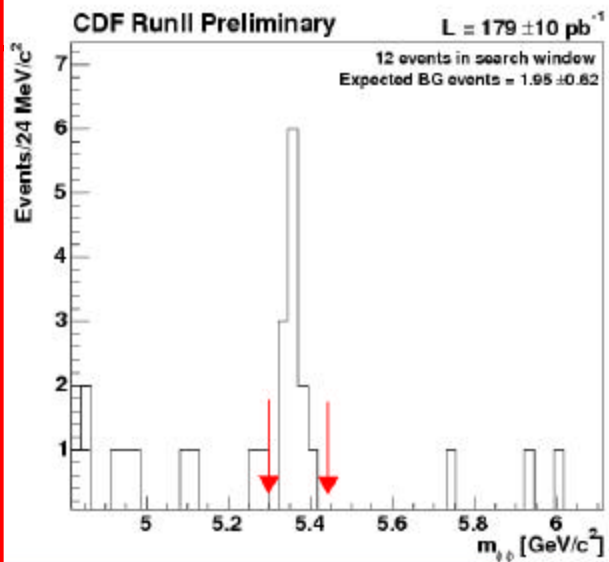
$$\frac{f_s}{f_d} \cdot \frac{Br(B_s \rightarrow D_s^- \pi^+)}{Br(B^0 \rightarrow D^- \pi^+)} = 0.35 \pm 0.05(stat) \pm 0.04(syst) \pm 0.09(BR)$$

<http://www-cdf.fnal.gov/physics/new/bottom/031002.blessed-bs-br/>



$$BR(B_s \rightarrow \phi\phi) = (1.4 \pm 0.6(stat.) \pm 0.2(syst.) \pm 0.5(BR's)) \cdot 10^{-5}$$

Hep-ex/0502044



$$\frac{Br(B_s \rightarrow \psi(2S)\phi)}{Br(B_s \rightarrow J/\psi\phi)} = 0.52 \pm 0.13[stat] \pm 0.06[BR] \pm 0.04[sys]$$

<http://www-cdf.fnal.gov/physics/new/bottom/050310.blessed-dsd/>

$$\frac{Br(B^0 \rightarrow D_s^+ D^-)}{Br(B^0 \rightarrow D^- 3\pi)} = 2.00 \pm 0.16(NC) \pm 0.12(syst) \pm 0.50(BR)$$

<http://www-cdf.fnal.gov/physics/new/bottom/050310.blessed-dsd/>

$$\frac{BR(\Lambda_b \rightarrow \Lambda_c^+ \pi^-)}{BR(\bar{B}^0 \rightarrow D^+ \pi^-)} = 3.3 \pm 0.3 (stat) \pm 0.4 (syst) \pm 1.1 (BR+FR)$$

[http://www-cdf.fnal.gov/physics/new/bottom/030702.blessed-lblcpi-ratio\\_new/](http://www-cdf.fnal.gov/physics/new/bottom/030702.blessed-lblcpi-ratio_new/)

$$\frac{B(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu)}{B(\Lambda_b \rightarrow \Lambda_c^+ \pi^-)} = 20.0 \pm 3.0 (stat) \pm 1.2 (syst) \begin{matrix} +0.7 \\ -2.1 \end{matrix} (BR) \pm 0.5 (UBR)$$

<http://www-cdf.fnal.gov/physics/new/bottom/050407.blessed-lbbr/>



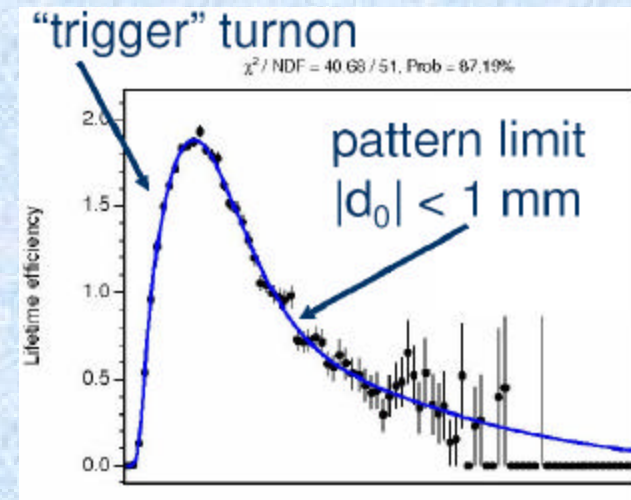
# Lifetimes: fully reconstructed **hadronic** modes

- Testbed for our ability to understand trigger biases
- Large, clean samples with understood backgrounds
- Excellent mass and vertex resolution
- Prerequisite for mixing fits!

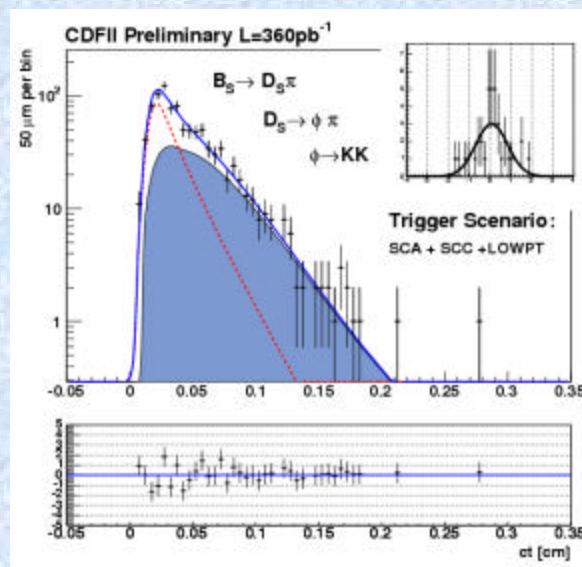
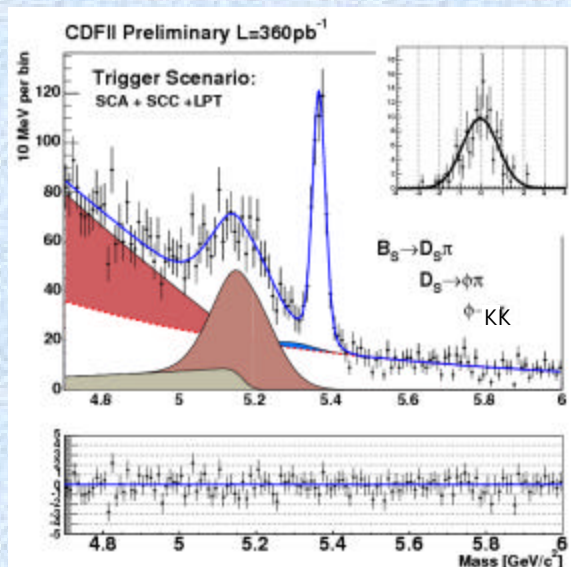
$$\tau(B^+) = 1.661 \pm 0.027 \pm 0.013 \text{ ps}$$

$$\tau(B^0) = 1.511 \pm 0.023 \pm 0.013 \text{ ps}$$

$$\tau(B_s) = 1.598 \pm 0.097 \pm 0.017 \text{ ps}$$



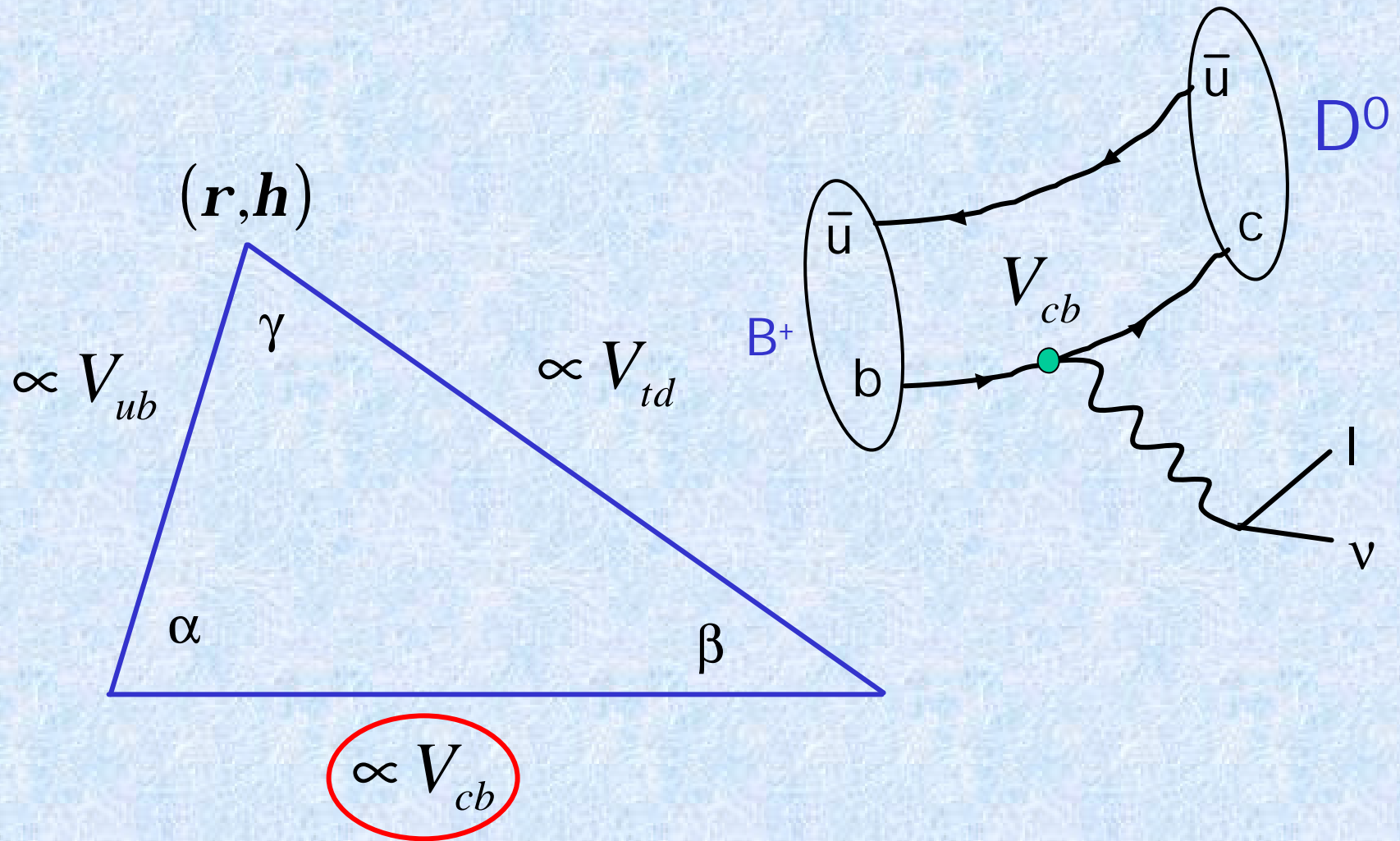
## Systematics ( $\mu\text{m}$ )



Effect	Variation( $\mu\text{m}$ ) $B^0$	Variation( $\mu\text{m}$ ) $B_s$
MC input $c\tau$	negligible	negligible
$p_T$ reweight	1.9	1.9
Scale Factor	negligible	negligible
Bkg $ct$ description	1.1	1.1
Bkg fraction	2.0	2.0
I.P. correlation	1.0	1.0
Eff. parameterization	1.5	1.5
$L_{xy}$ significance	negligible	2
$\Delta\Gamma_s$	-	1.0
Alignm. + others	2.4	2.4
Total	4.2	4.7

# Improving SM Tools

# Closing up on CKM



- QCD corrections  $\leftrightarrow$  uncertainty on the  $b$  wave function inside the meson
- This is something that **can be constrained experimentally!**

# Improving phenomenological tools: Hadronic Moments

No room for everything... I will focus on one example:

• **HQET/OPE** is a **fundamental** tool for CKM physics with B mesons. For instance it relates:

- $B \rightarrow X_u \ell \nu$  to  $[b \rightarrow u \ell \nu] \Rightarrow V_{ub}$

- $B \rightarrow X_c \ell \nu$  to  $[b \rightarrow c \ell \nu] \Rightarrow V_{cb}$

- OPE is “semi-empirical”: parameterizes any prediction in a series expansion of **effective operators**

- Expectation value of these operators is a “universal” property of the theory which can be assessed with concurrent measurements

- Example:  $V_{cb} (\pm 1\%_{\text{exp}} \pm 2.5\%_{\text{theo}}) \Leftrightarrow$  Hadronic Moments



# Moments-ology

Many inclusive observables can be written using the same expansion  
(same non-perturbative parameters). The spectral moments:

- Photonic moments: Photon energy in  $b \rightarrow s \gamma$  (CLEO)
- Leptonic moments:  $B \rightarrow X_c l \nu$ , lepton  $E$  in  $B$  rest frame (CLEO, DELPHI, BABAR)
- Hadronic moments:  $B \rightarrow X_c l \nu$ , recoil mass  $M(X_c)$  (CLEO, DELPHI, BABAR, CDF II)

$$M_1 = \int_{s_H^{\min}}^{s_H^{\max}} ds_H (s_H - \bar{m}_D^2) \frac{1}{\Gamma_{sl}} \frac{d\Gamma_{sl}}{ds_H} = \langle s_H \rangle - \bar{m}_D^2, \quad s_H \equiv M_{X_c}^2$$
$$M_2 = \int_{s_H^{\min}}^{s_H^{\max}} ds_H (s_H - \langle s_H \rangle)^2 \frac{1}{\Gamma_{sl}} \frac{d\Gamma_{sl}}{ds_H} = \langle (s_H - \bar{m}_D^2)^2 \rangle - M_1^2$$

**Aim:** Constrain the unknown non-pert. parameters and reduce  $|V_{cb}|$  uncertainty.

With enough measurements: test of underlying assumptions (duality...).

# What is $X_c$ ?

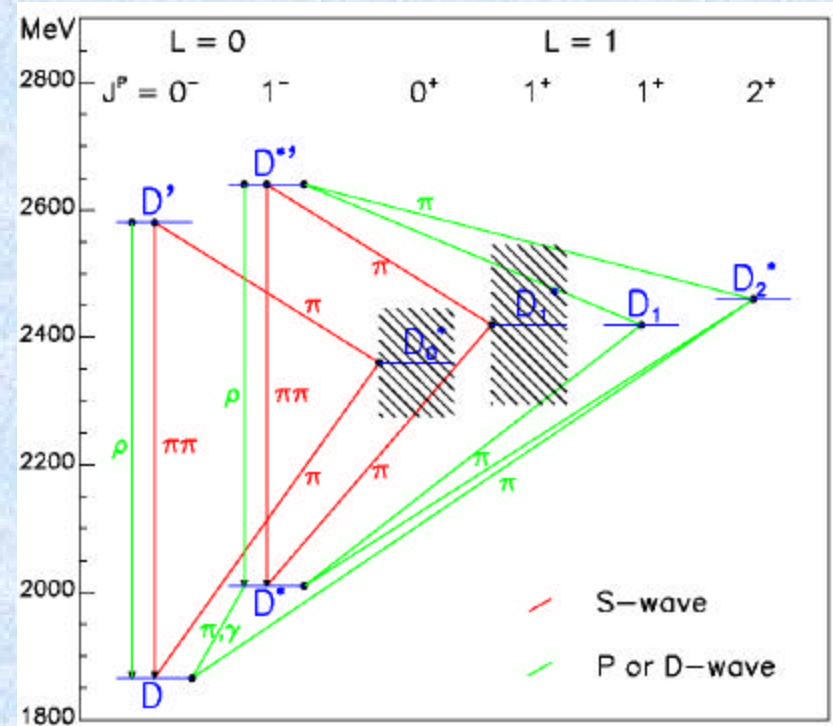
Semi-leptonic widths (PDG 04):

	Br (%)
$B^+ \rightarrow X_c   n$	$10.99 \pm 0.31$
$B^+ \rightarrow D^*   n$	$6.04 \pm 0.23$
$B^+ \rightarrow D   n$	$2.23 \pm 0.15$

(PDG b/B<sup>+</sup>/B<sup>0</sup> combination, b→u subtracted)

→ ~25% of semi-leptonic width is poorly known

Higher mass states: D<sup>\*\*</sup>



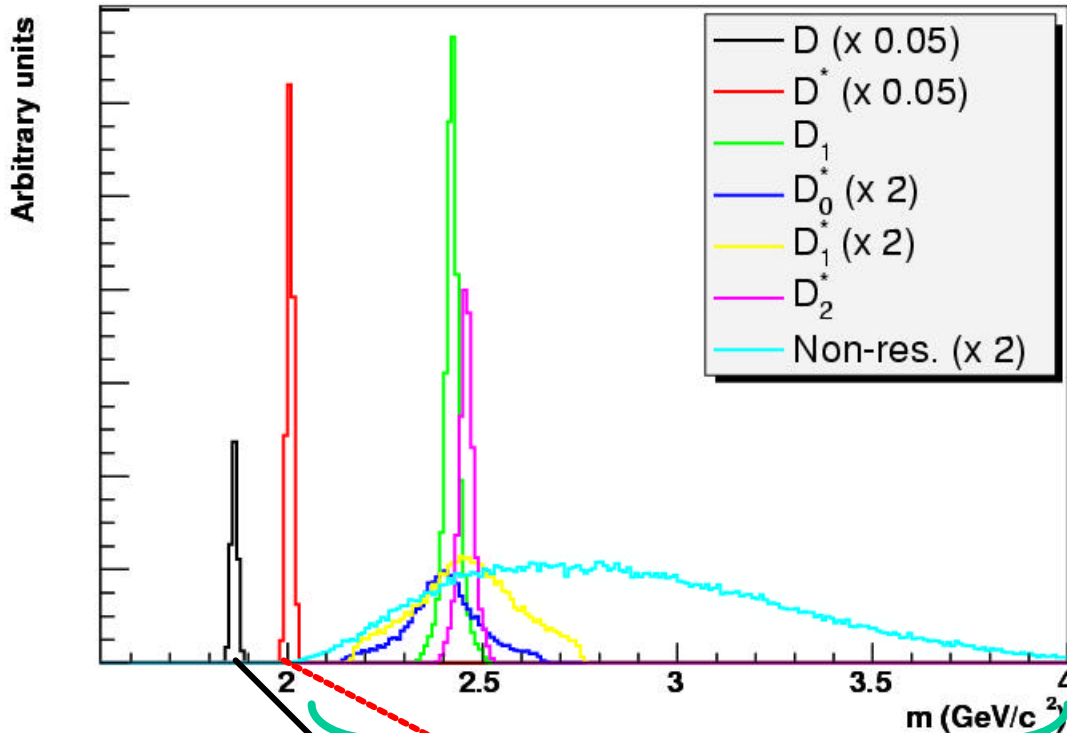
Possible  $D' \rightarrow D^{(*)} \pi \pi$  contributions neglected:

- No  $B \rightarrow ID'$  experimental evidence so far
- DELPHI limit:  $\begin{cases} BR(b \rightarrow D^+ p^+ p^- \ell^- n) < 0.18\% @ 90\% CL \\ BR(b \rightarrow D^{*+} p^+ p^- \ell^- n) < 0.17\% @ 90\% CL \end{cases}$

We assume no D' contribution in our sample

# Analysis Strategy

Typical mass spectrum  $M(X_c^0)$  (Monte Carlo):



$D^0$  and  $D^{*0}$  well-known  
 → measure only  $f^{**}$   
 → only shape needed

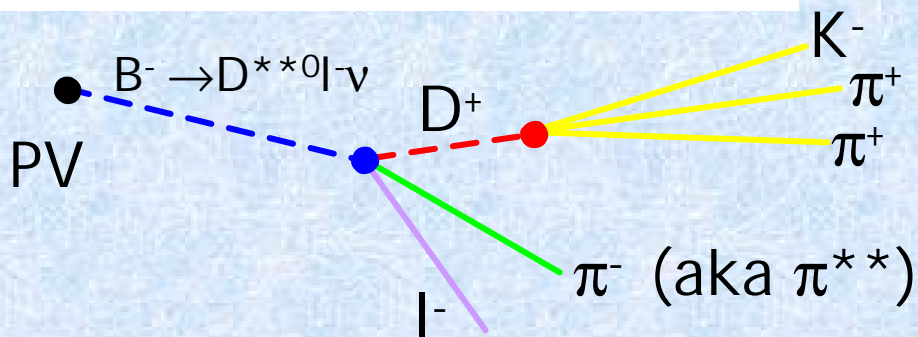
- 1) Measure  $f^{**}(s_H)$
- 2) Correct for background, acceptances, bias  
 → moments of  $D^{**}$
- 3) Add  $D$  and  $D^*$  →  $M_1, M_2$
- 4) Extract OPE parameters ( $L, l_1$ )

$$s_H \equiv M_{X_c}^2$$

$$\frac{1}{\Gamma_{sl}} \frac{d\Gamma_{sl}}{ds_H} = \frac{\Gamma_0}{\Gamma_{sl}} \delta(s_H - m_{D^0}^2) + \frac{\Gamma^*}{\Gamma_{sl}} \delta(s_H - m_{D^{*0}}^2) + \left(1 - \frac{\Gamma_0}{\Gamma_{sl}} - \frac{\Gamma^*}{\Gamma_{sl}}\right) \cdot f^{**}(s_H)$$

# D<sup>+</sup>/D<sup>\*+</sup> Reconstruction

Exclusive reconstruction of D<sup>\*\*</sup>:



$$D^{**0} \rightarrow D^{*+} \pi^{*-}$$

$$\hookrightarrow D^0 \pi^{*+}$$

(Br=67.7%)

$$\hookrightarrow K^- \pi^+$$

(Br=3.8%)

$$\hookrightarrow K^- \pi^+ \pi^- \pi^+$$

(Br=7.5%)

$$\hookrightarrow K^- \pi^+ \pi^0$$

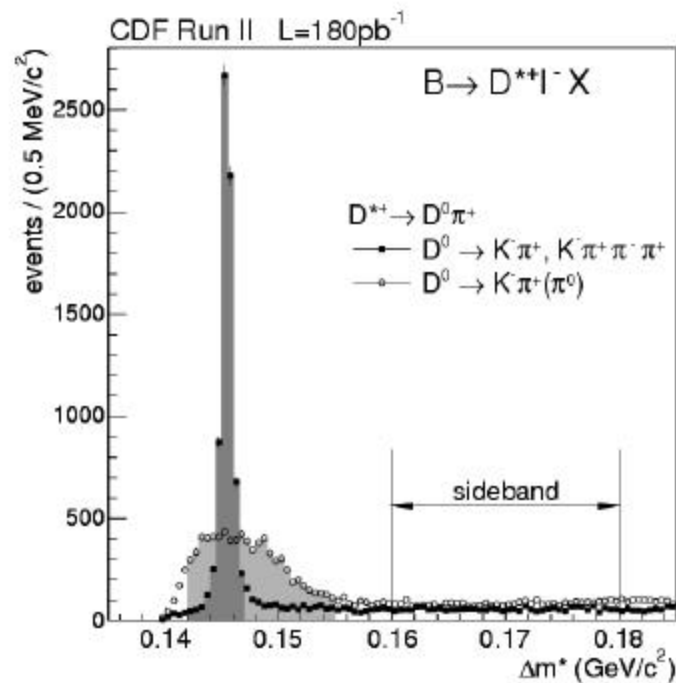
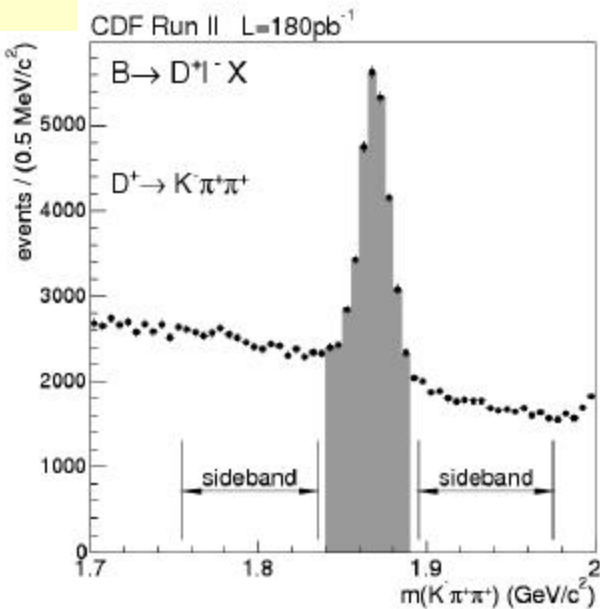
(Br=13.0%)

"D<sup>\*+</sup>"

$$D^{**0} \rightarrow D^+ \pi^{*-}$$

$$\hookrightarrow K^- \pi^+ \pi^+ \quad (\text{Br}=9.2\%)$$

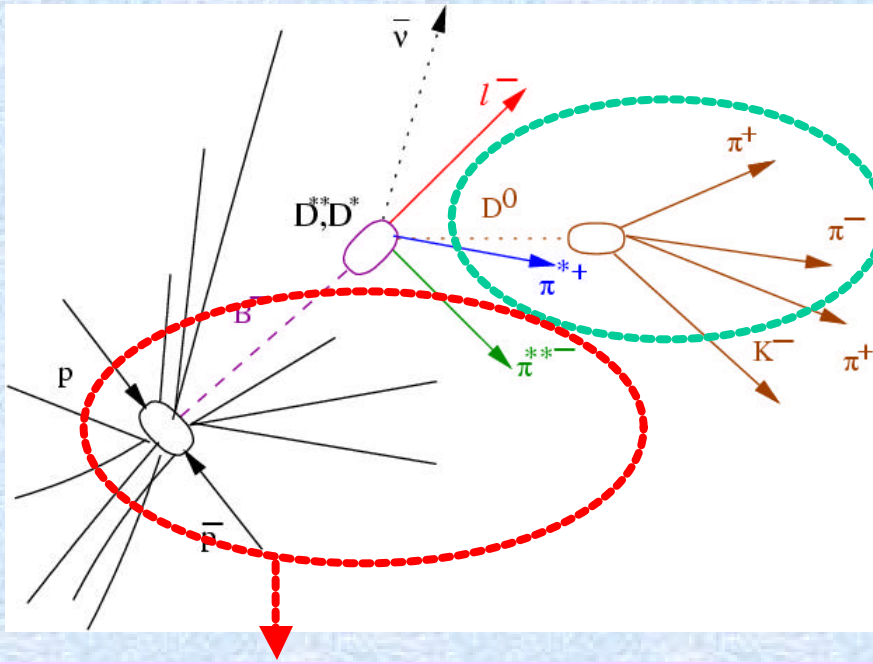
"D<sup>+</sup>"



~28K e/ $\mu$ D Candidates in total!



# Backgrounds



Physics background:  
 $B \rightarrow D^{(*)+} D_s^-$ ,  $D_{(s)} \rightarrow X l \nu$   
 $\rightarrow$  MC, subtracted

Combinatorial background under the  $D^{(*)}$  peaks:  
 $\rightarrow$  sideband subtraction

Feed-down in signal:  
 $D^{**0} \rightarrow D^{*+} (\rightarrow D^+ \pi^0) \pi^-$   
 irreducible background to  
 $D^{**0} \rightarrow D^+ \pi^-$ .

$\rightarrow$  subtracted using data:  
 $\rightarrow$  shape from  $D^0 \pi^-$  in  
 $D^{**0} \rightarrow D^{*+} (\rightarrow D^0 \pi^+) \pi^-$   
 $\rightarrow$  rate:  
 $\frac{1}{2}$  (isospin) x eff. x BR

Prompt pions faking  $\pi^{**}$ :

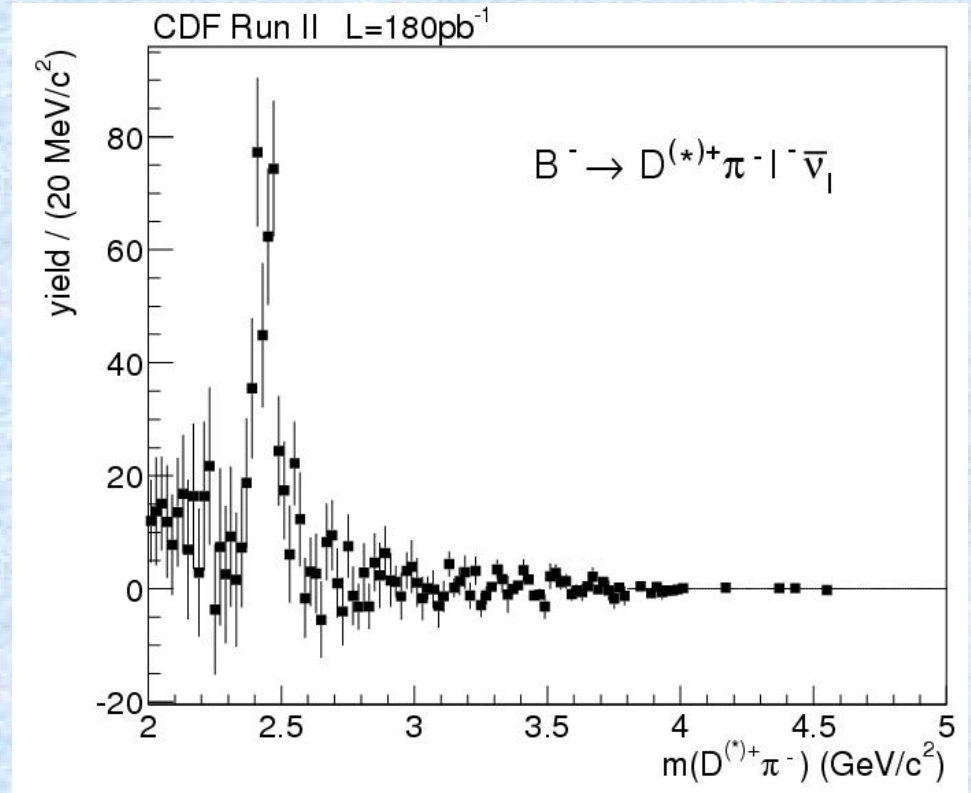
- **fragmentation**
- **underlying event**
- $\rightarrow$  **separate B and primary vertices**  
 (kills also prompt charm)
- $\rightarrow$  use impact parameters to discriminate
- $\rightarrow$  model: wrong-sign  $\pi^{**+} l^-$  combinations

# Corrected Mass and $D^{**}$ moments

## Procedure:

- Unbinned procedure using weighted events.
- Assign negative weights to background samples.
- Propagate efficiency corrections to weights.
- Take care of the  $D^+ / D^{*+}$  relative normalization.
- Compute mean and sigma of distribution.

## Results (in paper):



$$m_1 = \langle m_{D^{**}}^2 \rangle = (5.83 \pm 0.16_{stat}) \text{GeV}^2$$

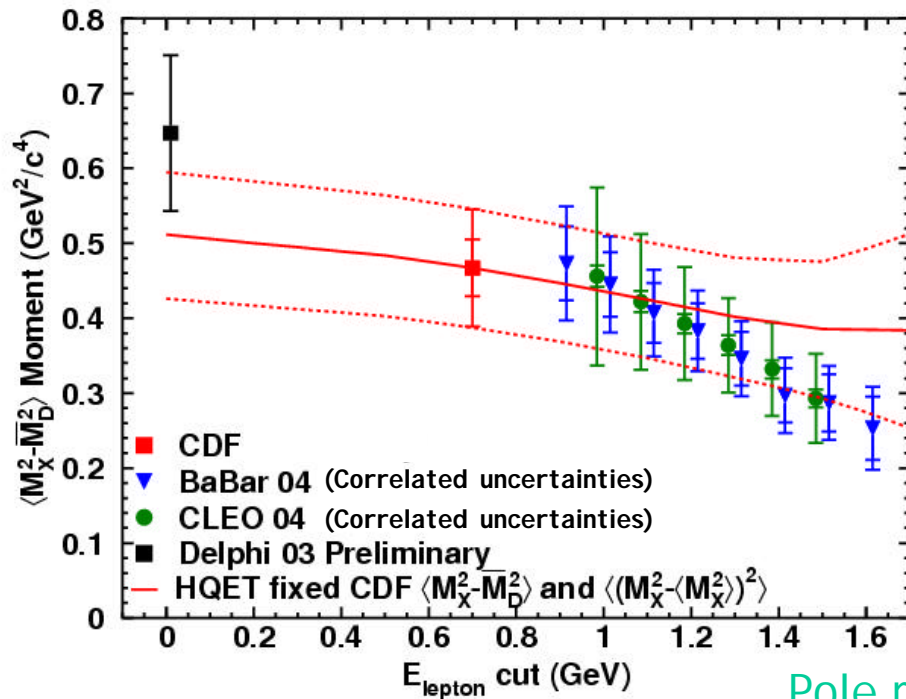
$$m_2 = \langle (m_{D^{**}}^2 - m_1)^2 \rangle = (1.30 \pm 0.69_{stat}) \text{GeV}^4$$

**No Fit !!!**

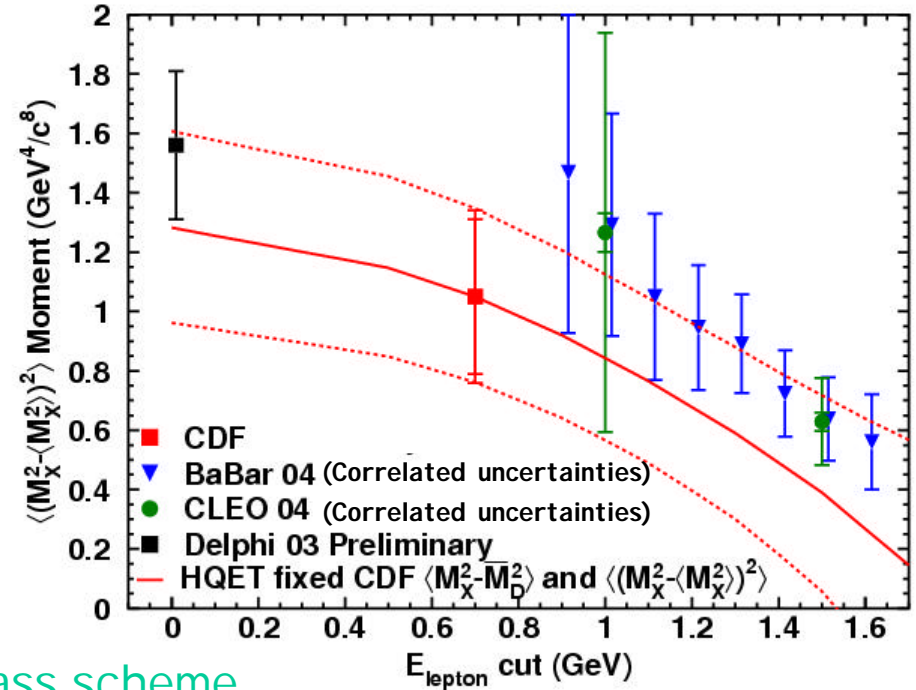
# Systematic Errors

	$\Delta m_1$ (GeV <sup>2</sup> )	$\Delta m_2$ (GeV <sup>4</sup> )	$\Delta M_1$ (GeV <sup>2</sup> )	$\Delta M_2$ (GeV <sup>4</sup> )	$\Delta \Lambda$ (GeV)	$\Delta \lambda_1$ (GeV <sup>2</sup> )
Stat.	0.16	0.69	0.038	0.26	0.078	0.057
Syst.	0.08	0.22	0.068	0.13	0.091	0.082
Mass resolution	0.02	0.13	0.005	0.04	0.012	0.009
Eff. Corr. (data)	0.03	0.13	0.006	0.05	0.014	0.011
Eff. Corr. (MC)	0.06	0.05	0.016	0.03	0.017	0.006
Bkgd. (scale)	0.01	0.03	0.002	0.01	0.003	0.002
Bkgd. (opt. Bias)	0.02	0.10	0.004	0.03	0.006	0.006
Physics bkgd.	0.01	0.02	0.002	0.01	0.004	0.002
D <sup>+</sup> / D <sup>*+</sup> BR	0.01	0.02	0.002	0.01	0.004	0.002
D <sup>+</sup> / D <sup>*+</sup> Eff.	0.02	0.03	0.004	0.01	0.005	0.002
Semileptonic BRs			0.065	0.10	0.064	0.022
$\rho_1$					0.041	0.069
$T_i$					0.032	0.031
$\alpha_s$					0.018	0.007
$m_b, m_c$					0.001	0.008
Choice of $p_1^*$ cut					0.019	0.009

# Results & Comparison with other experiments



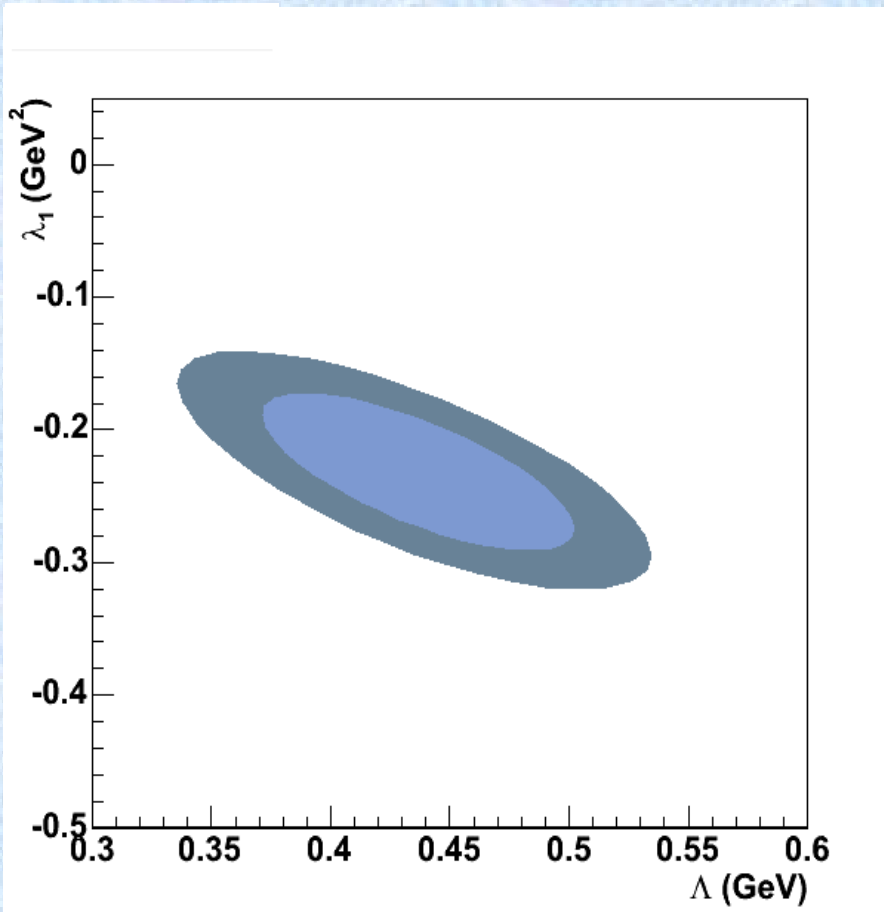
Pole mass scheme



- Good agreement with HQET  $\oplus$  previous determinations.
- First measurement at hadron machines: different environment and experimental techniques.
- Competitive with other experiments.

- **Little model dependency.** No assumptions on shape or rate of  $D^{**}$  components.
- Through integration with other experiments and other "moments" **we can seriously probe HQET/QHD**

# Extraction of the HQE Parameters

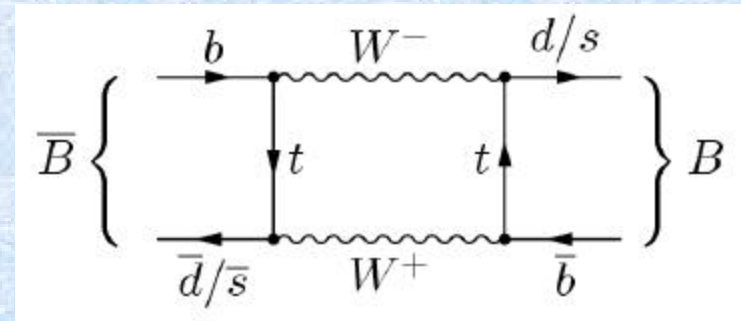
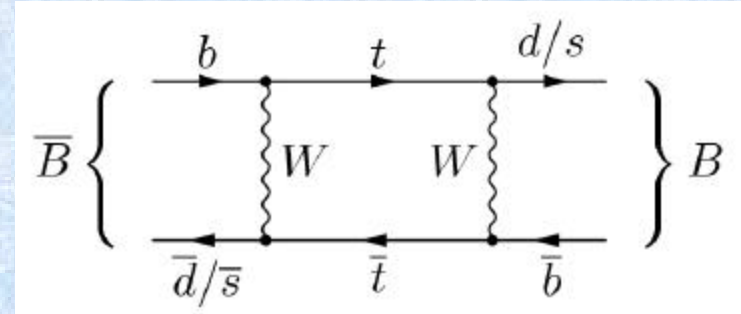
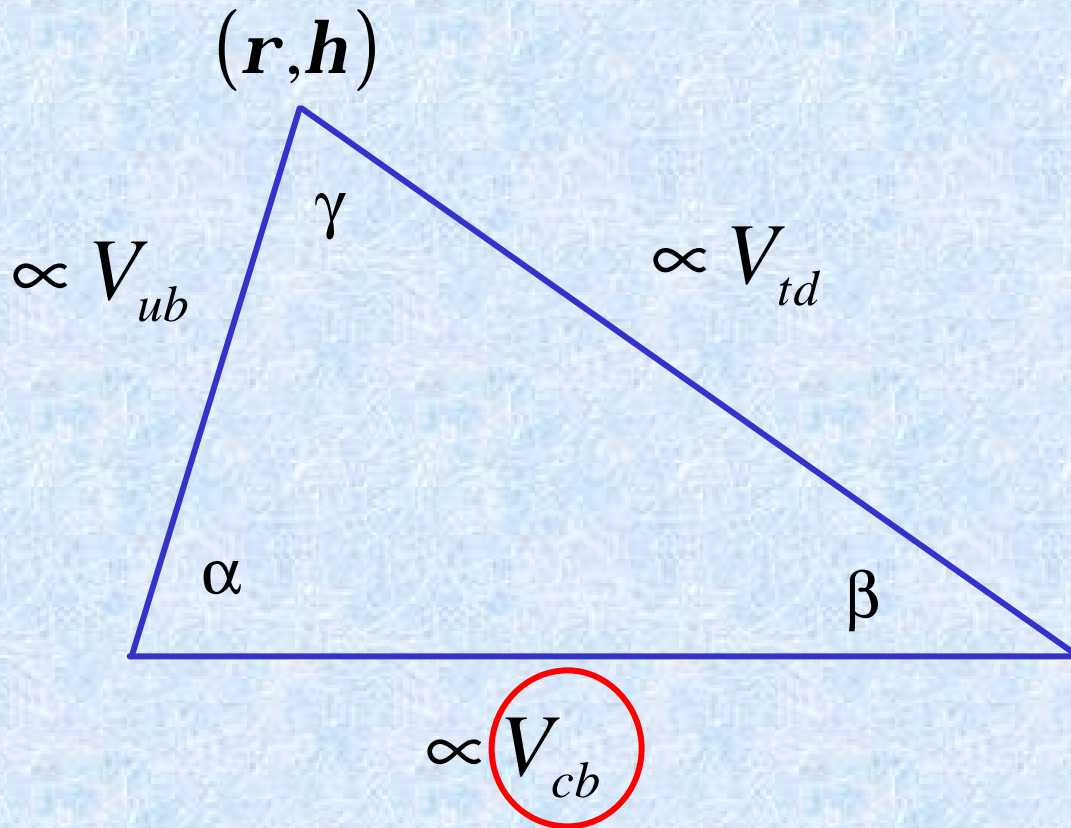


- Combination of all the experimental measurements of the hadronic moments
- Effective determination of the two OPE operators relevant at order  $1/m_B$  ( $\Lambda$ )  $1/m_B^2$  ( $\lambda_1$ )
- CDF contributes as much as the B factories in this determination!



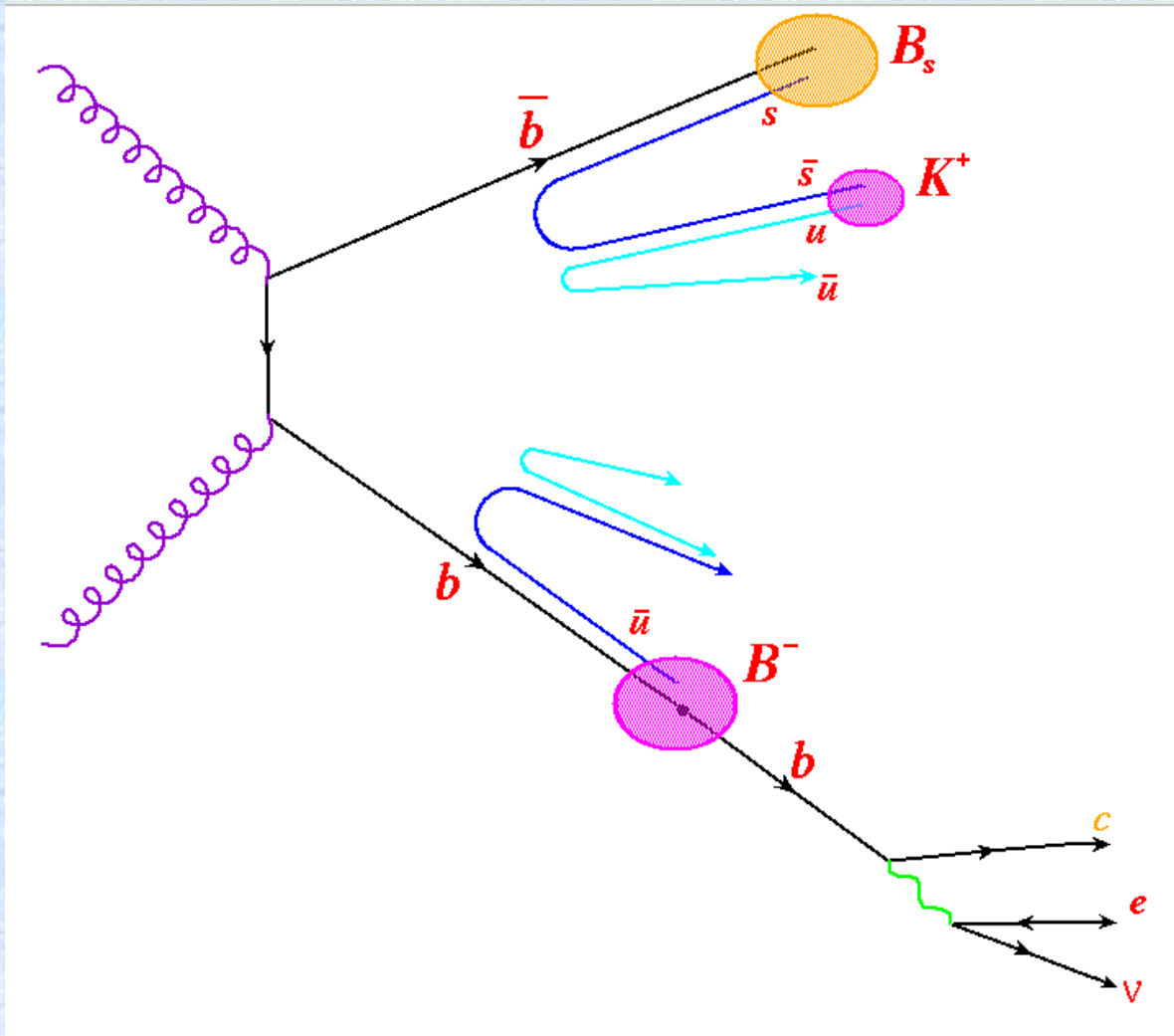
# $B_s$ Mixing

# Working our way on CKM sides



- $V_{td}$  is derived from mixing effects
- QCD uncertainty is factored out in this case resorting to the relative Bs/Bd mixing rate ( $V_{td}/V_{ts}$ )
- Beyond the SM physics could enter in loops!

# B production at the TeVatron



- Production:  $gg \rightarrow b\bar{b}$
- NO QM coherence, unlike B factories
- Opposite flavor at production  $\rightarrow$  one of the  $b$  quarks can be determined to assess the flavor of the other at production
- Fragmentation products have some memory of  $b$  flavor as well

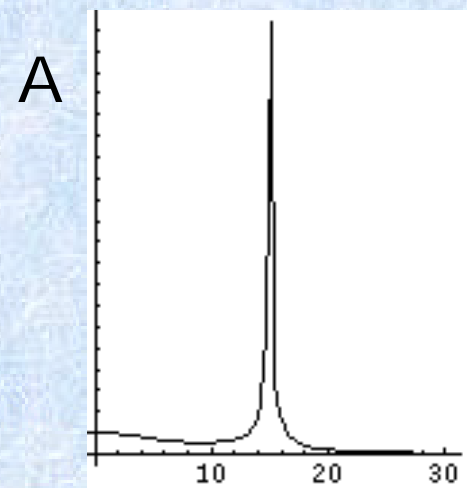
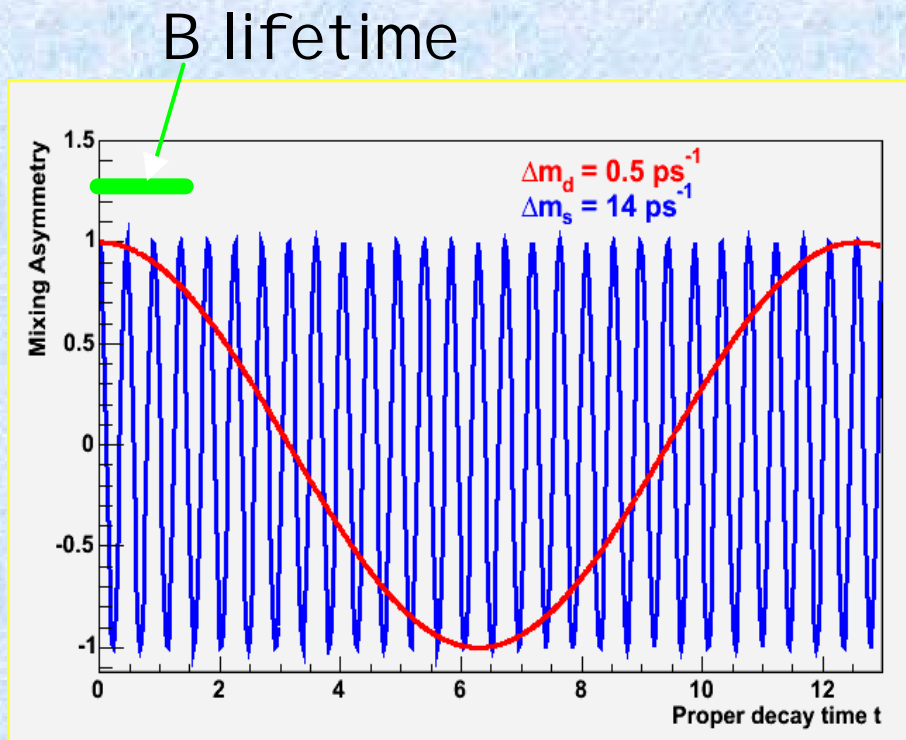
# B<sub>s</sub> Mixing 101

$$A = \frac{N_{\text{unmix}} - N_{\text{mix}}}{N_{\text{unmix}} + N_{\text{mix}}}$$

- $\Delta m_s \gg \Delta m_d$

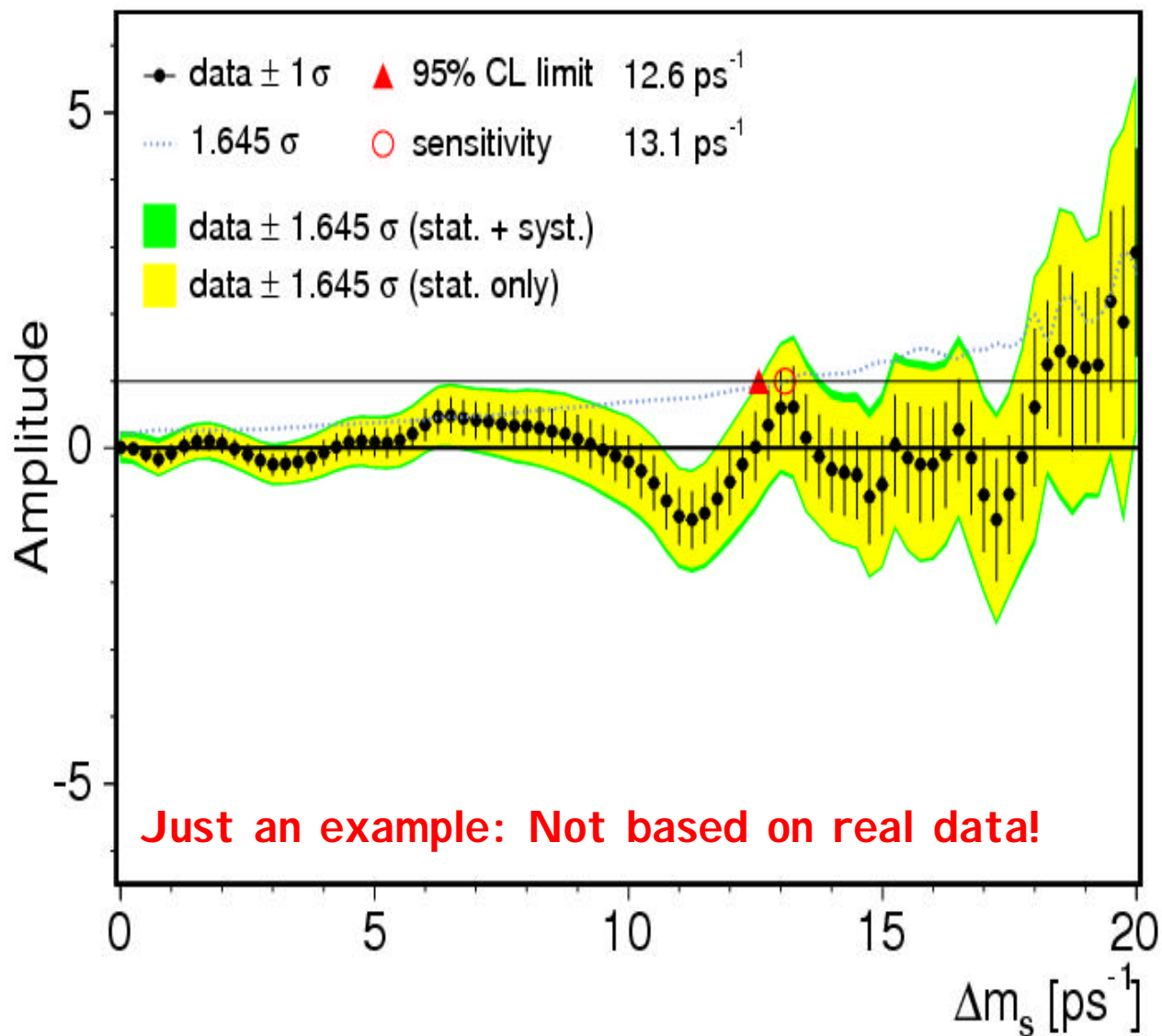
- Different oscillation regime → Amplitude Scan

Perform a 'fourier transform' rather than fit for frequency



$\Delta m_s \text{ [ps}^{-1}\text{]}$

# Amplitude Scan

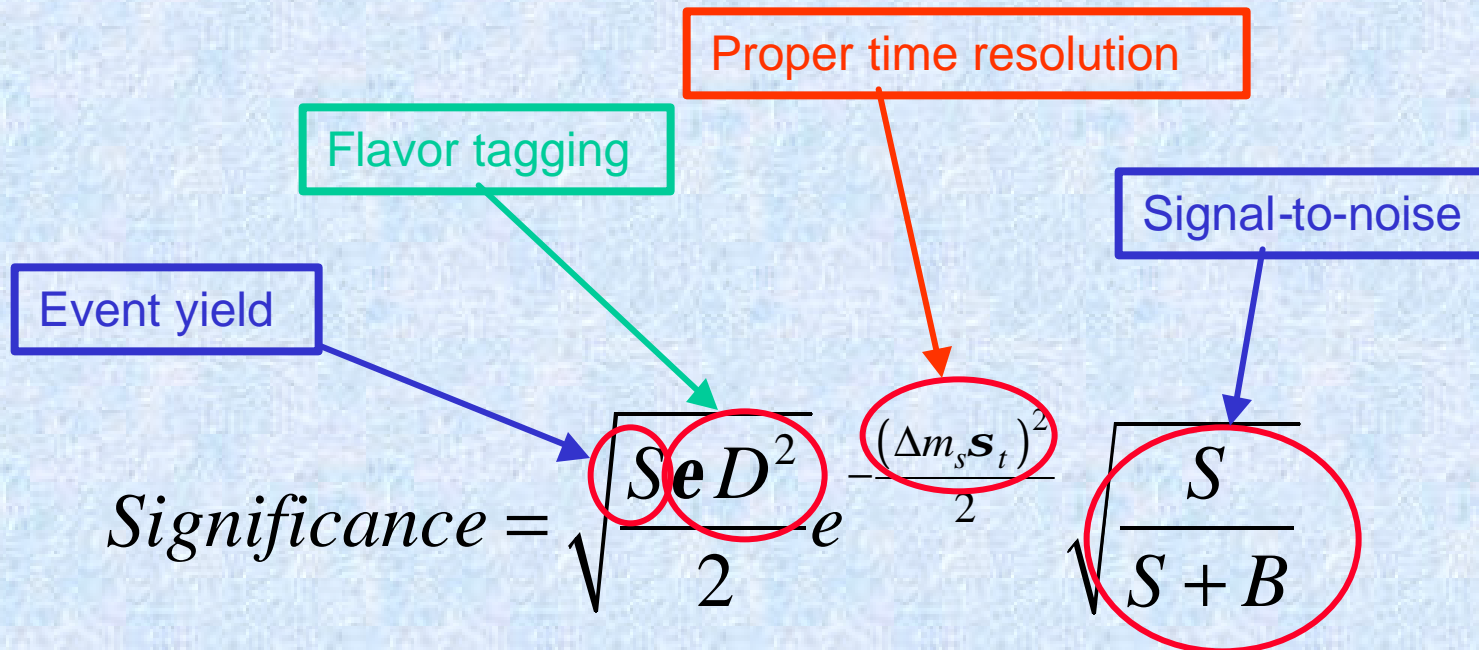


- Mixing amplitude fitted for each (fixed) value of  $\Delta m$
- On average every  $\Delta m$  value (except the true  $\Delta m$ ) will be 0
- “sensitivity” defined for the average experiment [mean 0]
- The actual experiment will have statistical fluctuations
- Actual limit for the actual experiment defined by the systematic band centered at the measured asymmetry





# $B_s$ Mixing Ingredients

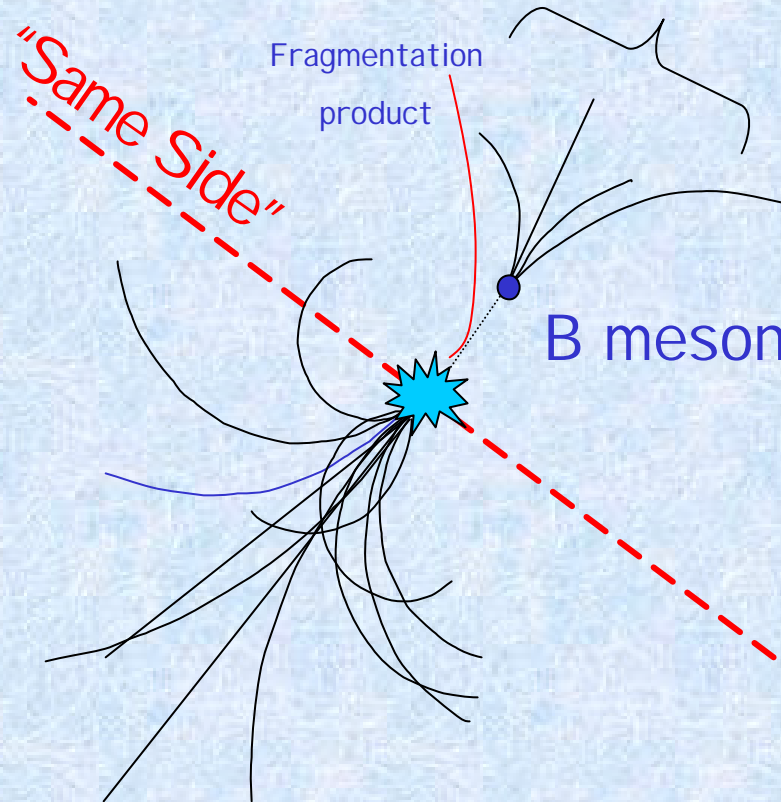


# Flavor Tagging

$$\text{Significance} = \sqrt{\frac{SeD^2}{2}} e^{-\frac{(\Delta m_s \mathcal{S}_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

$$A = \frac{N_{\text{unmix}} - N_{\text{mix}}}{N_{\text{unmix}} + N_{\text{mix}}}$$

Reconstructed decay



Several methods, none is perfect !!!

# $B_s$ Mixing: tagging performance

Measured from  $B_d$  data!

Summer '04	$\epsilon D^2$ Hadronic (%)	$\epsilon D^2$ Semileptonic (%)
Muon	$0.46 \pm 0.11 \pm 0.03$	$0.577 \pm 0.047 \pm 0.034$
Electron	$0.18 \pm 0.06 \pm 0.02$	$0.293 \pm 0.033 \pm 0.017$
JQ/Vertex	$0.14 \pm 0.07 \pm 0.01$	$0.263 \pm 0.035 \pm 0.021$
JQ/Prob.	$0.11 \pm 0.06 \pm 0.01$	$0.150 \pm 0.026 \pm 0.015$
JQ/High $p_T$	$0.24 \pm 0.09 \pm 0.01$	$0.157 \pm 0.027 \pm 0.015$
Total	$1.12 \pm 0.18$	$1.429 \pm 0.093$

- convention: first uncertainty is statistical, second is systematic
- use exclusive combination of tags
- results for hadronic and semileptonic comparable within errors
- use calibration derived from appropriate sample (ie hadronic for  $D_s \pi$ )

Fall '05 (mostly re-optimize existing taggers):

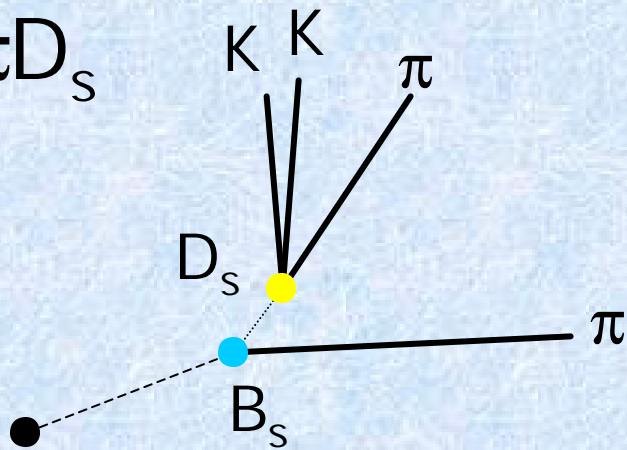
•  $1.12 \pm 0.18 \rightarrow 1.55 \pm 0.16$

•  $1.43 \pm 0.093 \rightarrow 1.55 \pm 0.085$

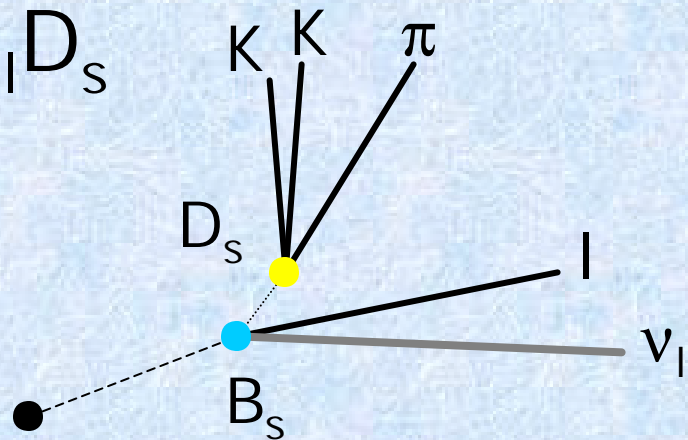
# Proper time resolution

$$\text{Significance} = \sqrt{\frac{SeD^2}{2}} e^{-\frac{(\Delta m \cdot \mathbf{s}_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

$B_s \rightarrow \pi D_s$



$B_s \rightarrow l \nu_l D_s$



$$ct = \frac{L_{xy}}{(bg)} = \frac{L_{xy} m_B}{p_T}$$

$$\mathbf{s}_{ct} = \frac{m_B}{p_T} \mathbf{s}_{L_{xy}} \oplus ct \left( \frac{\mathbf{s}_{p_T}}{p_T} \right)$$

~0.5%

~15%

$$ct = \frac{m_B L_{xy}}{P_t(lD_s)} \cdot \left\langle \frac{P_t(lD_s)}{P_t(B_s)} \right\rangle_{mc}$$

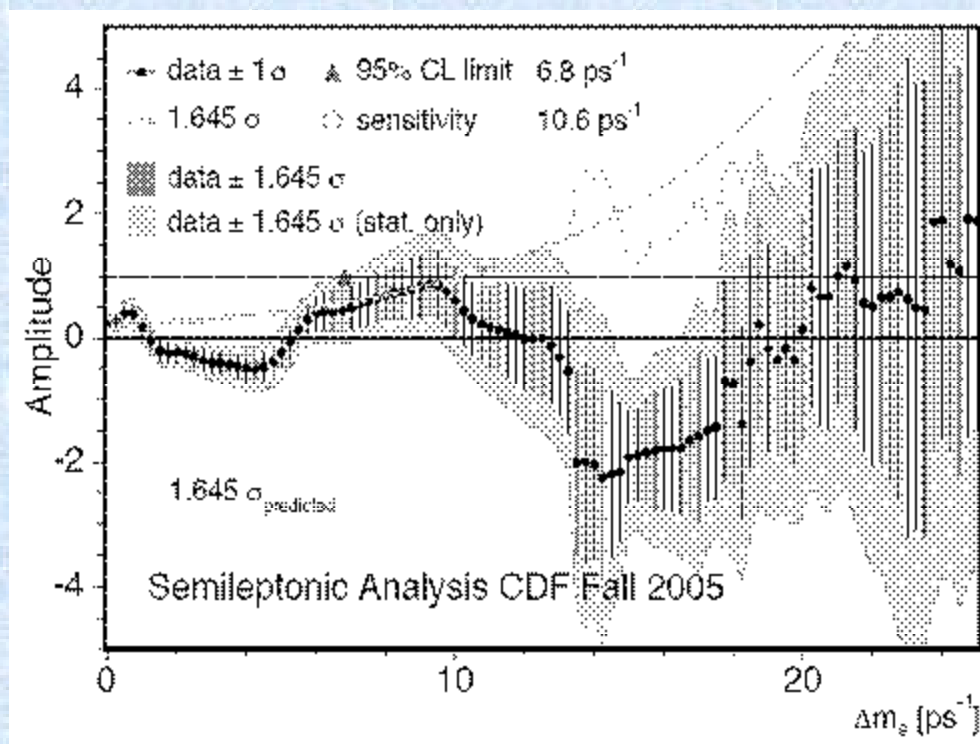
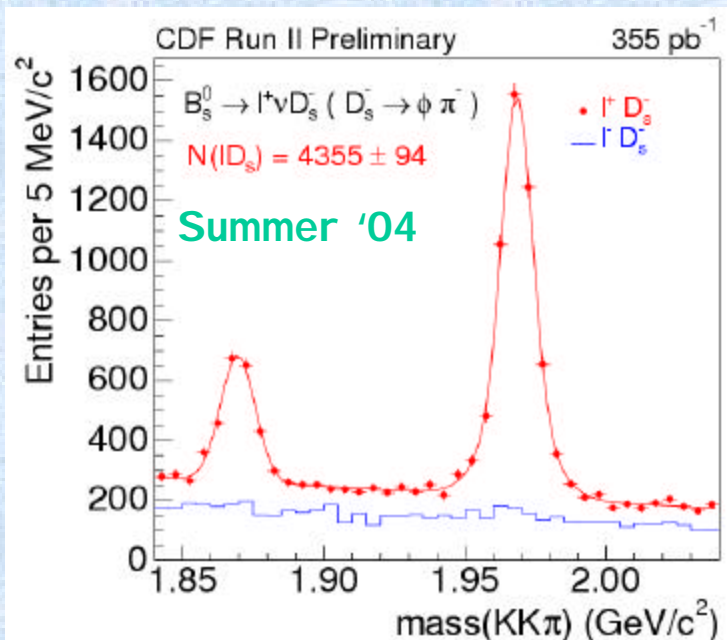
$$\mathbf{s}_{ct} = \frac{m_B}{P_t} \mathbf{s}_{L_{xy}} \oplus ct \left( \frac{\mathbf{s}_{P_t}}{P_t} \right) \otimes \mathbf{s}_K$$

Semileptonic modes: **momentum** uncertainty

Fully reconstructed: **L<sub>xy</sub>** uncertainty → improve reconstruction

# $B_s$ Mixing: semileptonic

- $B_s \rightarrow D_s l \nu$  Yield s/b
- $D_s \rightarrow \phi \pi$  (4350 ± 100 3.1)
- $D_s \rightarrow K^* K$  (1750 ± 80 0.42)
- $D_s \rightarrow \pi \pi \pi$  (1570 ± 90 0.32)



$\Delta m_s > 6.8 \text{ ps}^{-1}$  @ 95% CL

Sensitivity: 10.6 ps<sup>-1</sup>

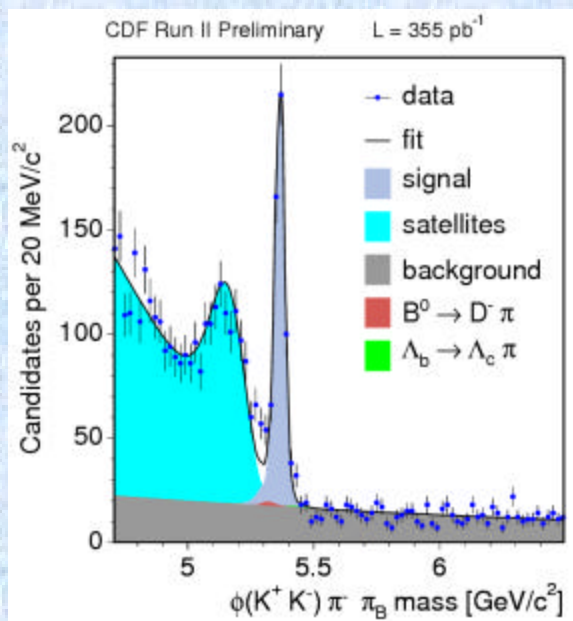
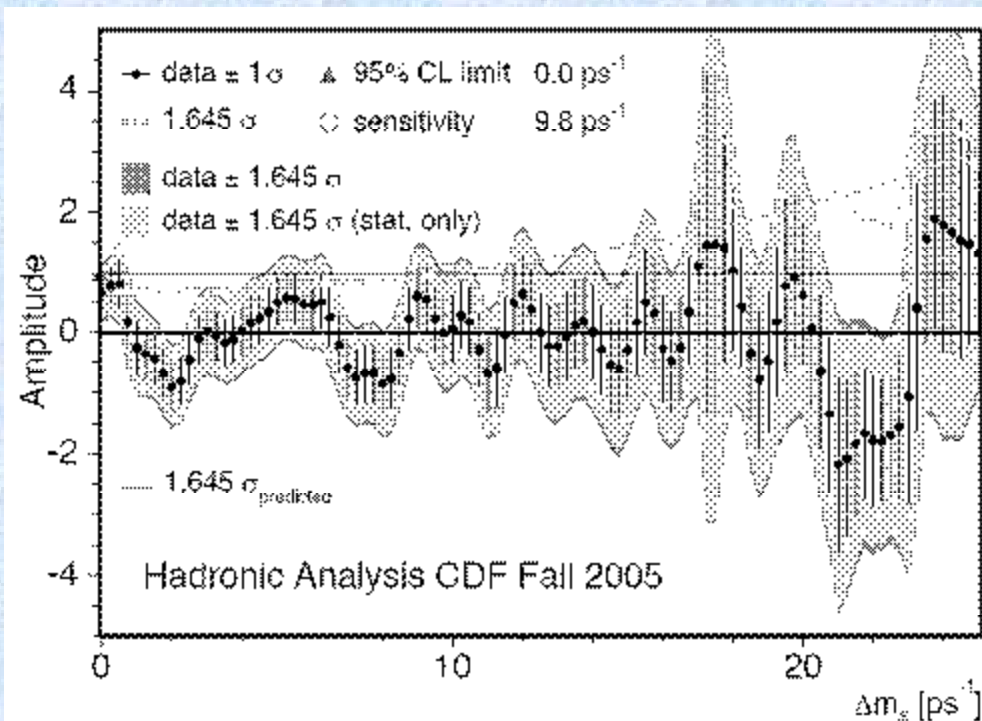
Reach at large  $\Delta m_s$  limited by incomplete reconstruction ( $\sigma_{ct}$ )!



# $B_S$ Mixing: hadronic

- $B_S \rightarrow D_S \pi$  Yield s/b
- $D_S \rightarrow \phi \pi$  ( $550 \pm 40$  ~1.8)
- $D_S \rightarrow K^* K$  ( $240 \pm 40$  ~1.7)
- $D_S \rightarrow \pi \pi \pi$  ( $110 \pm 25$  ~1.0)

• Using also  $B_S \rightarrow D_S \pi \pi \pi$   
[about 1/3 more statistics]

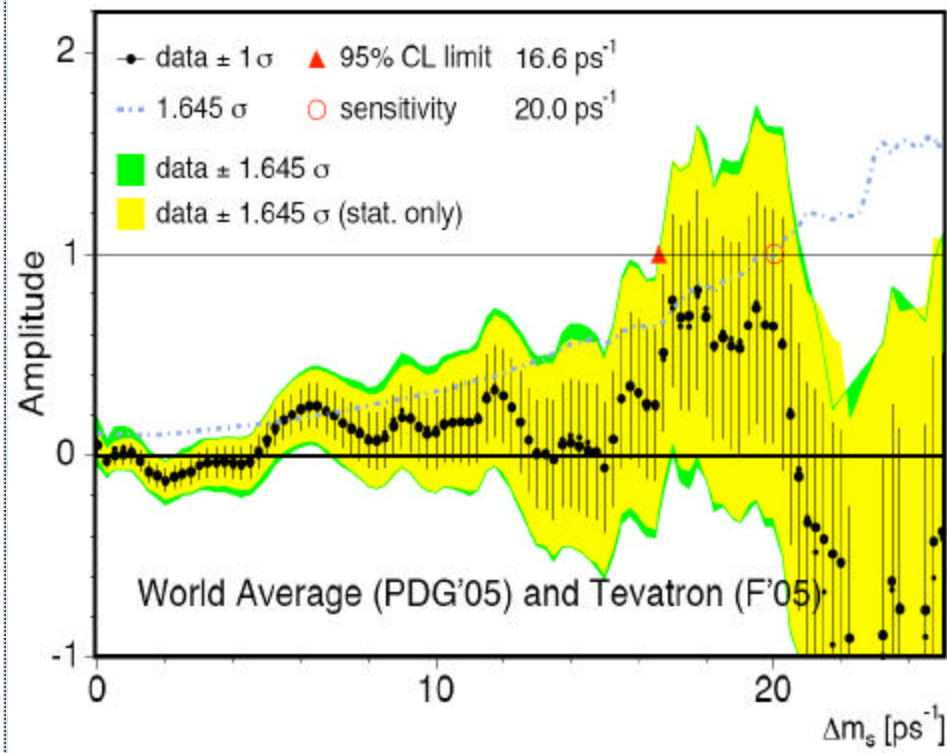
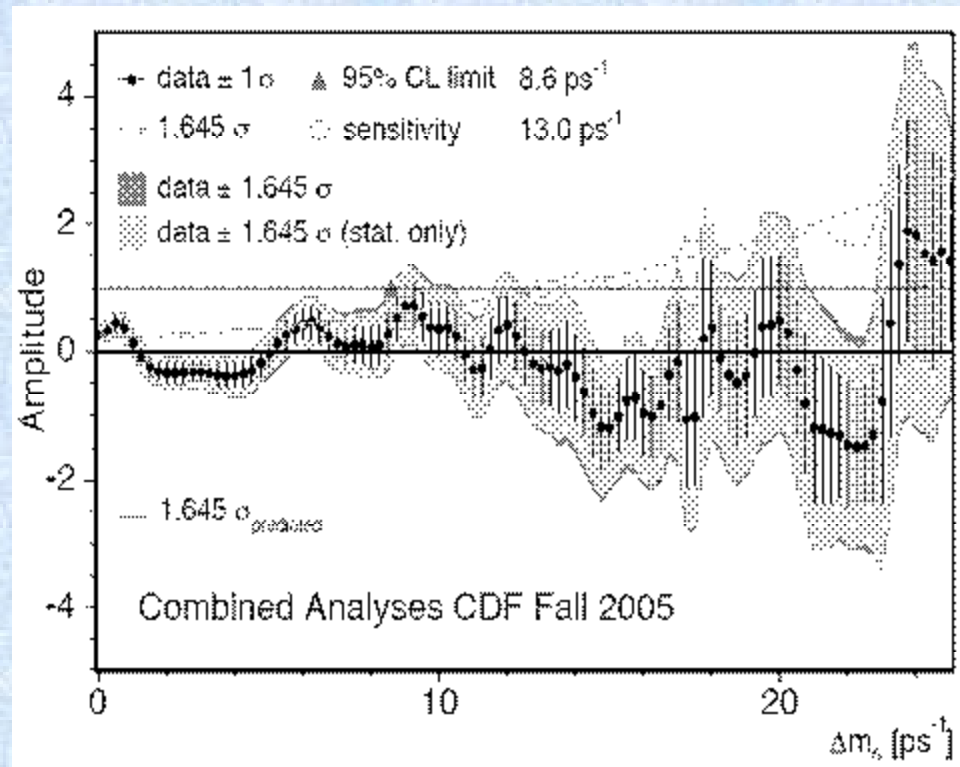


$\Delta m_S > 0.0 \text{ ps}^{-1}$  @ 95% CL

Sensitivity:  $9.8 \text{ ps}^{-1}$

Low statistics, but promising!

# Combined Bs mixing limit



$\Delta m_s > 8.6 \text{ ps}^{-1}$  @ 95% CL

Sensitivity: 13.0  $\text{ps}^{-1}$

**Competitive in precision with best experiment at large  $\Delta m_s$**

$\Delta m_s > 16.6 \text{ ps}^{-1}$  @ 95% CL

Sensitivity: 20.0  $\text{ps}^{-1}$

More statistics and improvements to come...

# $B_s$ Mixing Perspectives

Analysis is pretty much defined! We know where we can improve:

- Statistics

- Data (lumin.:  $350\text{pb}^{-1} \rightarrow 600\text{pb}^{-1} \rightarrow ??$ )

- New Modes (e.g.  $B_s \rightarrow D_s^* \pi > 2x?$ )

- $\epsilon D^2$ :

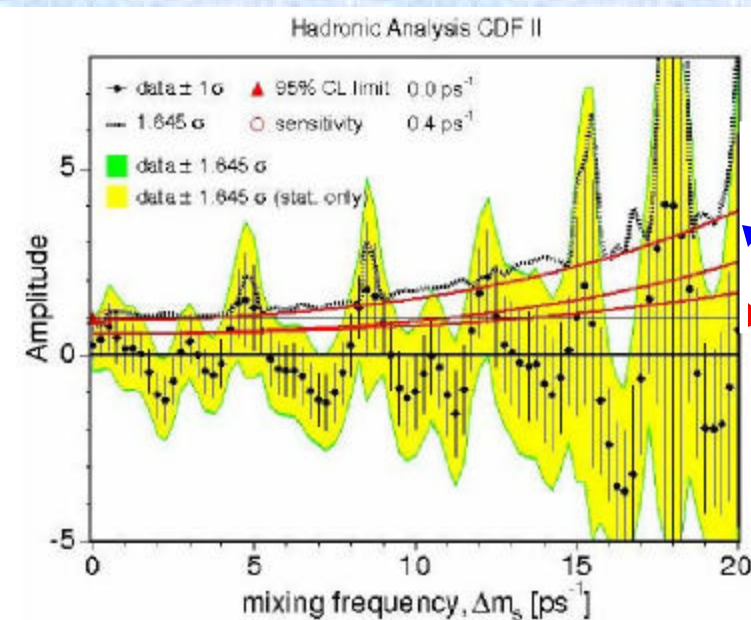
- Additional taggers (SSK, OSK...)

- Improve existing algorithms

- Proper time resolution

- Refine event-by-event reconstruction

- Optimal usage of kinematics for non-closed modes



With the March 2006 data sensitivity  $\sim$  SM value

# What happens for large $x_s$ ?

Indirect Measurement of  $\Delta m_s$ :

$$\left. \frac{\Delta\Gamma_s}{\Delta m_s} \right|_{SM} = \frac{2 m_t^2}{3p m_b^2} \frac{h\left(\frac{m_t^2}{M_W^2}\right)}{\left(1 - \frac{8 m_c^2}{3 m_b^2}\right)} = (3.7^{+0.8}_{-1.5}) \times 10^{-3}$$

-SM  $\Delta\Gamma_s/\Gamma_s = 0.12 \pm 0.06$  (Dunietz, Fleischer & Nierste)

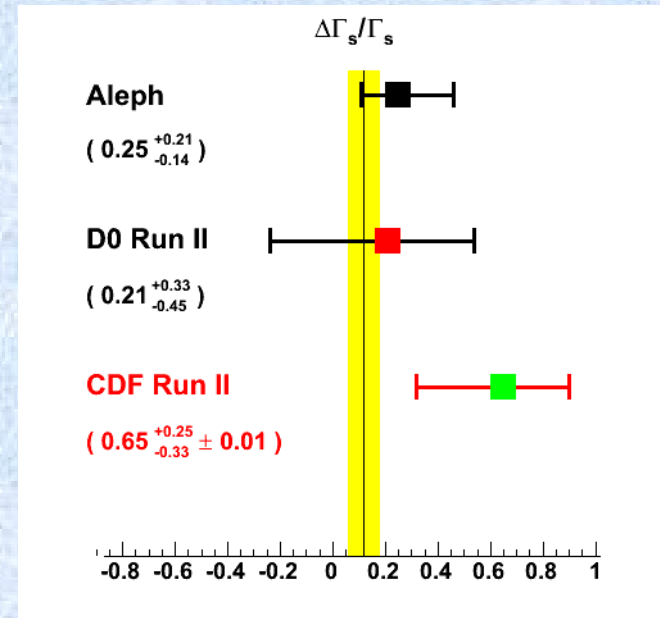
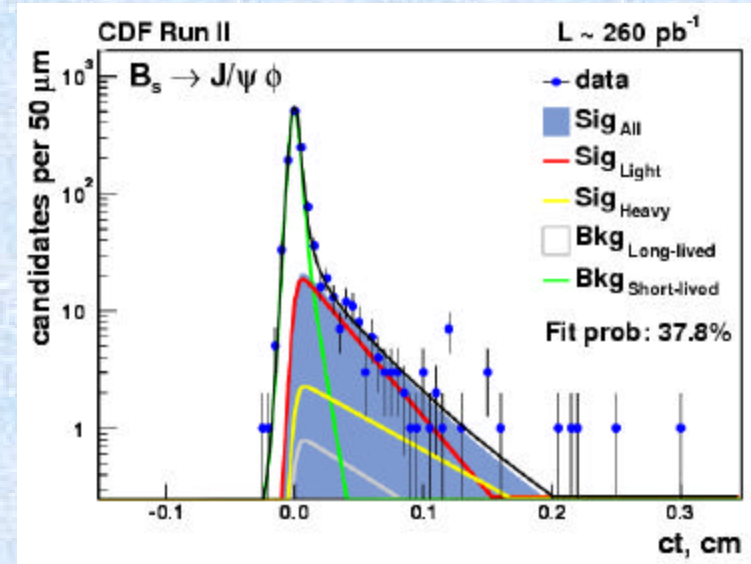


# Probing at large $\Delta m_s$ : $\Delta\Gamma/\Gamma$

- $B_s \rightarrow J/\psi \phi$ 
  - $B \rightarrow VV$ , mixture of CP even/odd separate by angular analysis
  - Combine two-lifetime fit + angular  $\rightarrow \Delta\Gamma_s = \Gamma_H - \Gamma_L$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = 0.65^{+0.25}_{-0.33} \pm 0.01$$

few  $\text{ps}^{-1}$  in  $\Delta m_s$  !



# Beyond the SM

Analyses like this have laid down the path and the tools and techniques for the exploration of the SM boundaries:

- Non SM effects:
  - $b \rightarrow d$  ?
  - $b \rightarrow s$ 
    - Rare decays ( $b \rightarrow s\gamma$ )
      - $B_s \rightarrow \mu\mu, \mu\mu\phi$  etc.
    - $B \rightarrow \phi K$
    - $B_s \rightarrow \phi\phi$
    - $X_s$

# Rare decays

- Exploit the large B production rate
- Measure relative BR (e.g.  $\mu\mu$  to  $J/\psi K$ ) to factor out absolute  $\epsilon$  and luminosity measurements
- SM:  $\text{BR}(B_s \rightarrow \mu\mu) < 3.8\text{E-}9$
- Sensitive to new physics!

## Result: World's best limits

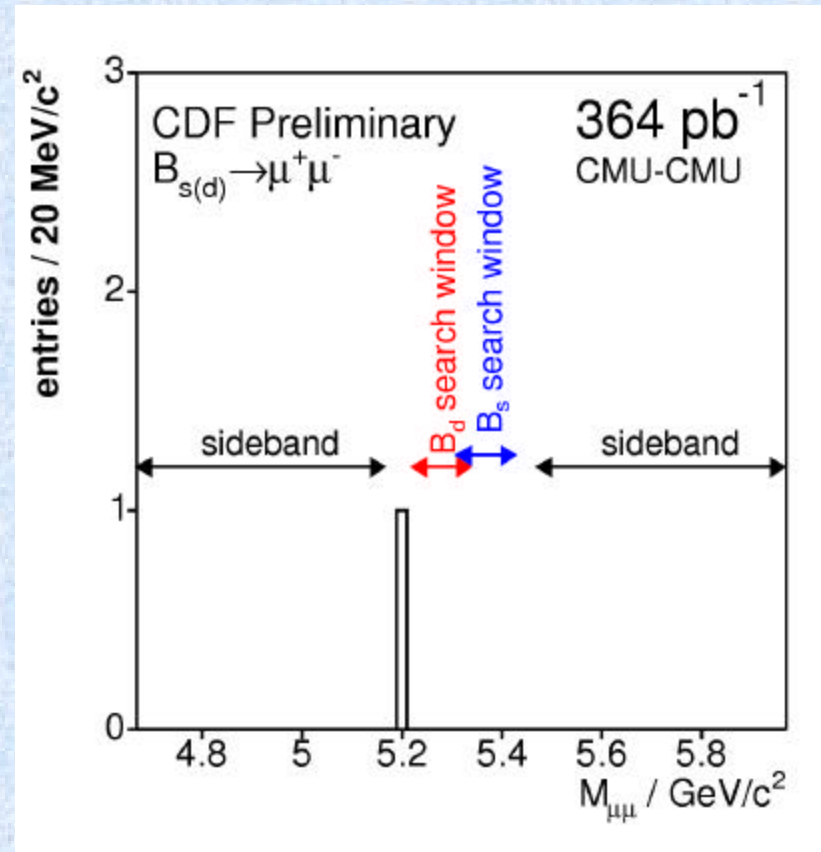
$$\text{BR}(B_s \rightarrow \mu\mu) < 2.0 \times 10^{-7} \text{ @95\% CL}$$

$$\text{BR}(B_d \rightarrow \mu\mu) < 4.9 \times 10^{-8} \text{ @95\% CL}$$

Publ: PRL 93, 032001 2004 Update: Hep-ex/0502044

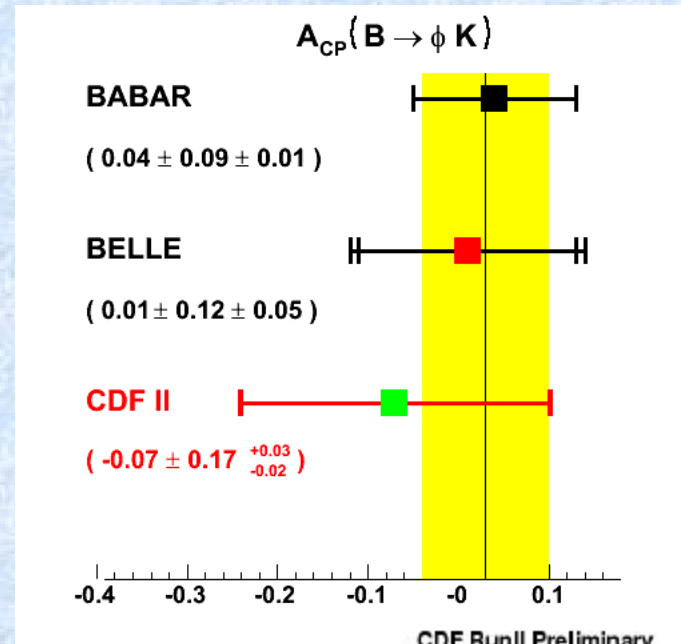
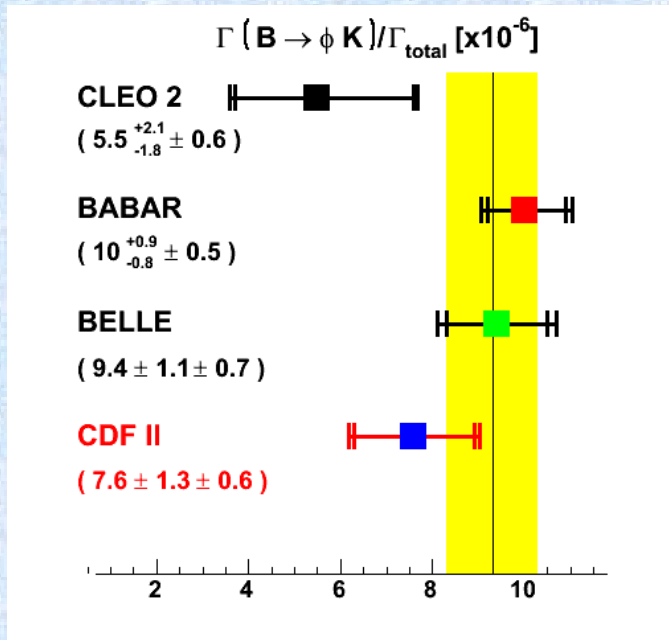
$$\text{BR}(D^0 \rightarrow \mu\mu) \leq 2.4 \times 10^{-6} \text{ at 90\% CL}$$

PRD 68, 091101 2003



# CP: $s\bar{s}s$

- $b \rightarrow sss$  transitions are 'misbehaving' at B factories
- ...CDF II can look at them too. We started from  $\phi K$ :

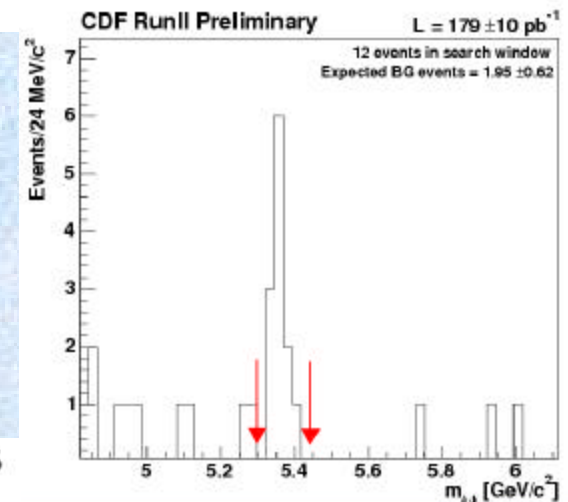


$$\frac{BR(B^\pm \rightarrow \phi K^\pm)}{BR(B^\pm \rightarrow J/\psi K^\pm)} = 0.0076 \pm 0.0013 (stat.) \pm 0.0006 (syst.)$$

$$A_{CP}(B^\pm \rightarrow \phi K^\pm) = -0.07 \pm 0.17 (stat.)^{+0.03}_{-0.02} (syst.)$$

• ...With the advantage of being able to look at  $B_s$  too:

$$BR(B_s \rightarrow \phi\phi) = (1.4 \pm 0.6(stat.) \pm 0.2(syst.) \pm 0.5(BR's)) \cdot 10^{-5}$$



# Perspectives



Exciting times ahead:

- Most analyses sensitive to BSM physics are statistically limited
- Significant improvements can be made including new modes and techniques
- $B_s$  results will be an important complementary addition to the CKM mapping!



# Conclusions

- We are living an exciting transition era of more and more quantitative results in the CKM sector
  - BSM physics could be around the corner, but hard to discern models without direct evidences
  - With LHC we will soon jump in the completely uncharted territory!
  - Living this constant exploration of new discoveries puts us at the forefront of human knowledge, but this is not news!
- “Modern science did not spring perfect and complete, as Athena from the head of Zeus, from the mind of Galileo and Descartes”



Purgatory





# A guiding theme

- Exploring the boundaries of knowledge is a recurrent theme in history
- Geographical explorations exemplify the paradigm:



G. Galilei



# Hadronic Moments, HQET and $V_{cb}$

Most precise determination of  $V_{cb}$  comes from  $\Gamma_{sl}$  ("inclusive" determination):

$$\Gamma_{sl}(b \rightarrow c \ell^- \bar{\mathbf{n}}) = \frac{BR(b \rightarrow c \ell^- \bar{\mathbf{n}})}{t_b} = |V_{cb}|^2 \times F_{theory}$$

Y(4S), LEP/SLD, CDF measurements.  
Experimental  $\Delta|V_{cb}| \sim 1\%$

Theory with pert. and non-pert. corrections.  $\Delta|V_{cb}| \sim 2.5\%$

$F_{theory}$  evaluated using OPE in HQET: expansion in  $\alpha_s$  and  $1/m_B$  powers:

$O(1/m_B)$   $\rightarrow$  1 parameter:  $\Lambda$

(Bauer et al., PRD 67 (2003) 071301)

$O(1/m_B^2)$   $\rightarrow$  2 more parameters:  $\lambda_1, \lambda_2$

Constrained from pseudo-scalar/vector B and D mass differences

$O(1/m_B^3)$   $\rightarrow$  6 more parameters:  $\rho_1, \rho_2, T_{1-4}$

$$G_{sl} = \frac{G_F^2 |V_{cb}|^2}{192 p^3} m_B^5 c_1 \left\{ 1 - c_2 \frac{a_s}{p} + \frac{c_3}{m_B} (1 - c_4 \frac{a_s}{p}) + \frac{c_5}{m_B^2} + c_6 + c_7 + O\left(\frac{1}{m_B^3}\right) + O\left(\frac{a_s^2}{p}\right) \dots \right\}$$



# How can CDF look at it?

Must reconstruct all channels to get all the  $D^{**}$  states.

→ However CDF has limited capability for neutrals

- $B^0 \rightarrow D^{*-} | +\nu$  always leads to neutral particles → ignore it
- $B^- \rightarrow D^{*0} | -\nu$  better, use isospin for missing channels:
  - $D^{*0} \rightarrow D^+ \pi^-$  OK
  - $D^{*0} \rightarrow D^0 \pi^0$  Not reconstructed. Half the rate of  $D^+ \pi^-$
  - $D^{*0} \rightarrow D^{*+} \pi^-$ 
    - $D^{*+} \rightarrow D^0 \pi^+$  OK
    - $D^{*+} \rightarrow D^+ \pi^0$  Not reconstructed. Feed-down to  $D^+ \pi^-$
  - $D^{*0} \rightarrow D^{*0} \pi^0$  Not reconstructed. Half the rate of  $D^{*+} \pi^-$

# How to solve the problem in practice

Reconstruct  
 $D^*/D^+$

Add another  
 $\pi^{**} \rightarrow D^{**}$

Correct for  $\epsilon(m_{**}),$   
 $\epsilon(D^+)/\epsilon(D^*)$

Measure  
 $\langle m_{**}^2 \rangle, \langle m_{**}^4 \rangle$

•Collect as many modes as possible:

- $(K\pi)\pi^*$
- $(K\pi\pi\pi)\pi^*$
- $(K\pi\pi\pi^0)\pi^*$
- $K\pi\pi$

- Check yields
- Validate MC

•Selection:

- Optimize on MC+WS combinations
- Cross check on  $\pi^*$

• $\pi^{**}$  Background

- Combinatorial
- $D'$
- $B \rightarrow DD$
- $CC$
- ...

•Measure selection bias on  $m_{**}$  from:

- MC
- $D^*$  candidates
- Rely on MC (& PDG) for:
  - $\epsilon(D^+)/\epsilon(D^*)$
  - Unseen modes (I sospin)
  - Lepton spectrum acceptance

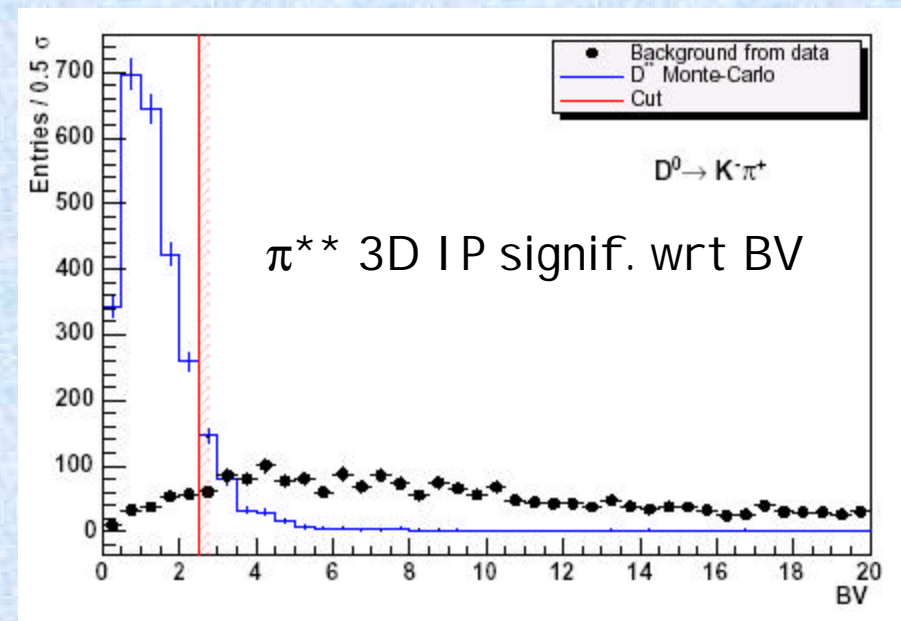
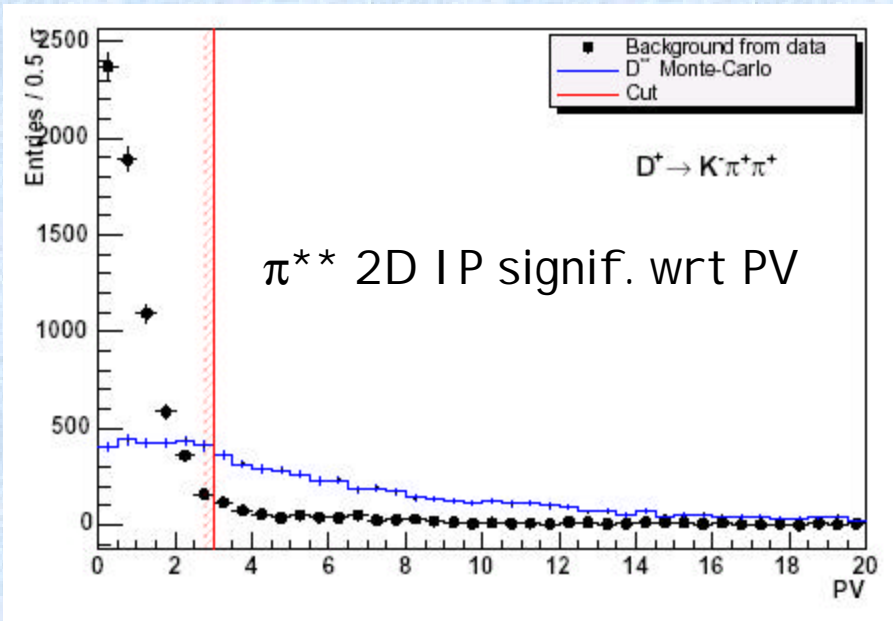
•Subtract backgrounds

- Use PDG to go  $\Delta m_{**} \rightarrow m_{**}$
- Compute  $\langle m_{**}^2 \rangle$  &  $\langle m_{**}^4 \rangle$
- Include  $D^{(*)0}$
- Extract  $\Lambda, \lambda_1$
- Systematics

# $\pi^{**}$ Selection

Based on topology:

- impact parameter significances w.r.t. primary, B and D vertices



Cuts are optimized using MC and **background (WS) data**:

Additional cuts only for  $D^+$ :

$$\bullet p_T > 0.4 \text{ GeV}$$

$$\bullet |d_0^{PV}/\sigma| > 3.0$$

$$|d_0^{DV}/\sigma| > 0.8$$

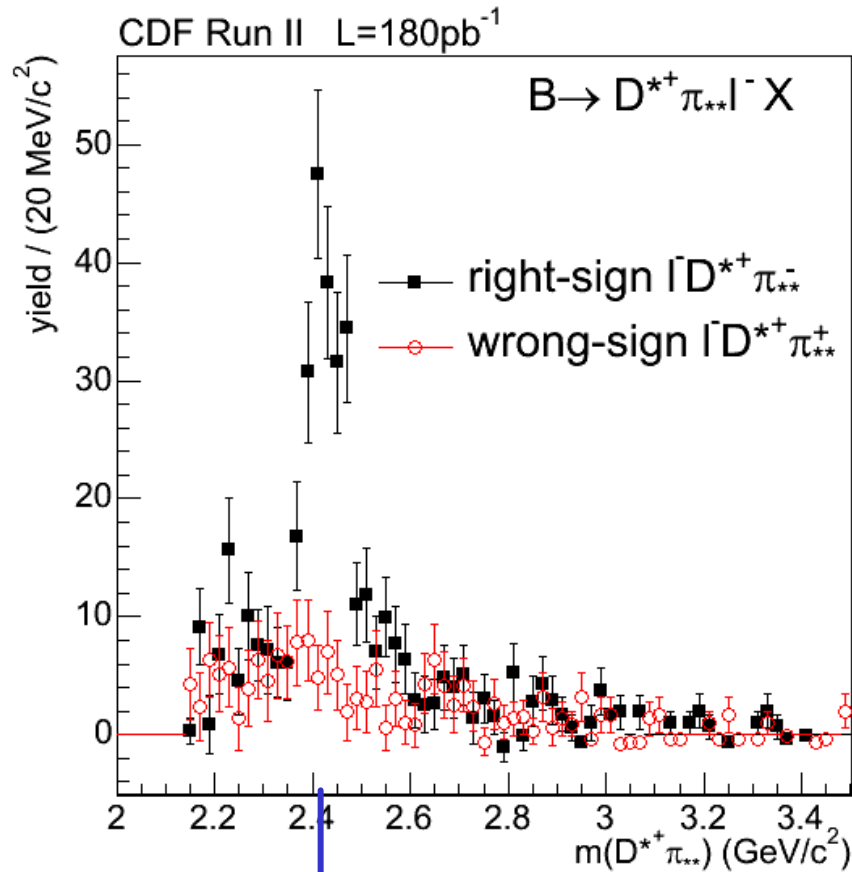
$$\bullet \Delta R < 1.0$$

$$\bullet |d_0^{BV}/\sigma| < 2.5$$

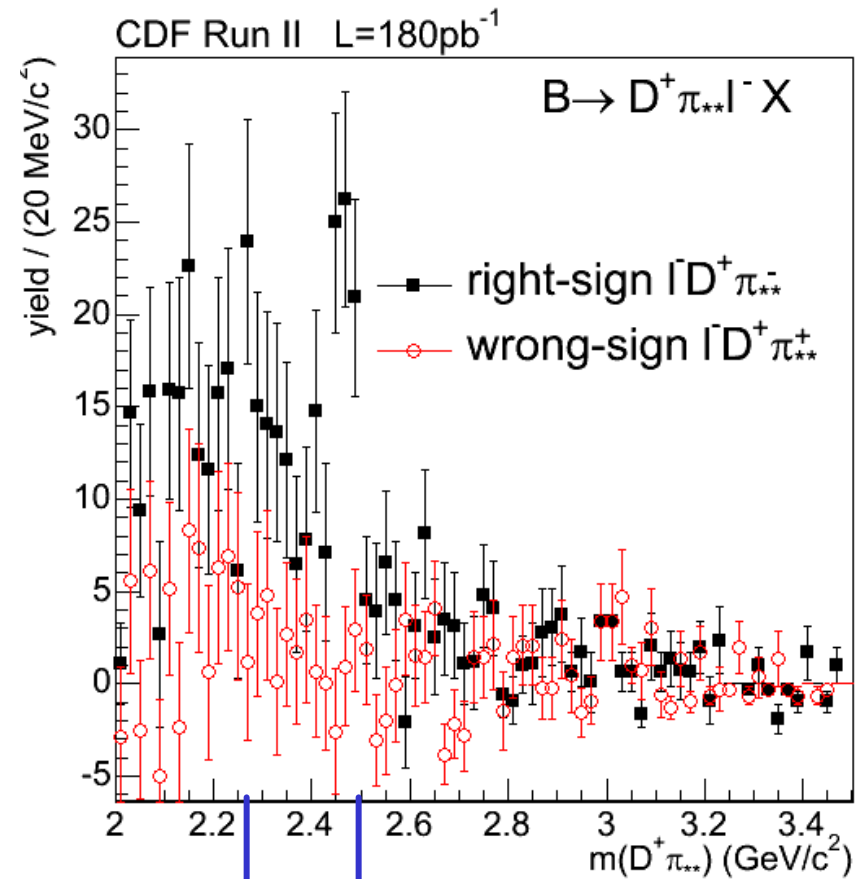
$$L_{xy}^{B \rightarrow D} > 500 \mu\text{m}$$

# Raw $m^{**}$ distributions

Measured in  $\Delta m^{**}$ , shifted by  $M(D^{(*)+})$ , side-band subtracted.



$D_1, D_1^*, D_2^*$



Feed-down

$D_2^*, D_0^*$

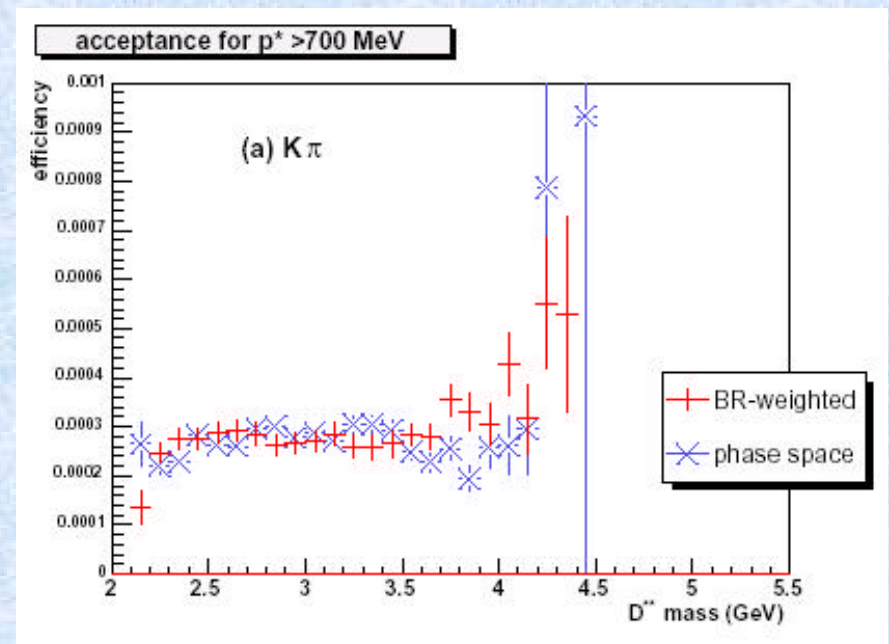
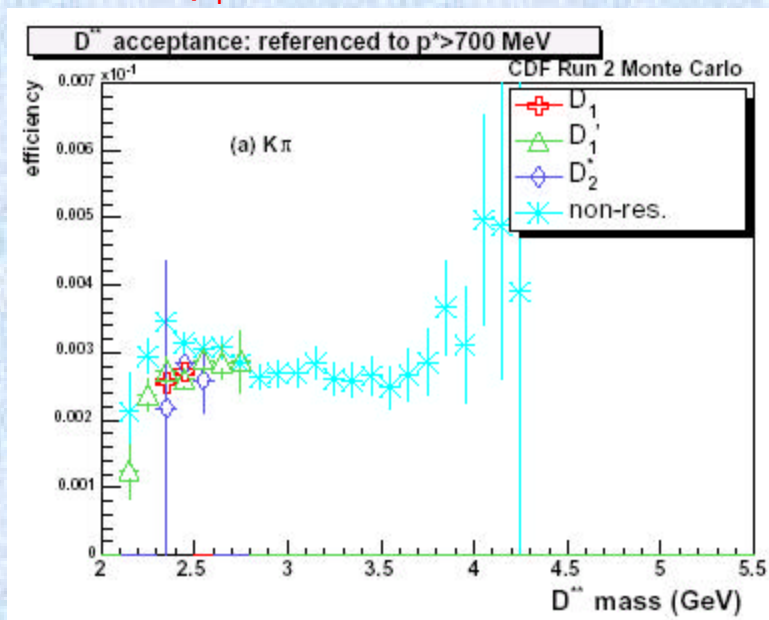
# Efficiency Corrections

1) Correct the raw mass for any dependence of  $\epsilon_{\text{reco}}$  on  $M(D^{**})$ :

- Possible dependence on the  $D^{**}$  species (spin).
- Monte-Carlo for all  $D^{**}$  (Goity-Roberts for non-resonant), cross-checked with pure phase space decays.
- Detector simulation shortcomings cause residual data/MC discrepancy: derive corrections from control samples ( $D^*$  and  $D$  daughters)

2) Cut on lepton energy in B rest frame:

- Theoretical predictions need well-defined  $p_l^*$  cut.
- We can't measure  $p_l^*$ , but we can correct our measurement to a given cut:  
→  $p_l^* > 700 \text{ MeV}/c$ .





# Final Result

$$m_1 \equiv \langle m_{D^{**}}^2 \rangle = (5.83 \pm 0.16_{\text{stat}} \pm 0.08_{\text{syst}}) \text{ GeV}^2$$

$$m_2 \equiv \left\langle \left( m_{D^{**}}^2 - \langle m_{D^{**}}^2 \rangle \right)^2 \right\rangle = (1.30 \pm 0.69_{\text{stat}} \pm 0.22_{\text{syst}}) \text{ GeV}^4$$

$$\rho(m_1, m_2) = 0.61$$

$$M_1 \equiv \langle s_H \rangle - m_D^2 = (0.467 \pm 0.038_{\text{stat}} \pm 0.019_{\text{exp}} \pm 0.065_{\text{BR}}) \text{ GeV}^2$$

$$M_2 \equiv \langle (s_H - \langle s_H \rangle)^2 \rangle = (1.05 \pm 0.26_{\text{stat}} \pm 0.08_{\text{exp}} \pm 0.10_{\text{BR}}) \text{ GeV}^4 ,$$

$$\rho(M_1, M_2) = 0.69$$

## Pole mass scheme

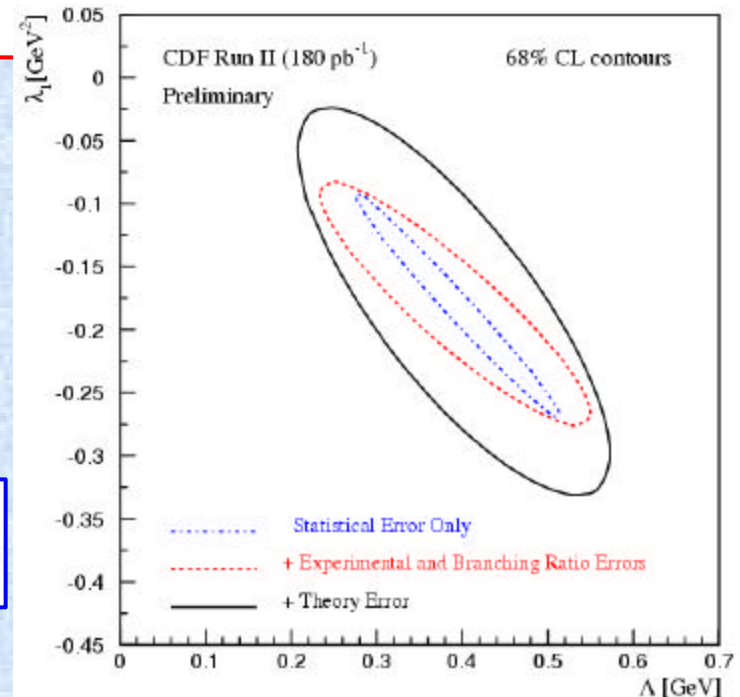
$$\Lambda = (0.397 \pm 0.078_{\text{stat}} \pm 0.027_{\text{exp}} \pm 0.064_{\text{BR}} \pm 0.058_{\text{theo}}) \text{ GeV}$$

$$\lambda_1 = (-0.184 \pm 0.057_{\text{stat}} \pm 0.017_{\text{exp}} \pm 0.022_{\text{BR}} \pm 0.077_{\text{theo}}) \text{ GeV}^2$$

## 1S mass scheme


$$m_b^{1S} = (4.654 \pm 0.078_{\text{stat}} \pm 0.027_{\text{exp}} \pm 0.064_{\text{BR}} \pm 0.089_{\text{theo}}) \text{ GeV}$$

$$\lambda_1^{1S} = (-0.277 \pm 0.049_{\text{stat}} \pm 0.017_{\text{exp}} \pm 0.022_{\text{BR}} \pm 0.094_{\text{theo}}) \text{ GeV}^2$$



# Systematics

## • Input parameters

- 
- $D^{(*)+}$  Masses, in combining  $D^{(*)}$  with  $D^{**}$   $m \rightarrow M$  [PDG errors]
  - BR ( $B \rightarrow D^+ / D^{*+}$   $m \rightarrow M$ ) [PDG errors]

## • Experimental

- • Detector resolution [re-smear satellite sample by full resolution:  $\pm 60 \text{ MeV}$ ]
- • Data/MC Efficiency discrepancies [measure  $P_t$  and  $m$  dependency on control sample, probe different fit models]
- • Decay models in MC [full kinematic description vs pure phase space]
- •  $P_1^*$  cut correction [repeat measurement at various  $P_1^*$  thresholds]

## • Backgrounds

- • Scale [charge correlation WS/RS from fully reconstructed B:  $\pm 4\%$ ]
- Optimization Bias [repeat optimization procedure on bootstrap copies of the sample]
- Physics background [vary  $\pm 100\%$ ]
- $B \rightarrow X_c \tau \nu$  [estimate  $\tau/\mu$  yield and kinematic differences using MC]
- Fake leptons [no evidence in WS  $D^+ I^+$ , charge-correlated negligible]

# CP: hh modes

- Good agreement with B factories
- First measurement ever of  $B_s \rightarrow KK$

$$\frac{BR(B_d \rightarrow \pi^\pm \pi^\mp)}{BR(B_d \rightarrow K^\pm \pi^\mp)} = 0.24 \pm 0.06 \text{ (stat.)} \pm 0.05 \text{ (syst.)}$$

$$A_{CP} = \frac{N(\bar{B}_d^0 \rightarrow K^- \pi^+) - N(B_d^0 \rightarrow K^+ \pi^-)}{N(\bar{B}_d^0 \rightarrow K^- \pi^+) + N(B_d^0 \rightarrow K^+ \pi^-)} = -0.04 \pm 0.08 \text{ (stat.)} \pm 0.01 \text{ (syst.)}$$

$$\frac{f_d \cdot BR(B_d \rightarrow \pi^\pm \pi^\mp)}{f_s \cdot BR(B_s \rightarrow K^\pm K^\mp)} = 0.48 \pm 0.12 \text{ (stat.)} \pm 0.07 \text{ (syst.)}$$

$$\frac{f_s \cdot BR(B_s \rightarrow K^\pm K^\mp)}{f_d \cdot BR(B_d \rightarrow K^\pm \pi^\mp)} = 0.50 \pm 0.08 \text{ (stat.)} \pm 0.07 \text{ (syst.)}$$

$$\frac{BR(B_s \rightarrow \pi^\pm \pi^\mp)}{BR(B_s \rightarrow K^\pm K^\mp)} < 0.10 \text{ @ 90\% C.L.}$$

$$\frac{BR(B_d \rightarrow K^\pm K^\mp)}{BR(B_d \rightarrow K^\pm \pi^\mp)} < 0.17 \text{ @ 90\% C.L.}$$

$$\frac{f_s \cdot BR(B_s \rightarrow K^\pm \pi^\mp)}{f_d \cdot BR(B_d \rightarrow K^\pm \pi^\mp)} < 0.11 \text{ @ 90\% C.L.}$$

<http://www-cdf.fnal.gov/physics/new/bottom/040722.blessed-bhh/>

$$BR(\Lambda_b \rightarrow hh) < 22 \cdot 10^{-6} \text{ (90\% C.L.)}$$

[http://www-cdf.fnal.gov/physics/new/bottom/040624.blessed\\_Lb\\_hh\\_limit/](http://www-cdf.fnal.gov/physics/new/bottom/040624.blessed_Lb_hh_limit/)

