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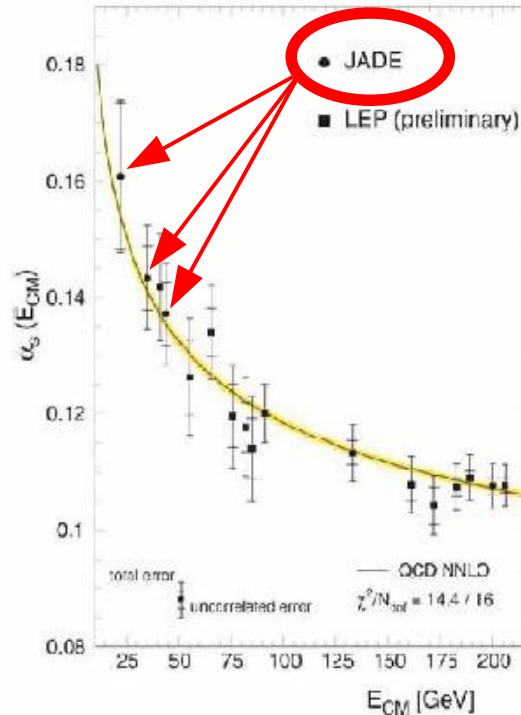
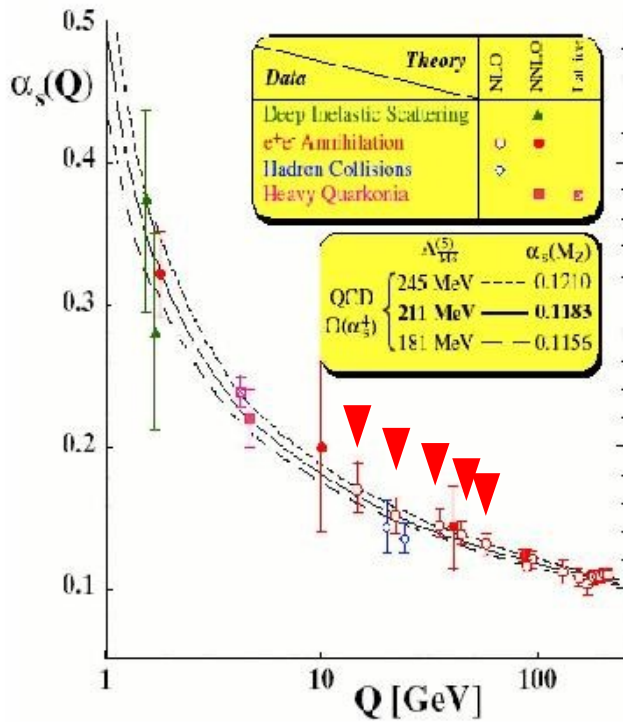


David J. Gross

H. David Politzer

Frank Wilczek

**Asymptotic Freedom and Quantum ChromoDynamics: the Key to the Understanding of the Strong Nuclear Forces**



...taken from the Physics Nobel Prize press release (Oct 5, 2004)

The left-hand panel shows a collection of different measurements by S. Bethke from High-Energy International Conference in Quantum Chromodynamics, Montpellier 2002 (hep-ex/0211012). The right-hand panel shows a collection by P. Zerwas, Eur. Phys. J. C34(2004)41. **JADE was one of the experiments at PETRA at DESY.** NNLO means Next-to-Next-to-Leading Order computation in QCD.

<http://nobelprize.org/physics/laureates/2004/press.html>

# Towards Precision Top Quark Mass Measurements



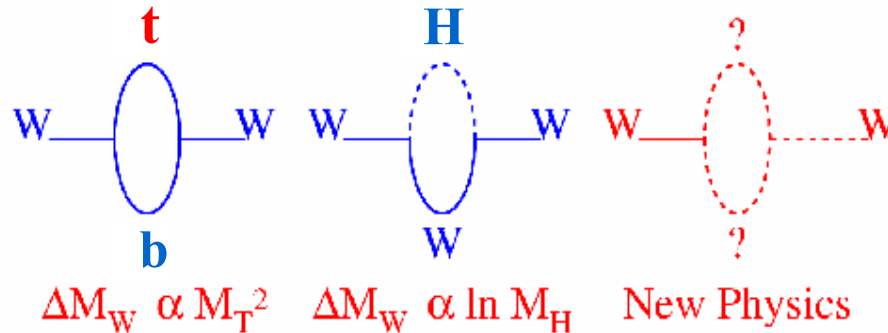
Pedro A. Movilla Fernández  
Lawrence Berkeley National Laboratory

FNAL/Rockefeller U., Aug 30<sup>th</sup> 2007

- Motivation
- Improving Measurements (I)  
Multivariate Method
- Improving Measurements (II)  
Calorimeter Simulation
- **Towards Precision Top Quark Mass**
- Outlook

# Top Quark Mass Implications

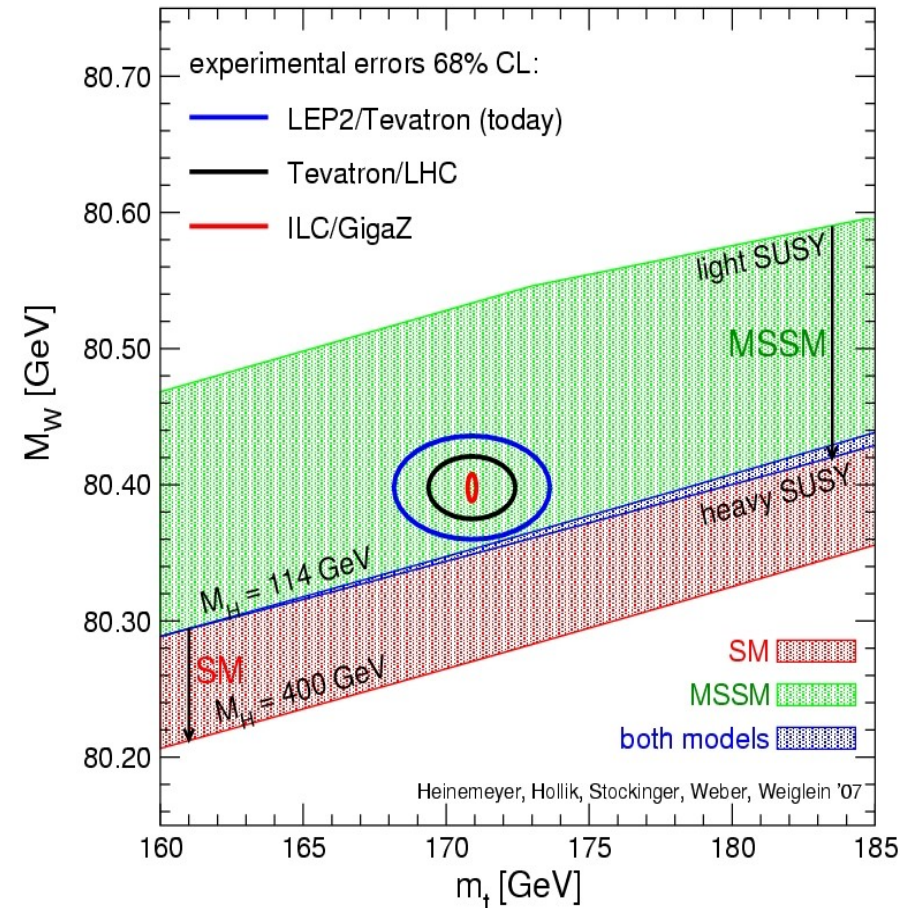
- It is a fundamental parameter.
- It is correlated to other SM parameters via electroweak corrections.



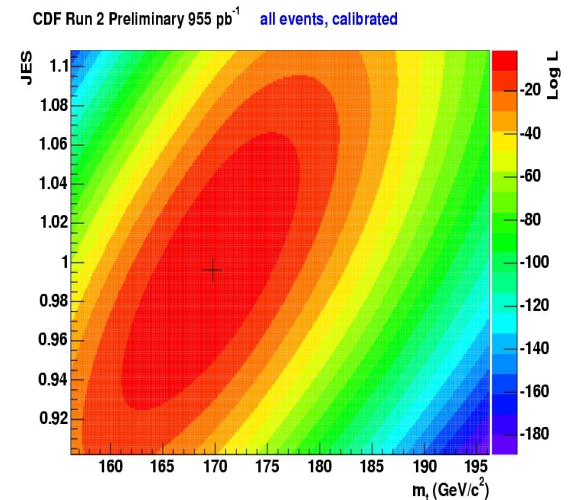
- Surprisingly large mass: A key to understand EWSB?
- Top quark and W boson mass predict the Higgs boson mass.
- Allow to impose constraints for physics beyond the SM.

- LEP limit:  $m_{\text{Higgs}} > 114 \text{ GeV}/c^2$  @ 95% C.L.
- Electroweak fit:  $m_{\text{Higgs}} = 76^{+33}_{-24} \text{ GeV}/c^2$

Heinemeyer et al. ,  
 JHEP 0608:052 (2006)  
 Update March 2007

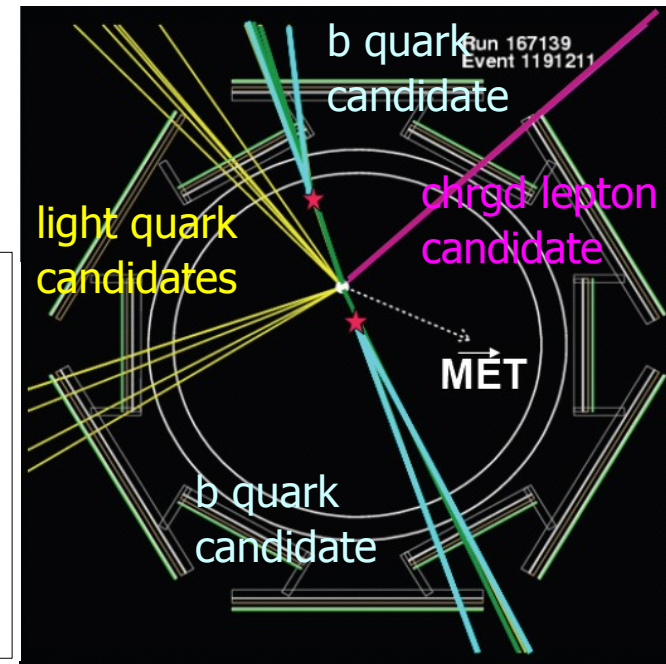
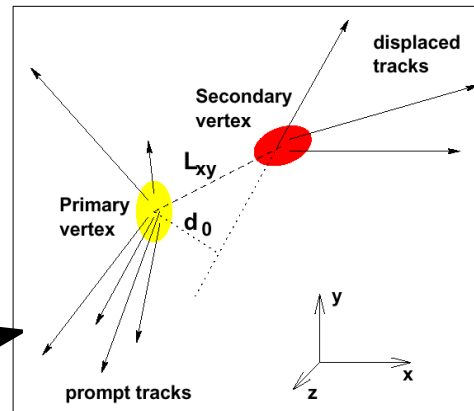
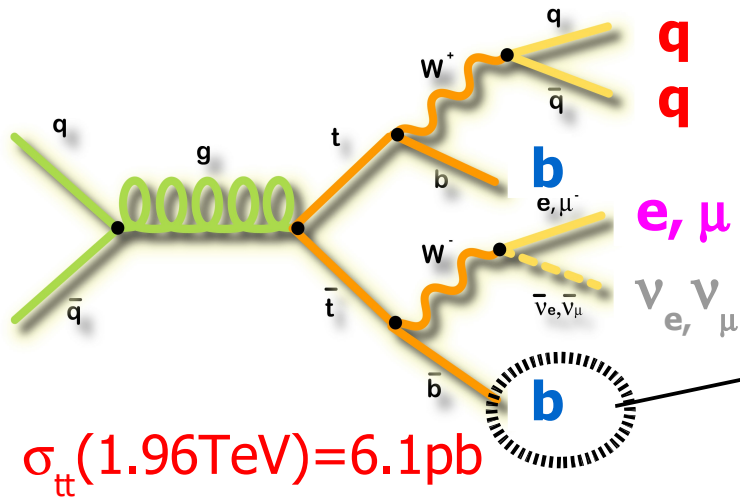


# Improving Measurements (I)



Multivariate Method

# Lepton+Jets Analysis



- Standard analysis cuts in "Multivariate Method":

- Exactly one central  $e/\mu$  with  $p_T > 20$  GeV,  $|\eta| < 1.0$
- Exactly four jets with  $E_T > 15$  GeV,  $|\eta| < 2.0$
- Undetected ("missing") energy  $> 20$  GeV
- At least one SecVtx tag

- Channel is compromise between statistics and purity:

- $BR \sim 30\%$ ,  $S/B = 1/4 - 11/1$

- Moderate combinatorial quark/jet ambiguity:

- 2-12 permutations

- Neutrino momentum partly derived from missing MET

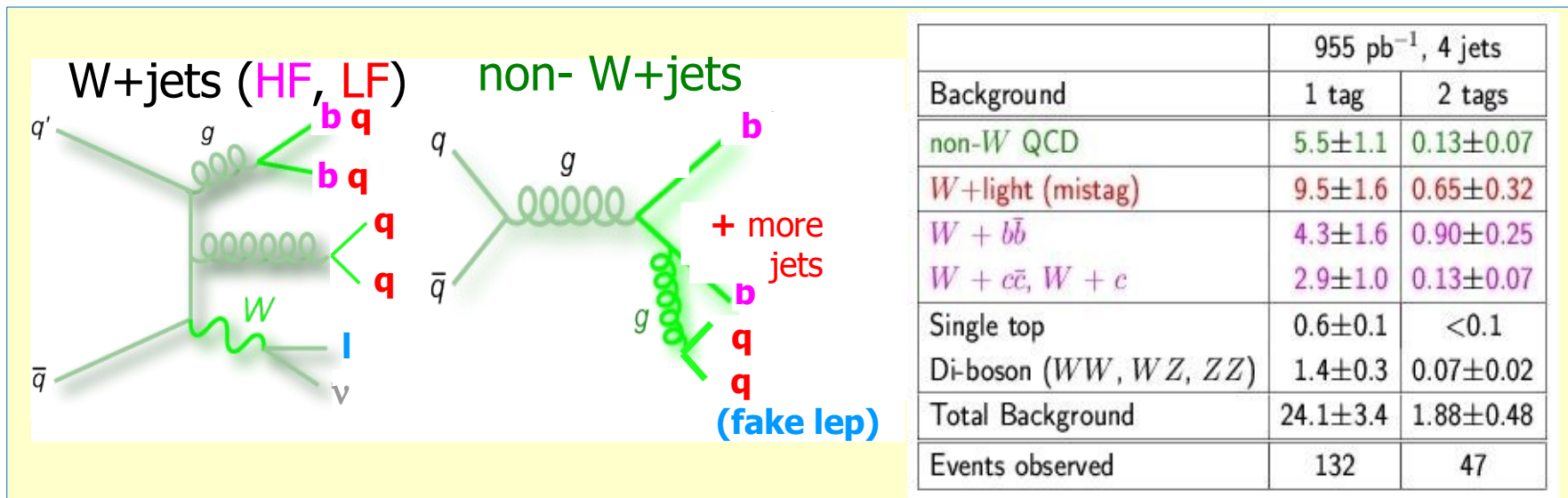
- two-fold ambiguity

very similar to other lepton-jets analyses

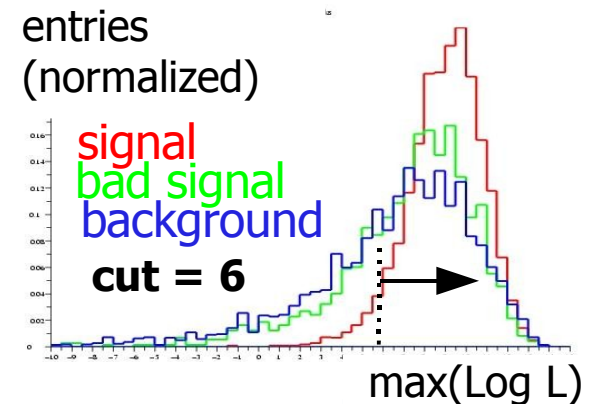
depending on b-tag requirement

# S/B in Multivariate Method

- Found **179** candidate events in **955/pb** of data.
- Background contributions:
  - non-W+jets containing fake leptons  $\sim 22\%$
  - W+light jets containing mistags  $\sim 40\%$
  - W+heavy flavor Wbb, Wcc, Wc  $\sim 33\%$
  - Di-Boson WW, ZZ, WZ
  - Single top



- Additional likelihood cut to clean up background and bad signal (ISR/FSR, W $\rightarrow\tau\nu$ ...)
- Number of candidates: 179  $\rightarrow$  149



# Multivariate Method Basics (1)



## Event-by-event probability density

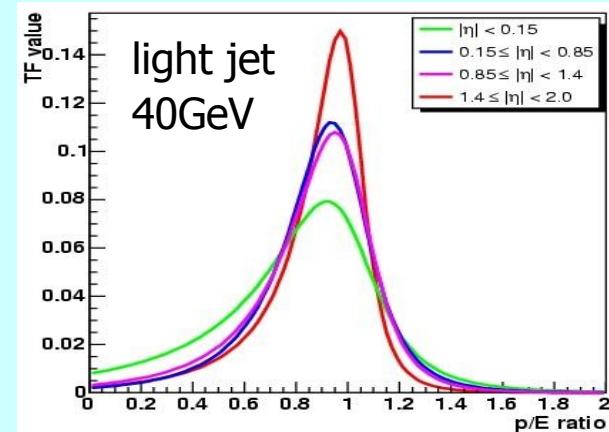
detector level observables      jet-quark combinations      proton-parton density functions      transfer functions

$$\mathcal{P}_{t\bar{t}}(\mathbf{y}|m_t, \text{JES}) \propto \sum_{i=1}^{N_{\text{perm}}} w_i \int d\Phi_6(\mathbf{x}) f_{\text{pdf}}(q_1) f_{\text{pdf}}(q_2) \times |M_{\text{eff}}(m_t, \mathbf{x})|^2 \times W(\mathbf{y}|\mathbf{x}, \text{JES})$$

b-tag weight      phase space      leading order signal matrix element

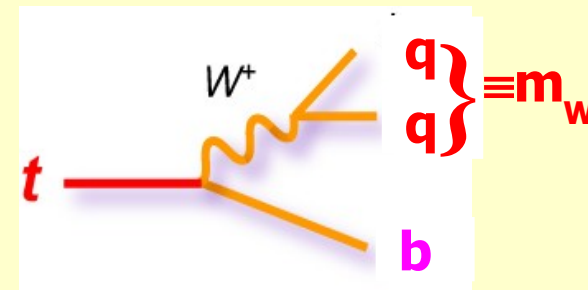
## Transfer Functions

- Probabilities for a set of detector variables  $\mathbf{y}$  to be measured given parton configuration  $\mathbf{x}$  and JES.
- Smooth function of  $p(\text{jet})/E(\text{parton})$ , dependent on quark flavor and jet  $\eta$



## In-Situ JES Calibration

- JES hypothesis giving  $W$  mass inconsistent with word average value/width penalizes the event probability.  
 → Part of  $\Delta\text{JES}$  becomes statistical component of  $\Delta m_t$  and scales down with integrated luminosity!





# Multivariate Method Basics (2)



## Integration

- Integration over full phase space intractable, make simplifying assumptions:
  - quark angles | charged lepton momentum | quark & lepton masses
- Seven integration variables remaining:
  - $m_W^2$  (had),  $m_t^2$  (had),  $m_W^2$  (lep),  $m_t^2$  (lep),  $\log(p_1/p_2)$  (light quarks),  $p_x(t\bar{t})$ ,  $p_y(t\bar{t})$
- Use of modified ("effective") propagators:
  - corrects mismatch between ME, MC and integration assumptions

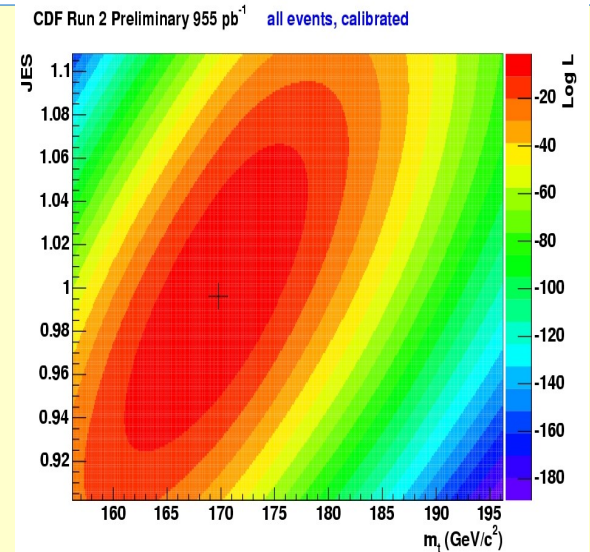
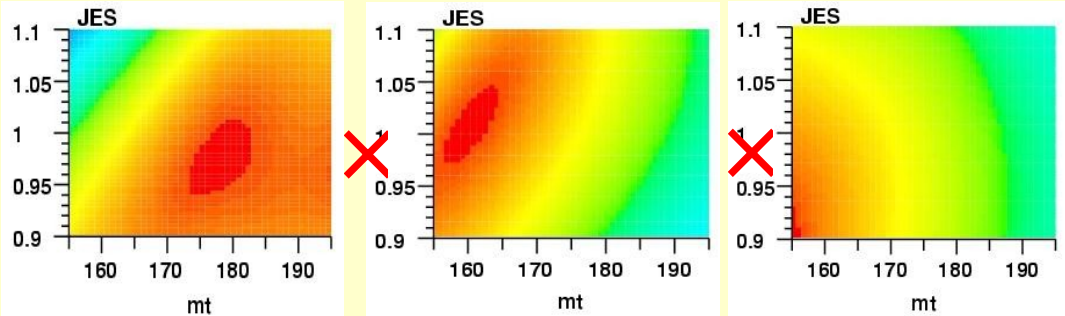
## Matrix Element

- Use complete signal matrix elements (R. Kleiss and W.J. Stirling, Z.Phys. C40 (1988) 419) for a more consistent approach:
  - $qq \rightarrow t\bar{t} + gg \rightarrow t\bar{t}$  tree level amplitudes | finite width of  $W$ , top quark | non-zero b-quark masses | complete spin correlations between top production and decay

## Multivariate aspect

- Signal probability is weighted using a specially designed S/B discriminant.
  - Requirements for the second variable
    - minimum top quark mass dependence
    - minimum JES dependence
    - maximum S/B discrimination
- } essential to allow multiplication of per-event likelihoods

# Extracting the Top Quark Mass



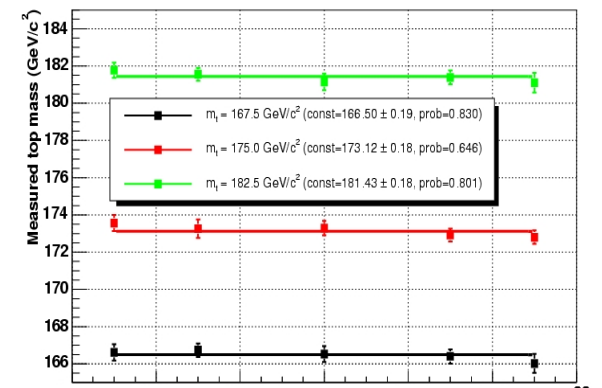
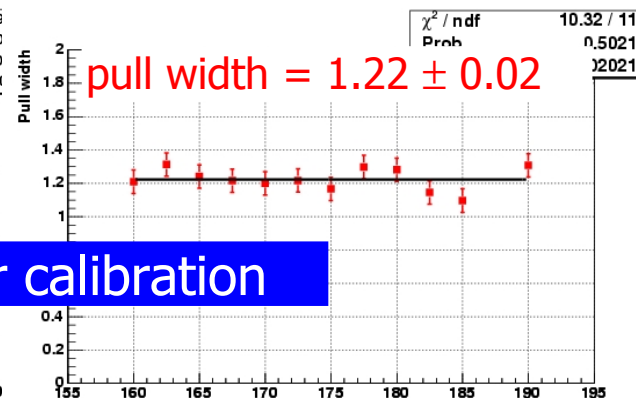
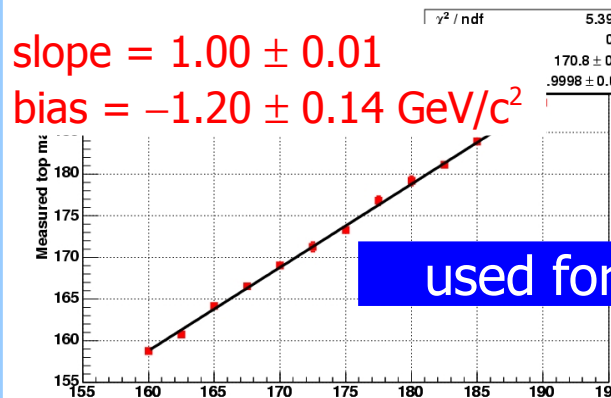
- Build the total 2-dim. likelihood and extract peak of profile likelihood:
- Correct mass and uncertainty value using calibration obtained from pseudo-experiments

$$M_{\text{top}} = 169.8 \pm 2.3 (\text{stat.} + \text{JES}) \pm 1.4 (\text{syst.}) \text{ GeV}/c^2$$

$$M_{\text{top}} = 169.8 \pm 2.7 (\text{tot.}) \text{ GeV}/c^2$$

$$\text{JES} = 0.996 \pm 0.018 (\text{stat.})$$

Only 0.1 GeV/c<sup>2</sup> less precise than world's single best 1fb<sup>-1</sup> result!



used for calibration

Measured vs. input mass

Pull Widths

Input JES Variation

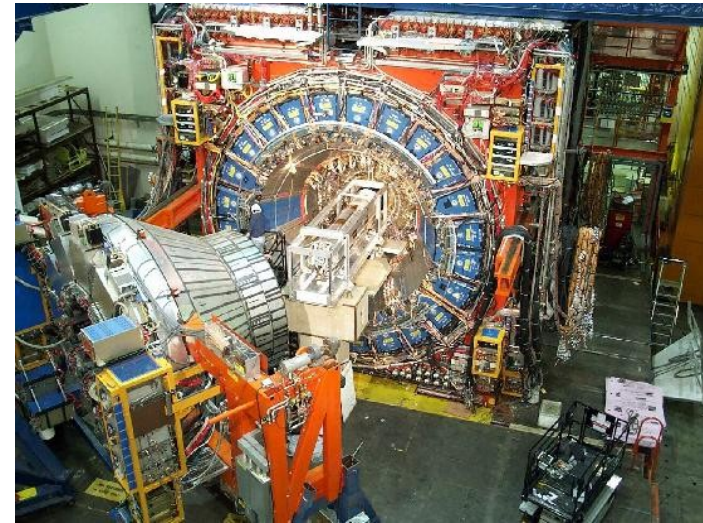
# Future Plans



- Major problem is the presence bad signal:
  - wrong jet-to-parton assignment
  - ISR/FSR jets among the four leading jets: contamination is highest in least energetic jet
- Possible remedy:
  - consider also a signal probability which ignores 4<sup>th</sup> leading jet
  - introduce a bad signal discriminant (ANN)
- Get rid of simplifying integration assumptions and effective propagators:
  - Requires expansion of integration phase space (up to 19 dimensions)
- Improve background discrimination:
  - ANN discriminant with no top quark mass and JES dependence?
- Introduce a-priori JES constraint

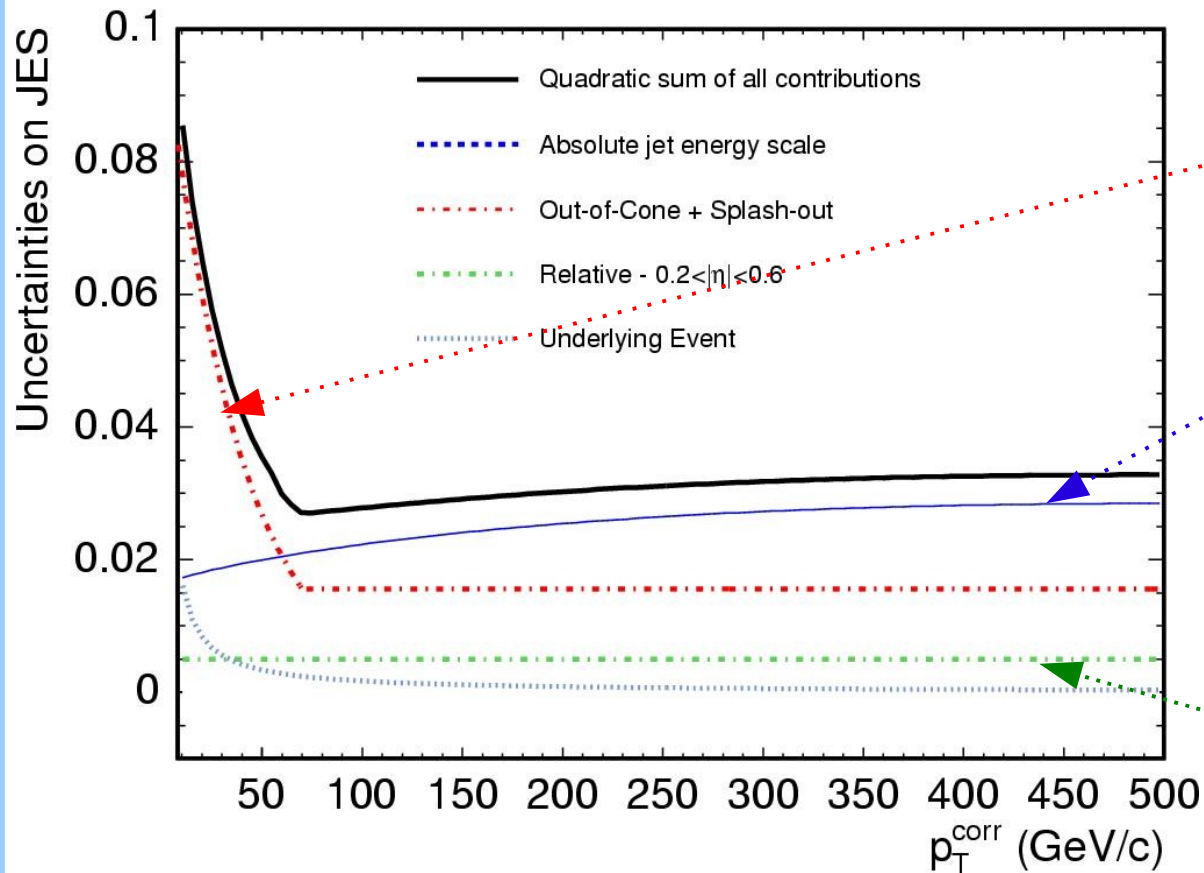
hurts resolution, causes bias,  
causes pull widths  $\neq 1$

# Improving Measurements (II)



Calorimeter Simulation

# Total JES Uncertainty



## Out-of-Cone correction

- MC/data mismatch of energy flow outside the jet cone
- direct contribution from lateral E/p shower profile

## Absolute correction

- contribution from absolute E/p response simulation

## Relative Correction

- contribution from imperfection of Plug/Wall simulation

- Above plot reflects simulation performance of CDF-II publications (excluding recent improvements)
- **Calorimeter simulation uncertainties are the dominant source of uncertainty** (specially if **no JES** in-situ calibration possible).

# GFLASH in a Nutshell

- GFLASH treats calorimeter as a single effective medium.
- EM and HAD responses are related to **MIP** response

## Sampling structure/spatial energy distribution:

$$d E_{vis}(\mathbf{r}) = E_{inc} \hat{m} \sum_{\hat{k}} \frac{\hat{k}}{\hat{m}} c_{\hat{k}} f_{\hat{k}}(\mathbf{r}) d\mathbf{r}$$

$\hat{k} = EM, HAD$

MIP response

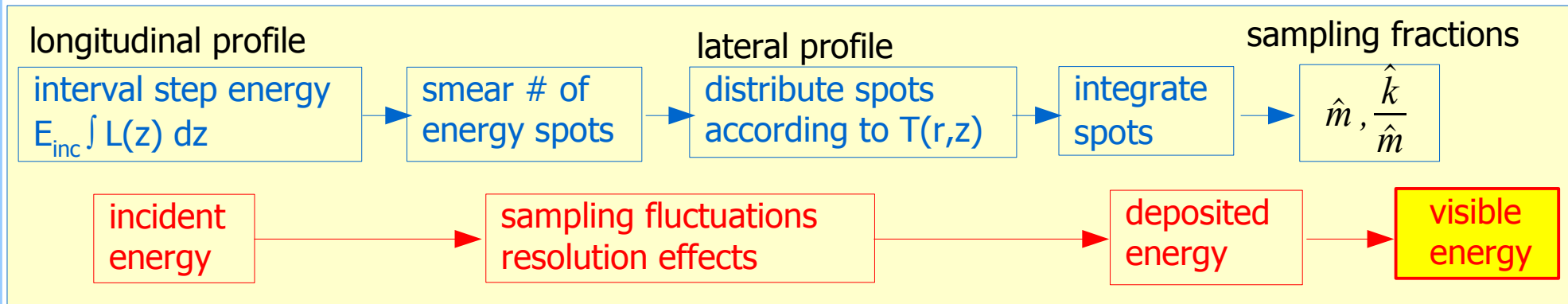
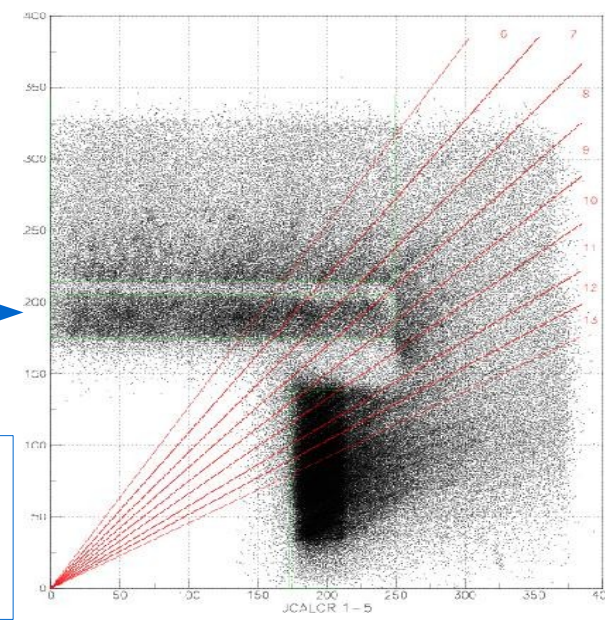
response relative to MIP

relative fraction EM/HAD

## Profile:

$$f(\mathbf{r}) \propto L(z) T(r, z)$$

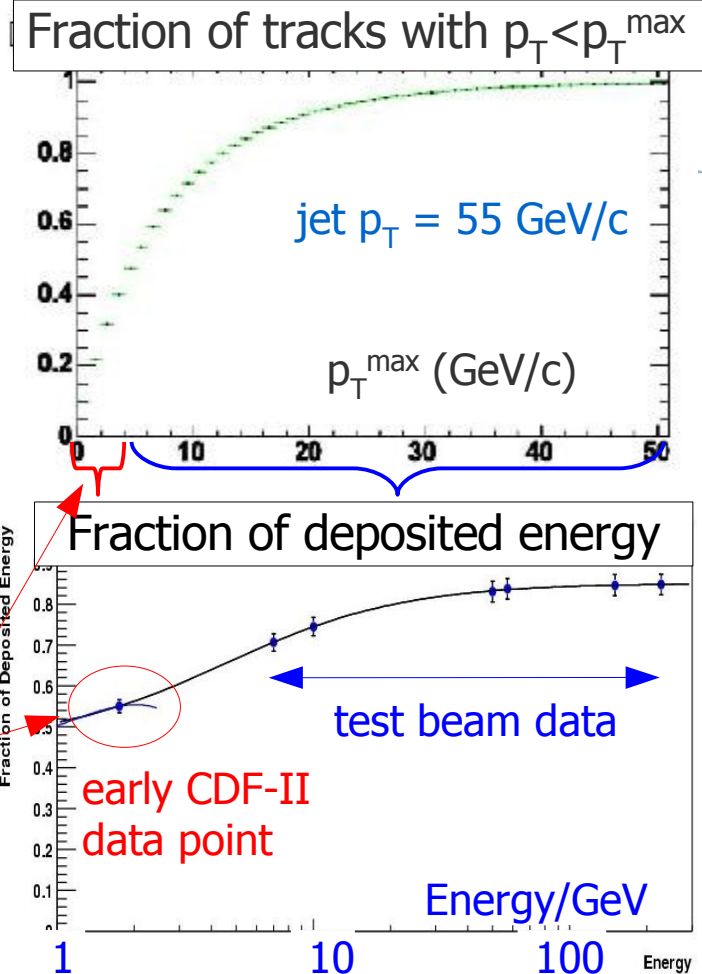
longitudinal      lateral



# In Situ Tuning Approach

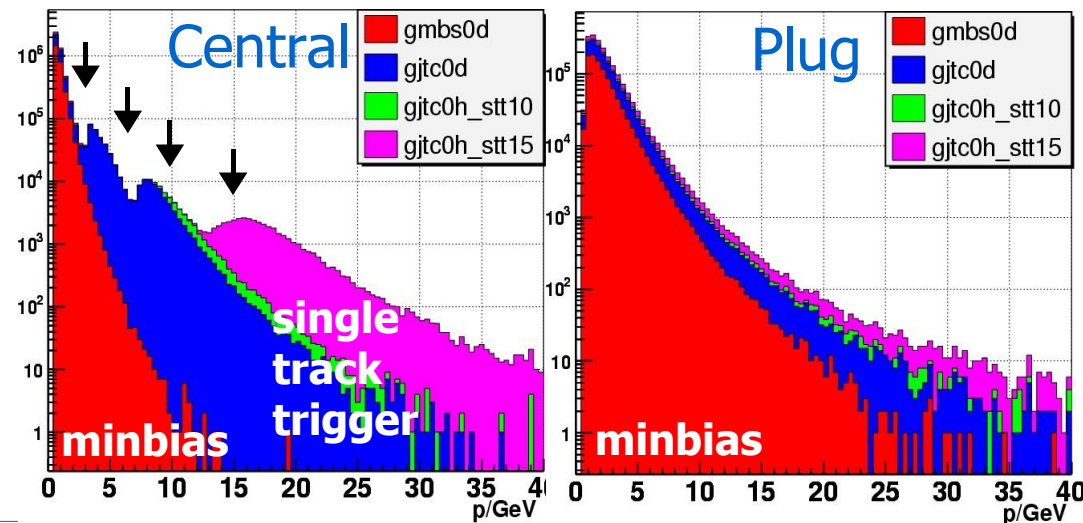
## In-situ Run-II data (plus test beam data)

- **Energy dependence:**  
Interpolate energy dependence of parameters using  $\langle E/p \rangle$  response in EM and HAD
- **Lateral profile:**  
Adjust  $\langle E/p \rangle$  profile in EM and HAD
- **Early Run-II:** Poor in-situ control up to 2.5 (5) GeV



## Run-II improvements

- Single track triggers with thresholds up to 15 GeV/c.
- Single charged particle response analysis.
- In-situ tuning extended up to 40(20) GeV/c in Central (Plug)



# Lateral Profile

$$T(r) = \frac{2rR_0^2}{(r^2 + R_0^2)^2}$$

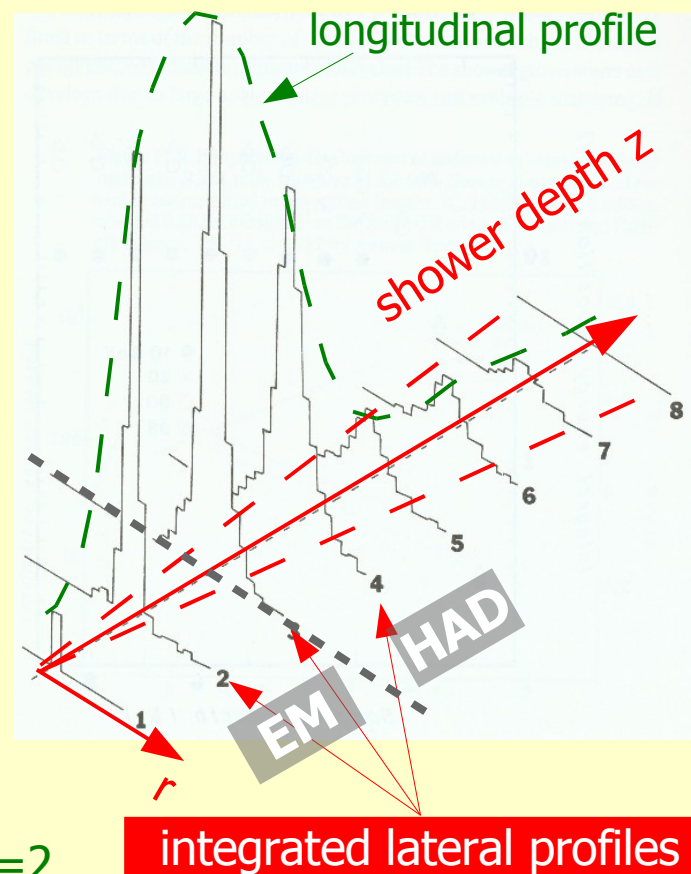
- r: radial distance from shower center
- z = shower depth

- $R_0$ : log-normal distribution (in units of Moliere radius or absorptions lengths)
- Mean & width of  $R_0$ :

$$\langle R_0(E, z) \rangle = [R_1 + (R_2 - R_3 \log E) z]^n$$

$$\frac{\sigma_{R_0}(E, z)}{\langle R_0(E, z) \rangle} = [(S_1 - S_2 \log E)(S_3 + S_4 z)]^2$$

hadrons:  $n=1$   
 photons, electrons:  $n=2$



- Hadronic showers: linear dependence on shower depth
- Logarithmic dependence on incident particle energy

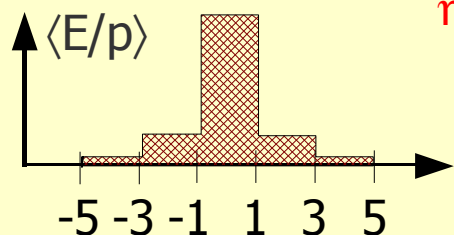
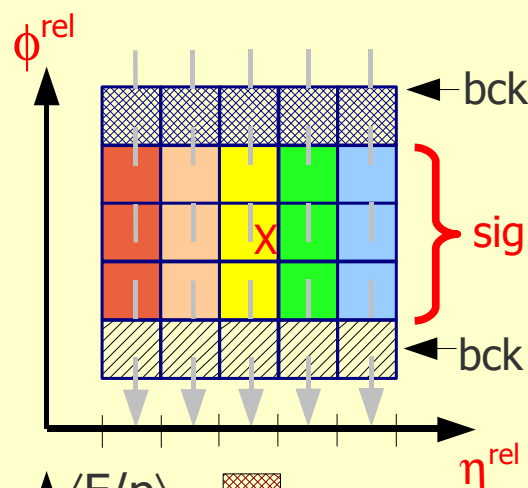
7 parameters



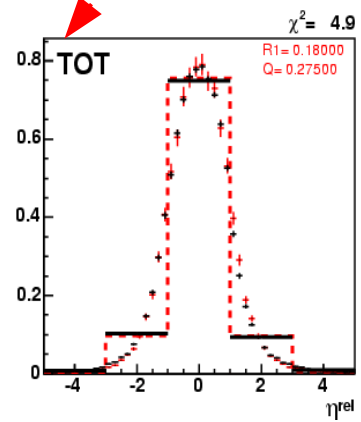
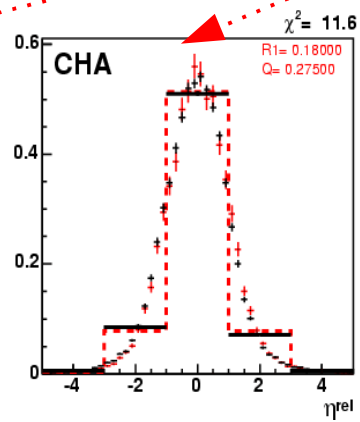
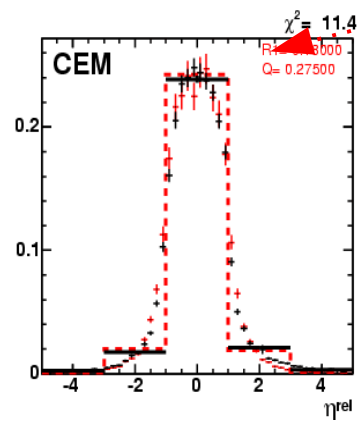
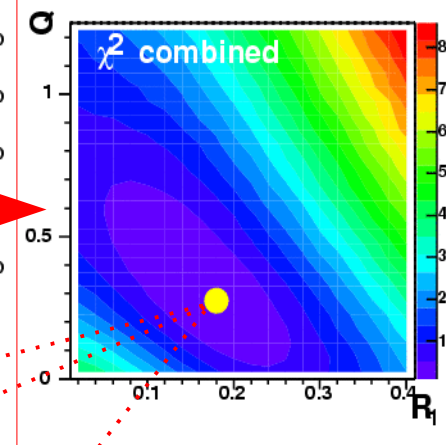
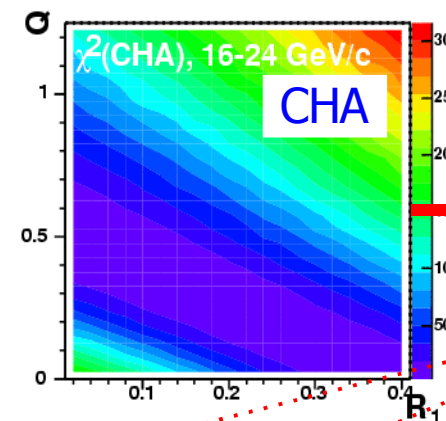
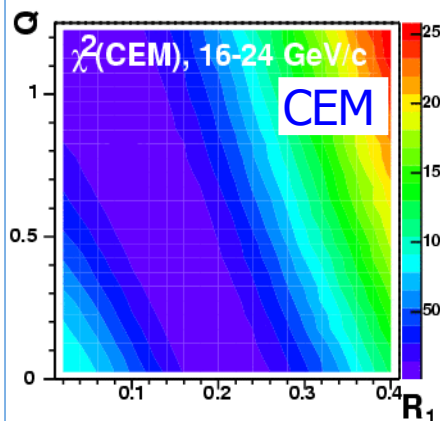
# Lateral Profile Tuning

Example: 20 GeV profile (Central)

X extrapol. track impact point



$$\eta^{rel} = \frac{\eta - (\eta^{max} + \eta^{min})/2}{(\eta^{max} - \eta^{min})/2}$$



## Tuning

$$\langle R_0(E_{inc}, z) \rangle = [R_1] + ([R_2 - R_3 \ln E_{inc}] z)^n$$

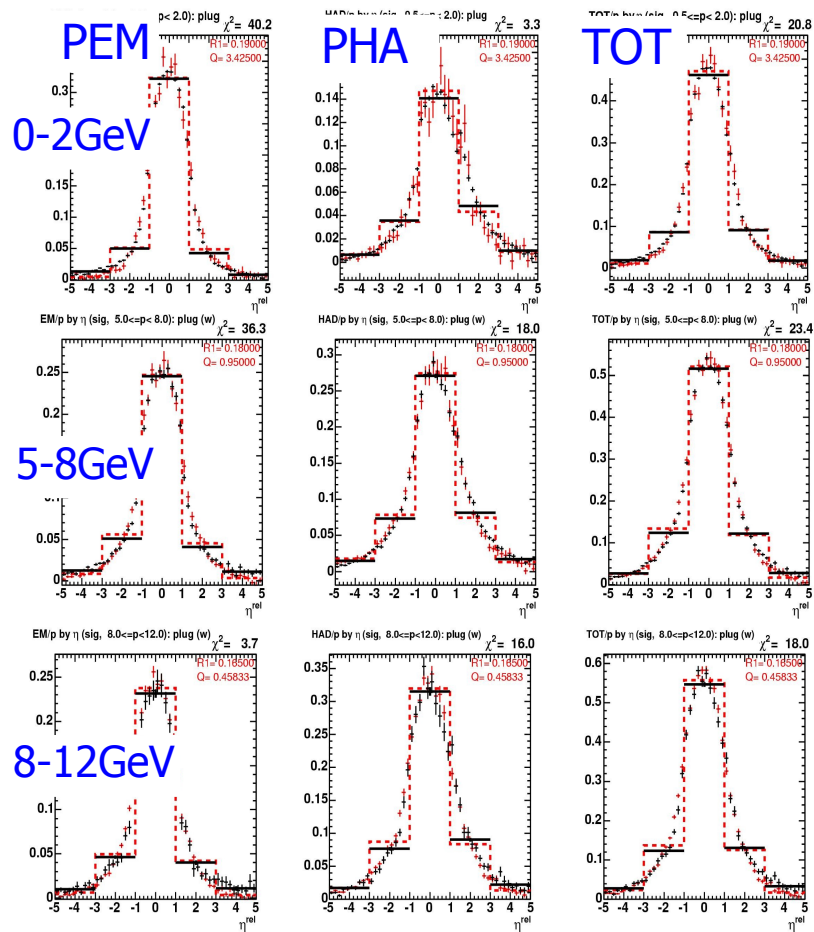
core term  $R_1$

spread term  $Q$

- shower depth
- incident particle energy

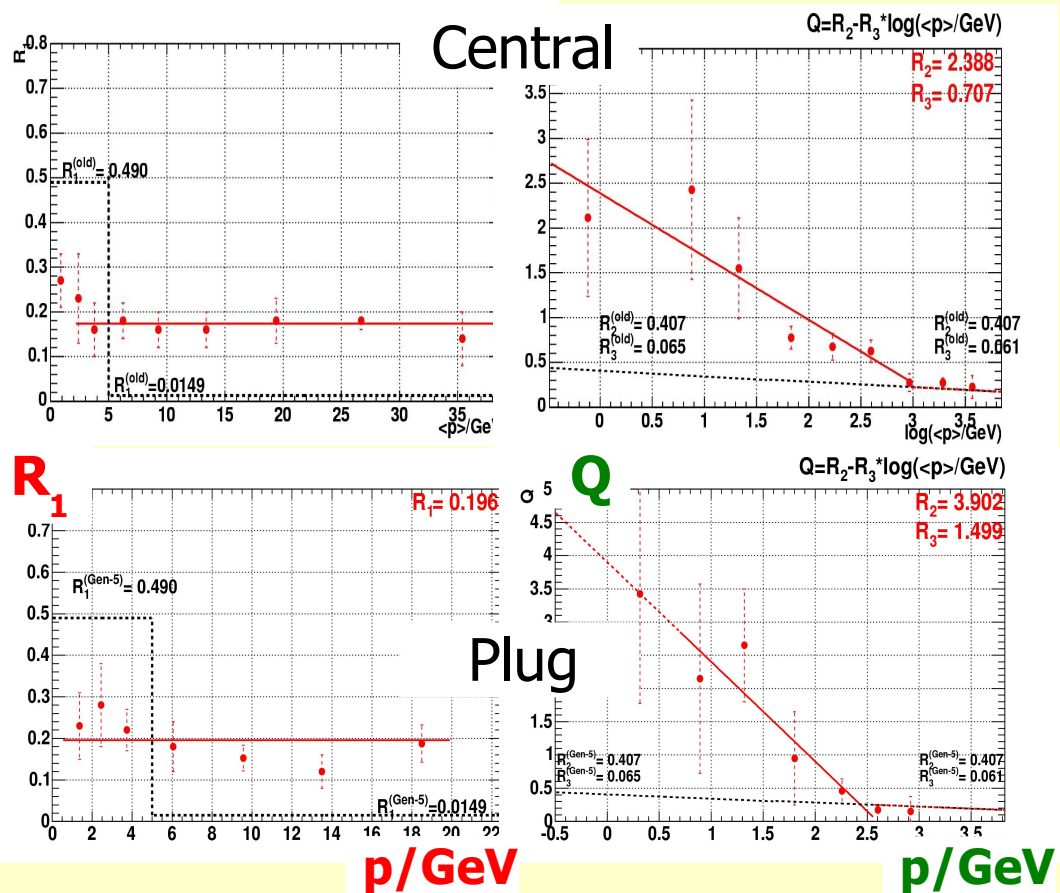
- EM and HAD probe different stages of shower development.
- Normalization to absolute data response decouples tuning from longitudinal profile details.

# Lateral Profile Tuning (2)



shower core

shower spread



- Consistent global tuning in Central and Plug
- Lateral profiles must match as perfectly as possible to avoid bias in absolute response tuning

# Longitudinal Profile

$$d E_{vis}(\mathbf{r}) = E_{inc} \hat{m} \sum_{\hat{k}} \left( \frac{\hat{k}}{\hat{m}} \right) c_{\hat{k}} f_{\hat{k}}(\mathbf{r}) d\mathbf{r}$$

- Hadrons: superposition of 3 shower classes:

$$L \propto f_{dep}(E) [c_h H_h(x) + c_f H_f(y) + c_l H_l(z)]$$

$$H_h(x) = \frac{(\beta_h x)^{\alpha_h - 1} e^{-\beta_h x}}{\Gamma(\alpha_h)}, \quad c_h = 1 - f_{\pi^0}(E)$$

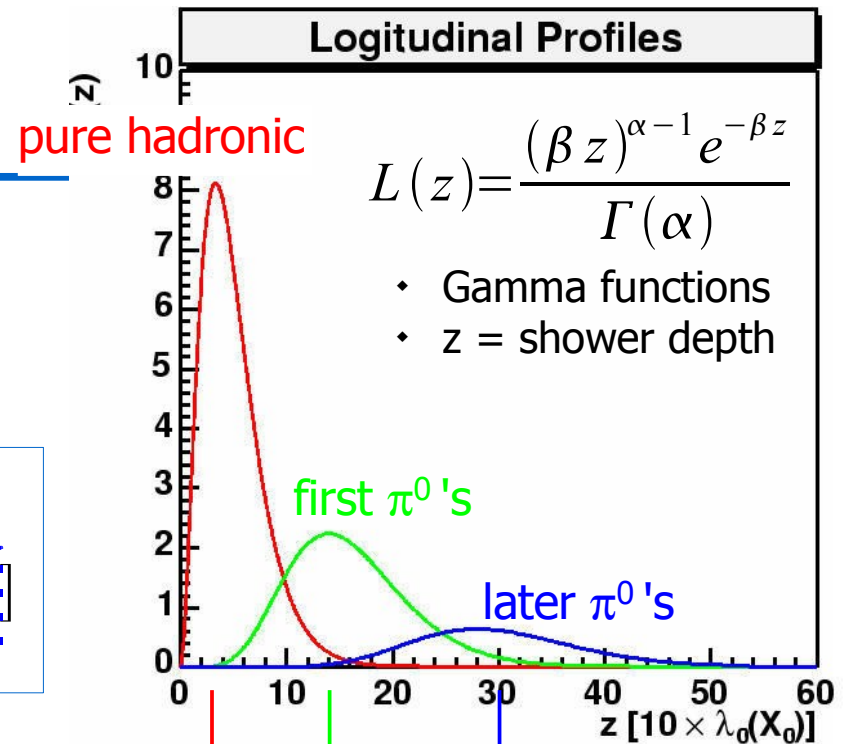
$$H_f(y) = \frac{(\beta_f y)^{\alpha_f - 1} e^{-\beta_f y}}{\Gamma(\alpha_f)}, \quad c_f = f_{\pi^0}(E) (1 - f_{\pi^0}^l(E))$$

$$H_l(z) = \frac{(\beta_l z)^{\alpha_l - 1} e^{-\beta_l z}}{\Gamma(\alpha_l)}, \quad c_l = f_{\pi^0}(E) f_{\pi^0}^l(E)$$

- Incident particle energy dependence of fractions

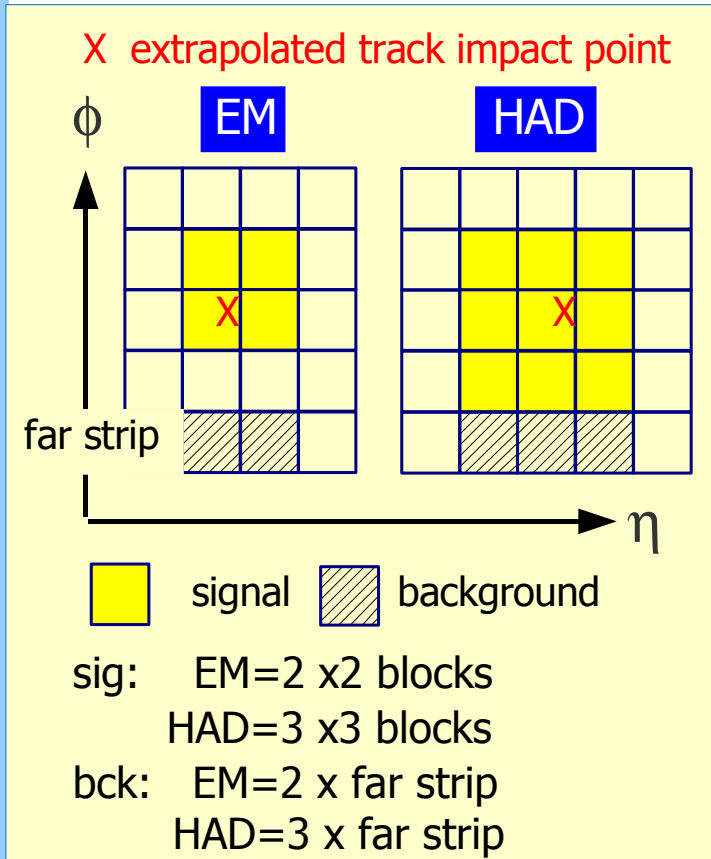
$$f_i(E) = a + b \tanh(c \log E + d) \quad (\text{typically})$$

...primary switches for Run-II tuning improvements!



Total of 20 parameters:  
 - means & widths of  
 - the class fractions f's,  
 - the α's and β's

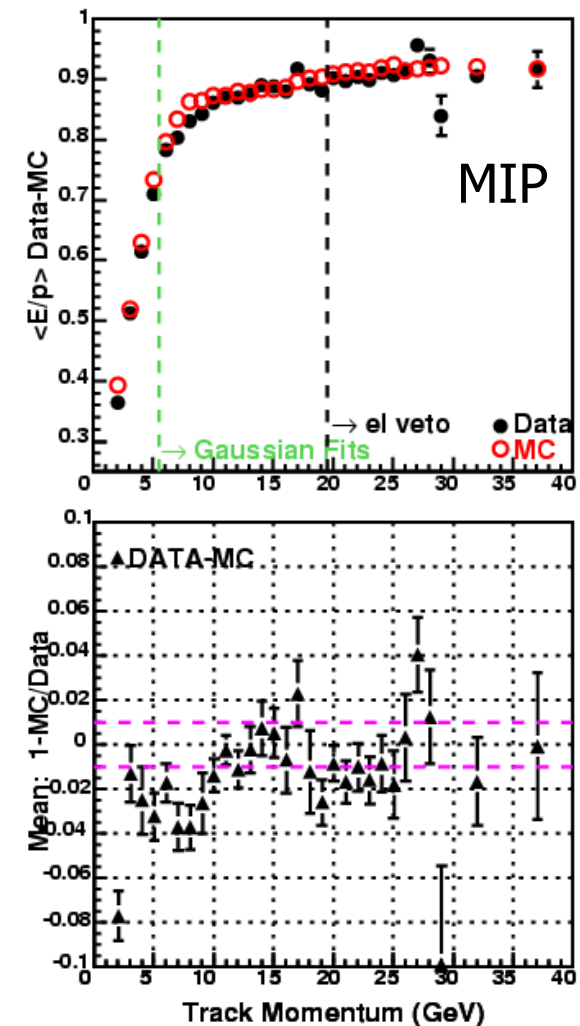
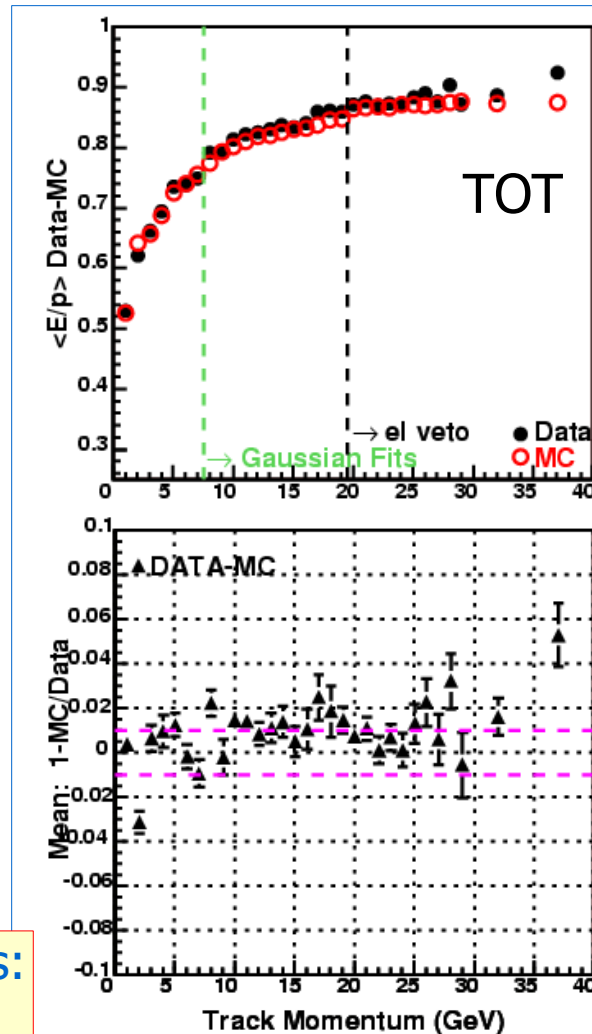
# Absolute Response Tuning (Central)



## Tuning

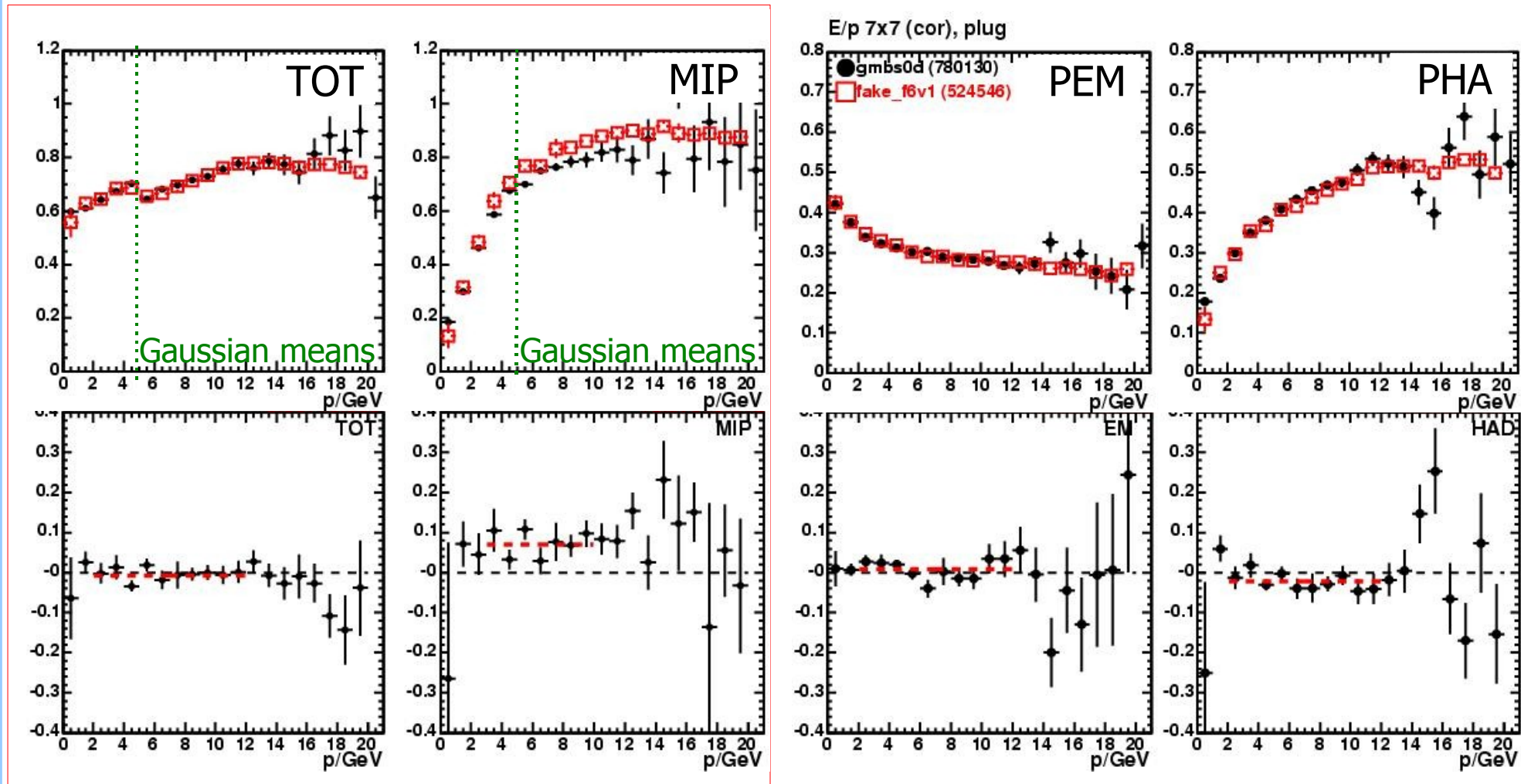
- FEDP and relative sampling fractions:

$$f_i(E) = a + b \tanh(c \log E + d)$$



- TOT and MIP is primary reference: shower almost fully contained  $\rightarrow$  response less dependent on shower starting point & particle flavor (appendix)
- TOT is basis for JES uncertainty determination

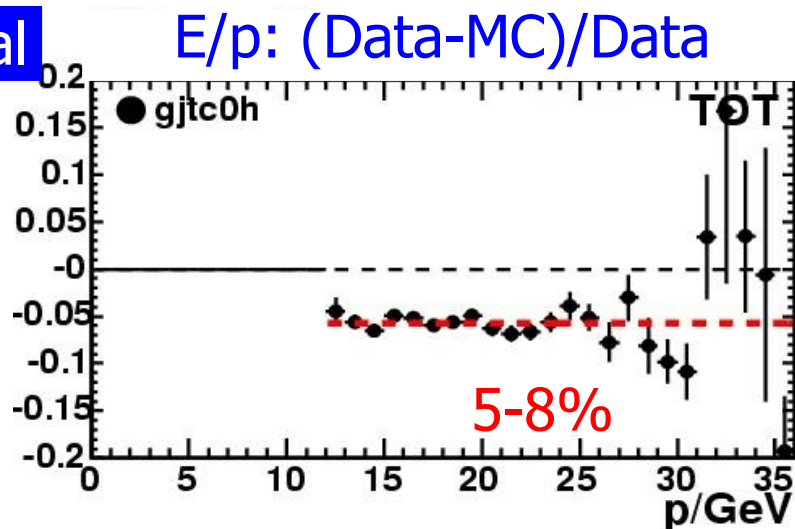
# Absolute Response Tuning (Plug)



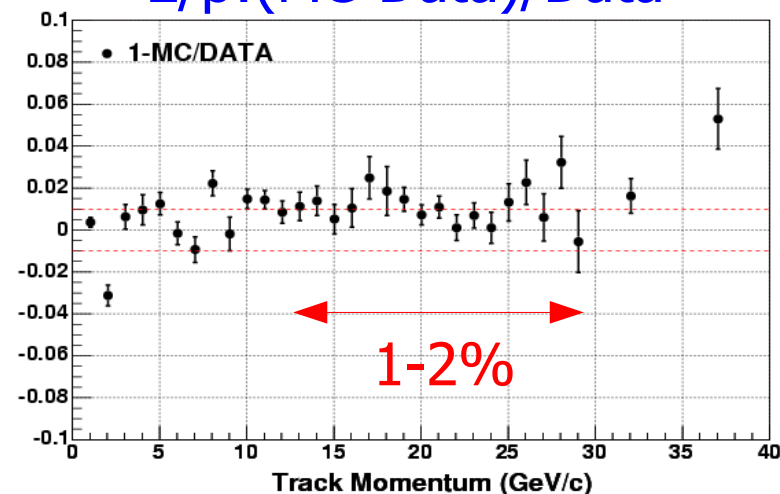
- Priority to get TOT right
- Moderate discrepancy in MIP

# Changes

Central

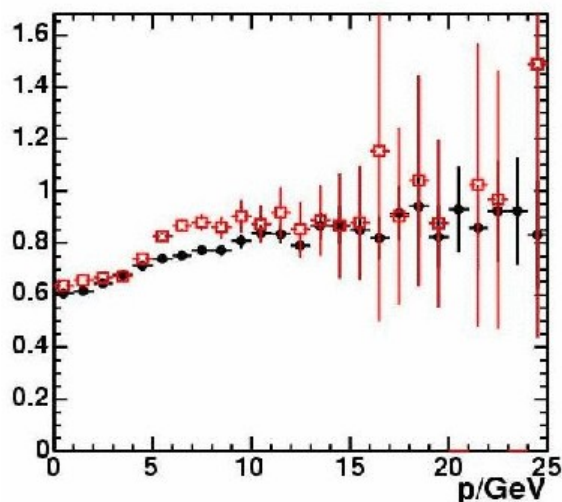


E/p:(MC-Data)/Data



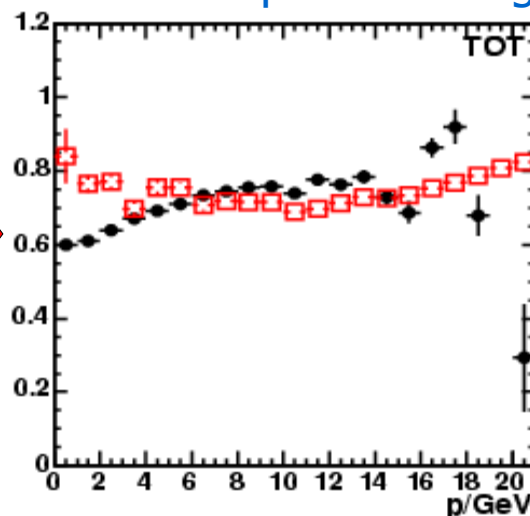
Plug

a) initial picture

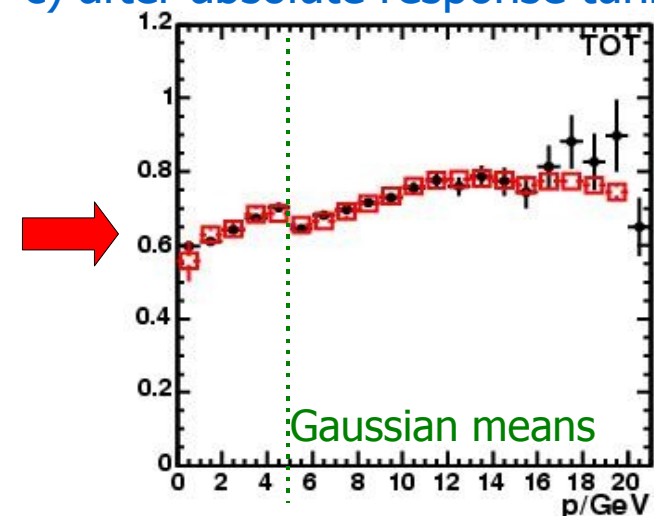


E/p (total response)

b) after lateral profile tuning



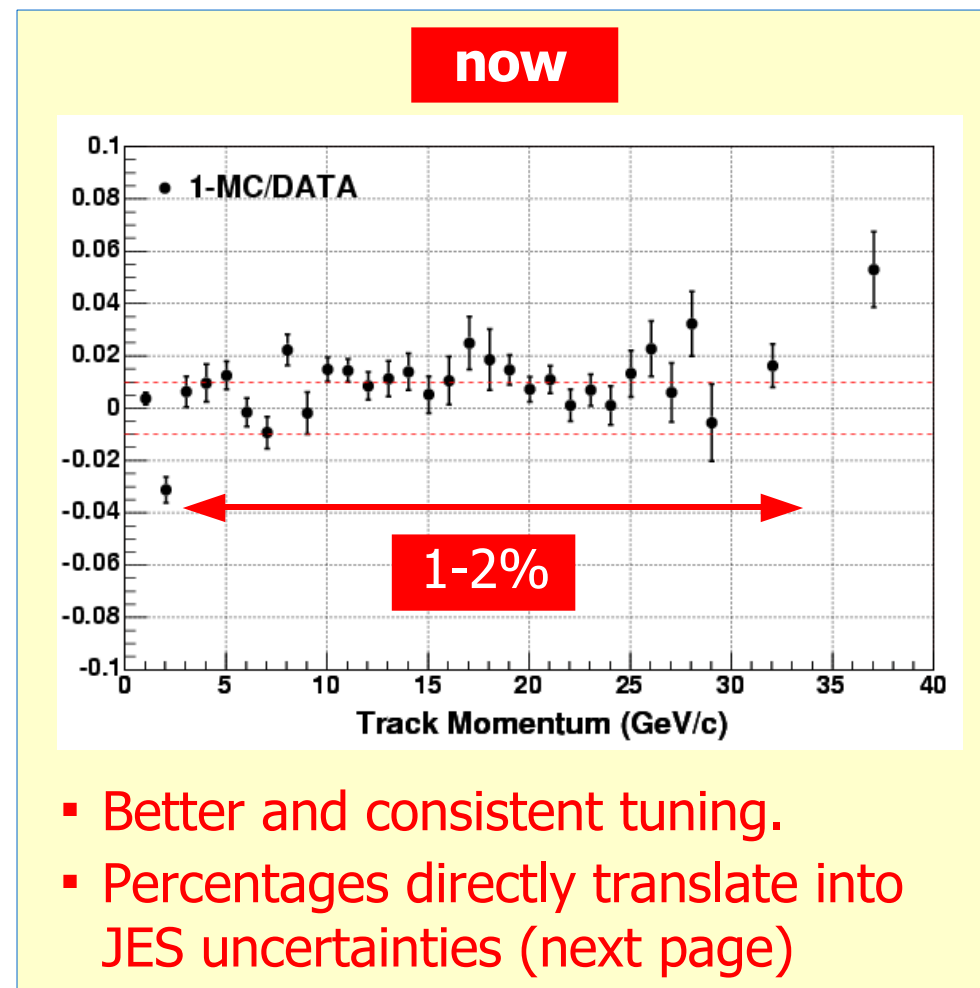
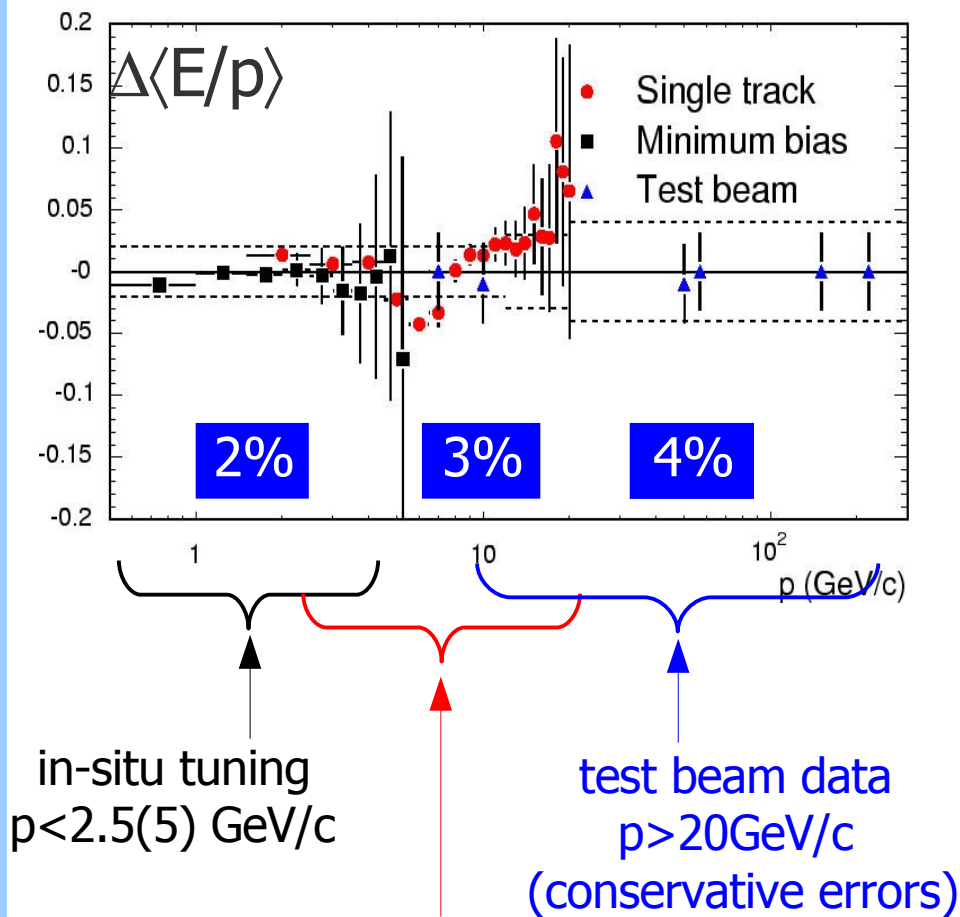
c) after absolute response tuning



- Have gained substantial in-situ control up to 40 (20) GeV in Central (Plug)

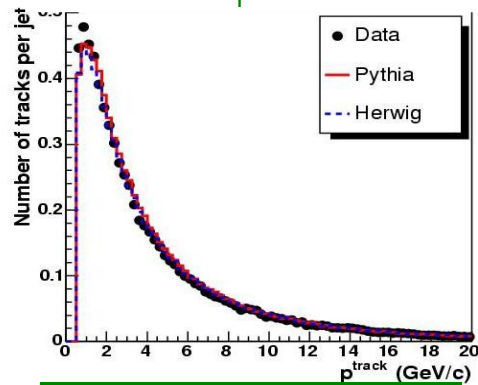
# Simulation Performance

Performance early Run-II effective in past/ongoing CDF publications:

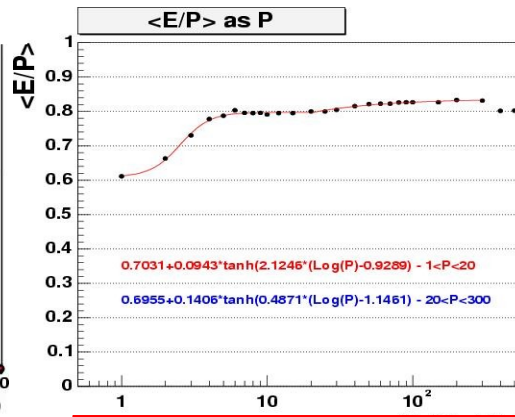


# Jet Energy Scale Uncertainties

e.g. jet  $p_T = 50-60 \text{ GeV}$

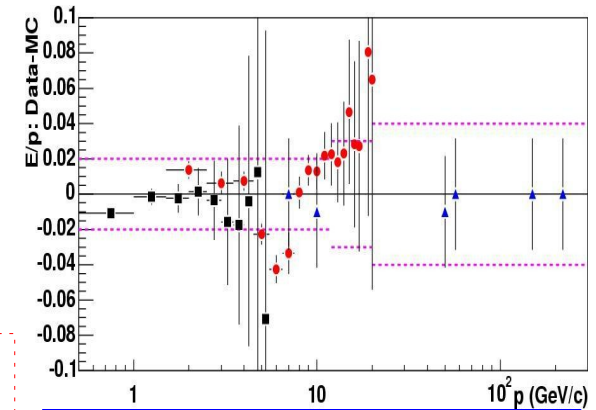


particle spectrum



$\langle E/p \rangle$  (had)

$\langle E/p \rangle(e, \gamma) = 1$   
(30% fraction)

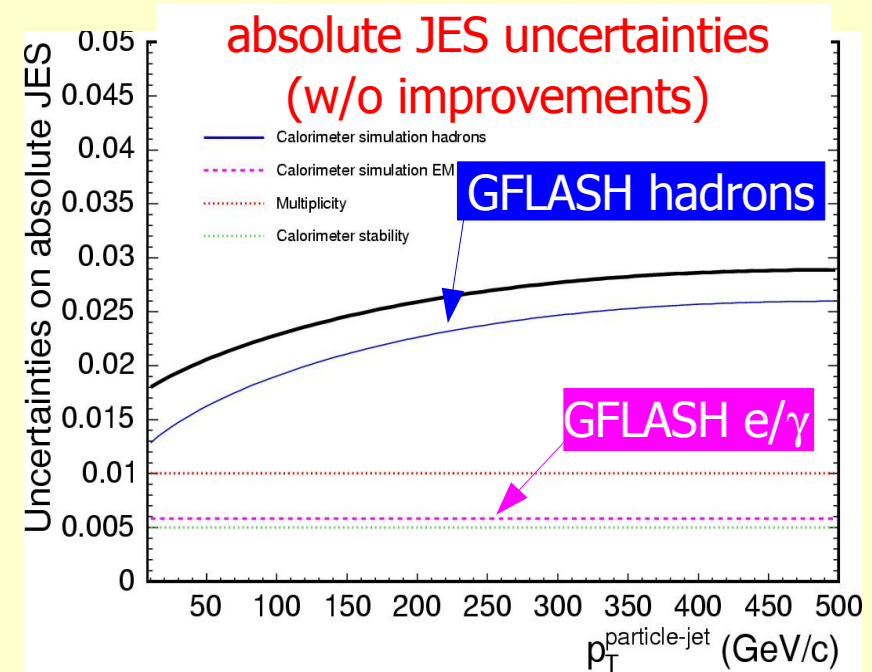


$\Delta \langle E/p \rangle$

$$\frac{\Delta E}{E} = \frac{1}{E} \sum_i p_i \left[ \frac{E_i}{p_i} \right] \Delta \left\langle \frac{E_i}{p_i} \right\rangle$$

- Derived from "first principles" :
- Convolution of MC/data difference with the jet's particle spectrum and E/p response

→ absolute JES uncertainty

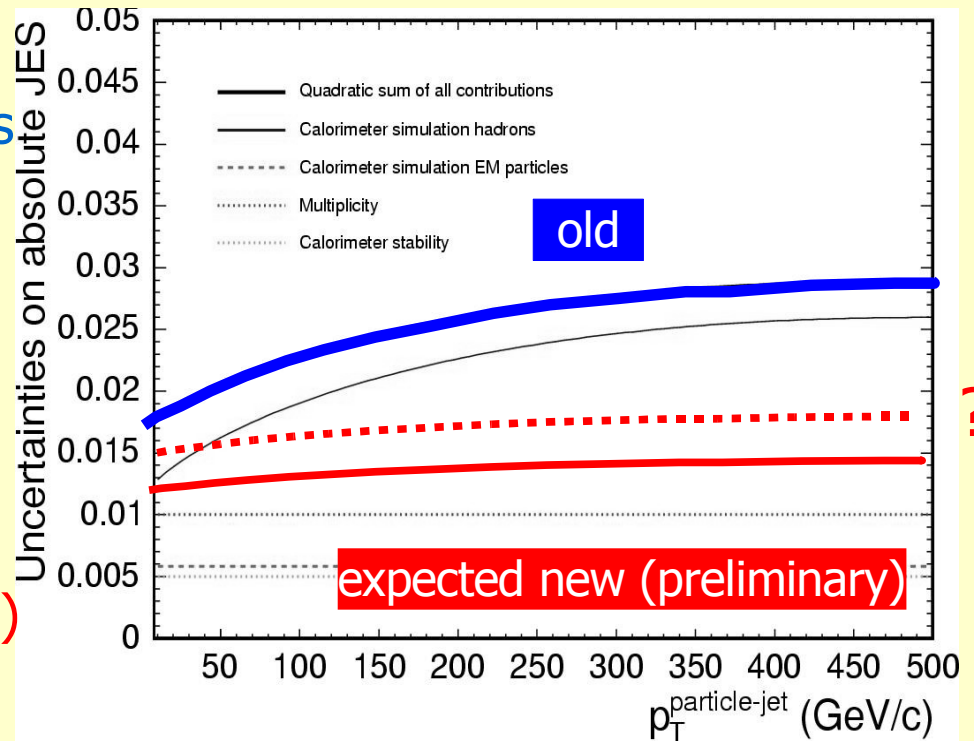




# Absolute JES Uncertainty

- We can get rid of old test beam based conservative high  $p$  estimates
- Have better agreement at low and medium  $p$
- Absolute E/p uncertainty reduced by a factor of  $\sim 2$ :

expected JES uncertainty:  
 1.8-2.8%  $\rightarrow$  1.4-2.0% (preliminary)



Impact to performance top quark mass measurements:

- w/o in situ JES: di-lepton channel
- w/ in situ JES but a-priory JES constraint: all-jets channel
- reduction of residual JES uncertainties: all analyses

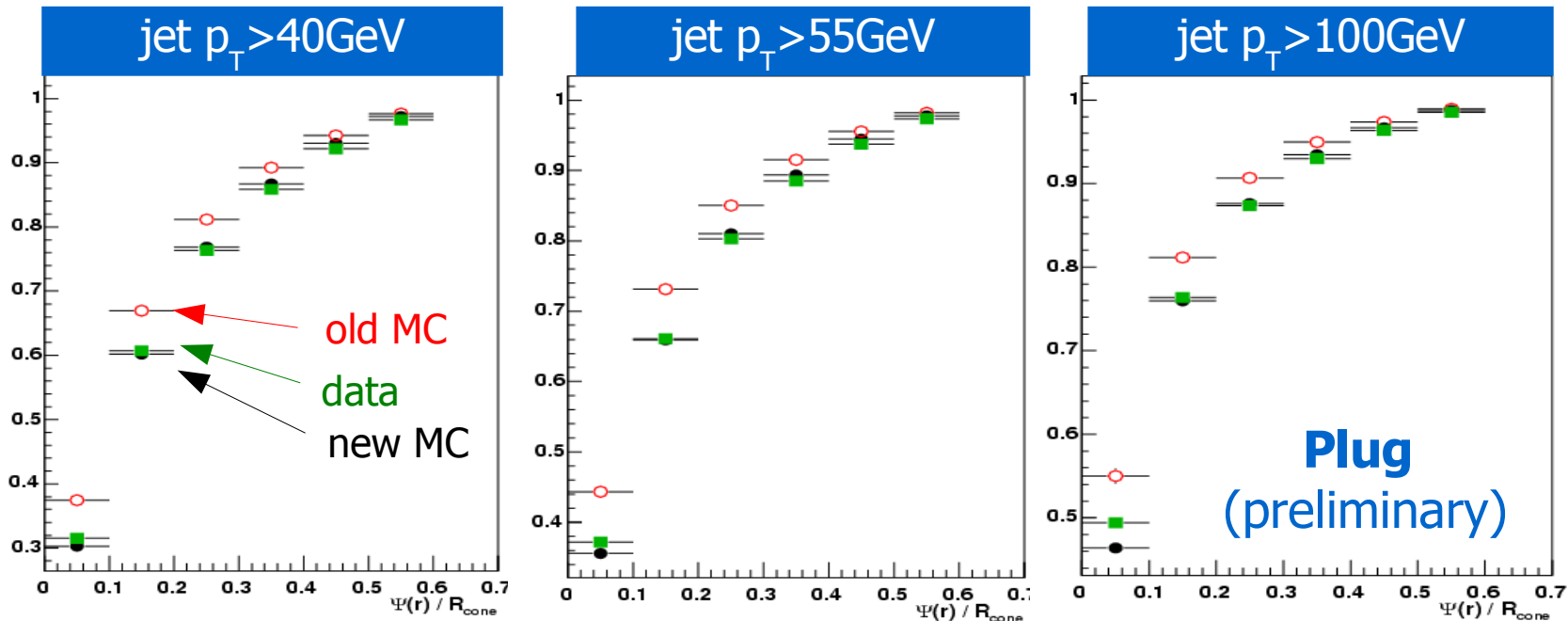
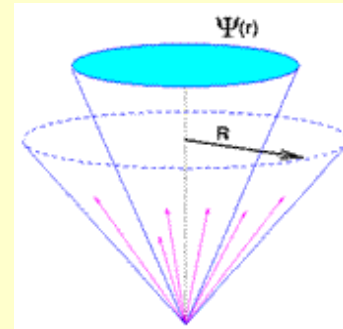
→ Reduction of  $\Delta M_{\text{top}}$  (Absolute),  $\Delta M_{\text{top}}(\text{JES}_{\text{stat}})$ ?

... more comments later!

# Jet Shapes

- For example: Integrated jet energy flow

$$\Psi(r) = \frac{1}{N_{jets}} \sum_{jets} \frac{p_T(0,r)}{p_T(0,R)}$$

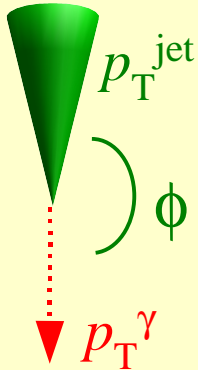


- Much better agreement

→ reduces bias in relative correction Plug to Central } (next slides)  
 → impact to OOC uncertainties

# OOC Uncertainties

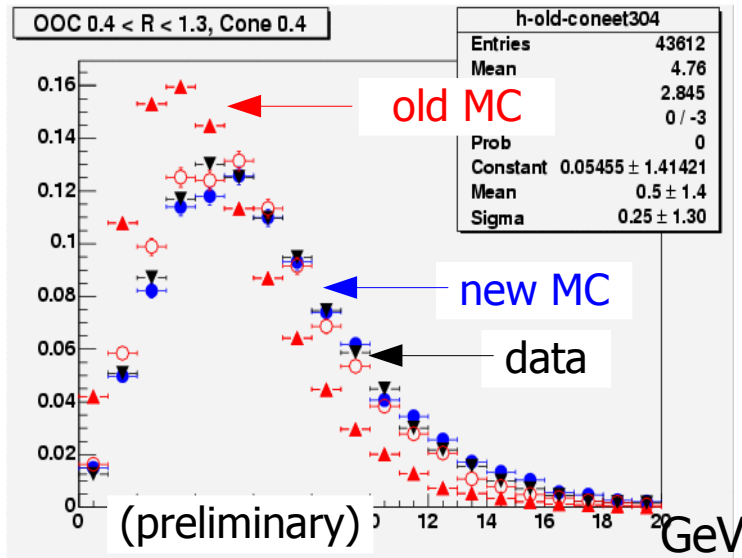
- Photon-jet balance technique: validate the probe jet using well measured photon energy



$$f_y = 1 - \frac{p_T^{jet}}{p_T^y}$$

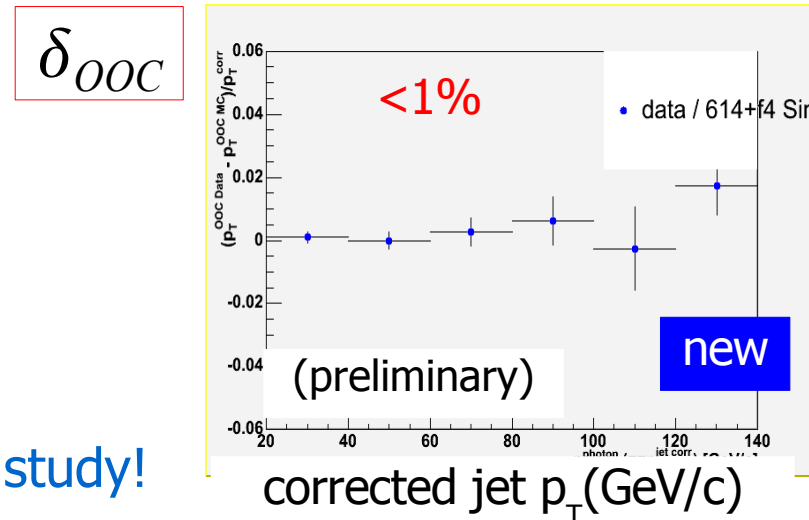
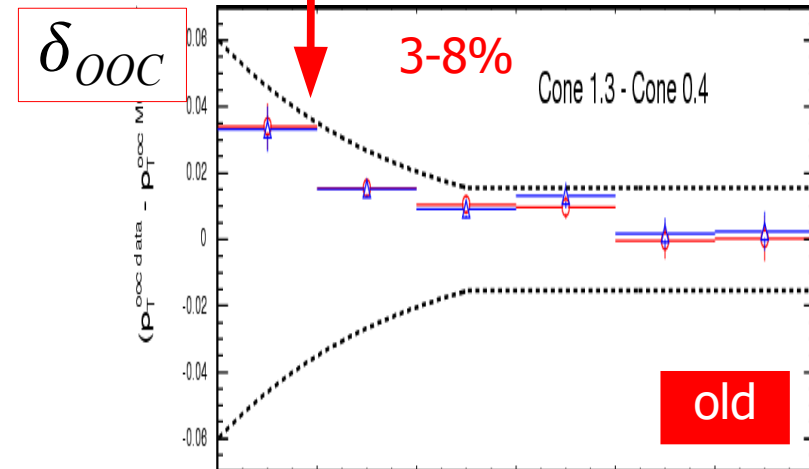
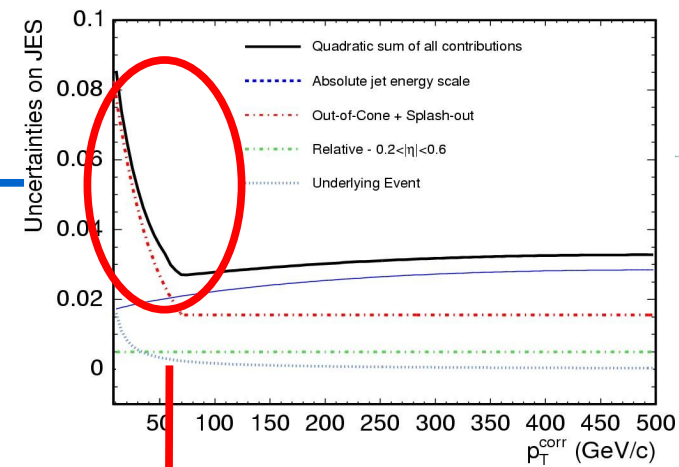
$$\delta_{OOC} = f_y^{data, cor} - f_y^{MC, cor}$$

OOC transverse energy flow (R=0.4...1.3)



→ Reduction of  $\Delta M_{top}$  (OOC)?

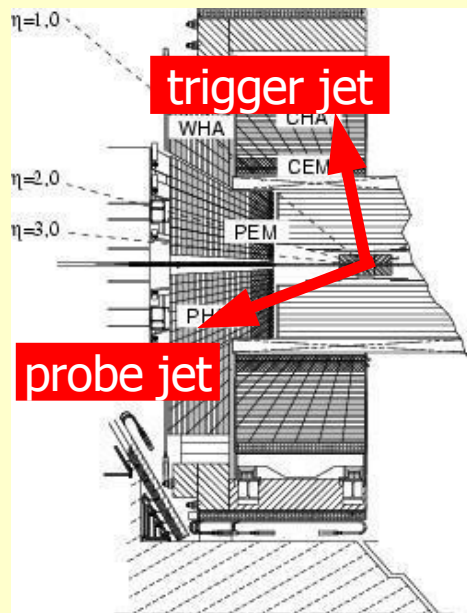
... still under study!



# Di-Jet Balance

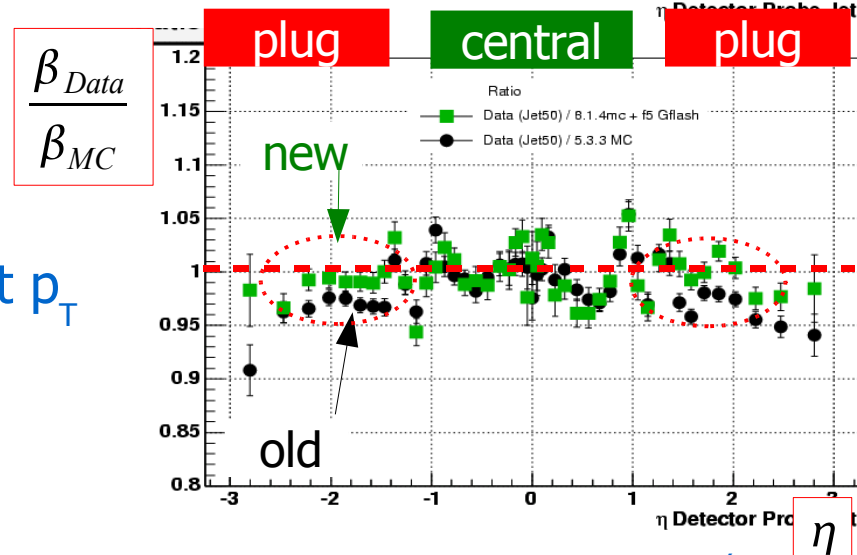
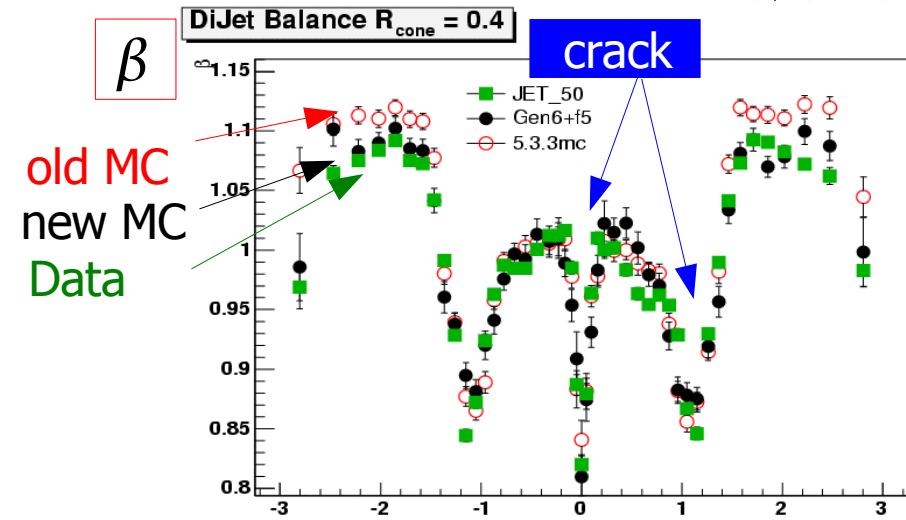
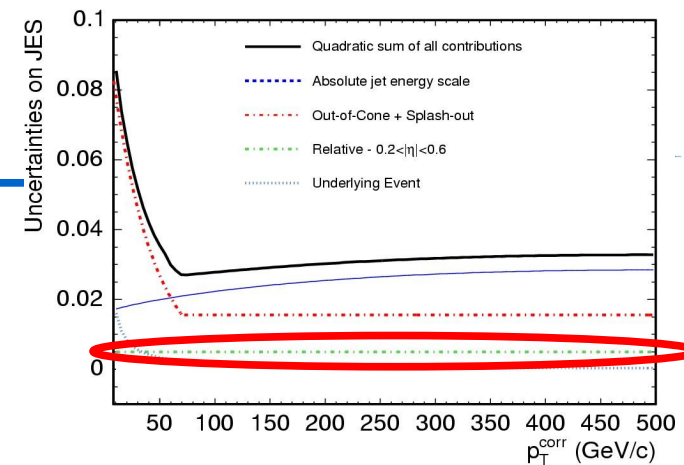
## Di-jet balancing technique

- Monitoring and correction of the inhomogeneous calorimeter response using reference jet  $p_T$  in Central part.



$$f = \frac{p_T^{probe} - p_T^{trigger}}{(p_T^{probe} + p_T^{trigger})/2}$$

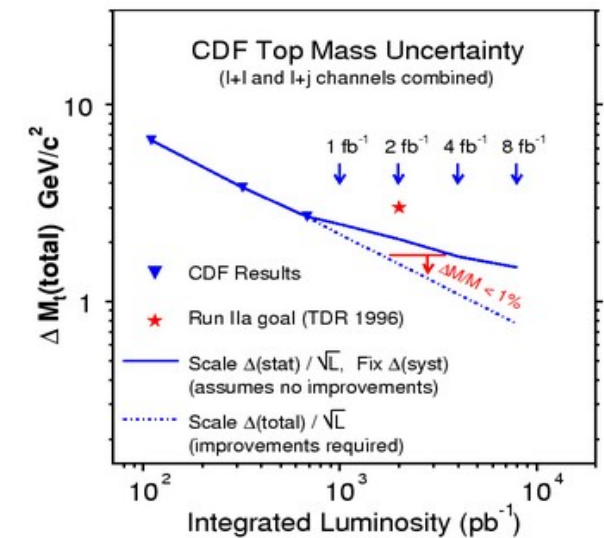
$$\beta \equiv \frac{2+f}{2-f} = \frac{p_T^{probe}}{p_T^{trigger}}$$



- Improvements for certain cone sizes and jet  $p_T$

→ Reduction of  $\Delta M_{top}$  (Relative)?

# Towards Precision Top Quark Mass



# Di-Lepton Channel

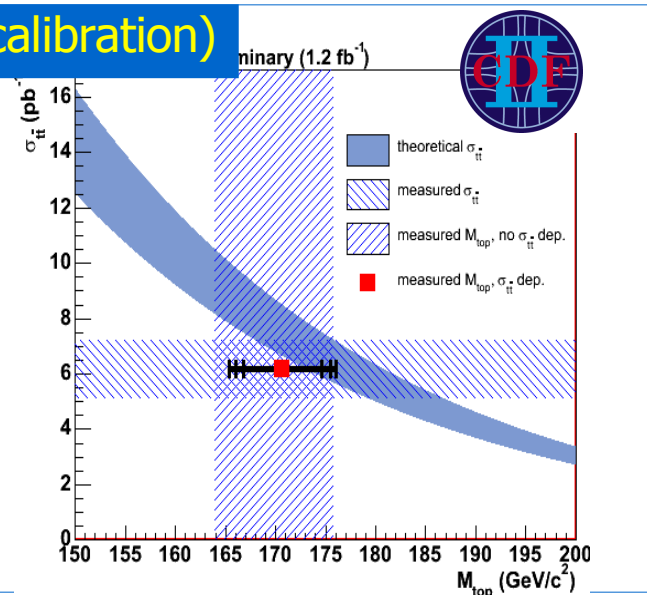
Template Method,  $p_z(tt)$  assumption,  $1.2\text{fb}^{-1}$  (no in situ JES calibration)

w/ cross section constraint (reduced JES systematics)

$$M_{\text{top}} = 170.7^{+4.2}_{-3.9} (\text{stat.}) \pm 2.6 (\text{syst.}) \pm 2.4 (\text{theo.}) \text{GeV}/c^2$$

JES <sub>tot</sub>	b-JES	JES	Relative	Absolute	OOC
GeV/c <sup>2</sup>	0.9	1.5	0.3	1.1	1.0

expect to improve



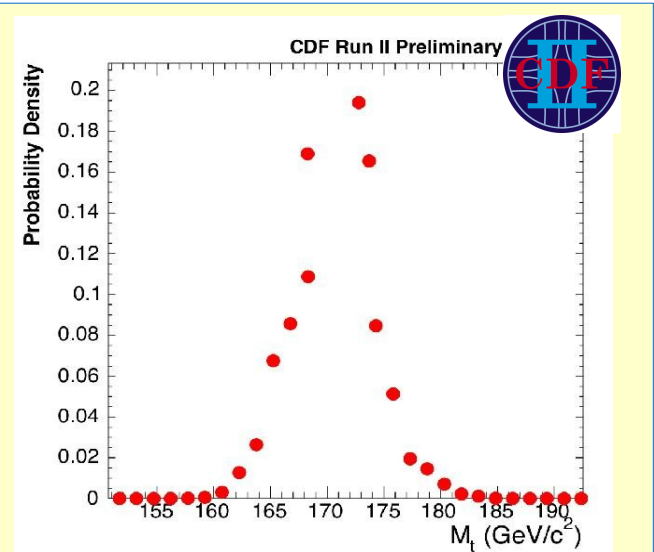
Matrix Element Method,  $1.8\text{fb}^{-1}$  (no in situ JES calibration)

$$M_{\text{top}} = 170.4 \pm 3.1 (\text{stat.}) \pm 3.0 (\text{syst.}) \text{GeV}/c^2$$

JES <sub>tot</sub>	b-JES	JES	Relative	Absolute	OOC
GeV/c <sup>2</sup>	0.2	2.6	0.1	1.8	1.8

expect to improve

$\delta(\Delta m_t)/\delta(\Delta_{\text{JES}})$  difficult to assess : 0.9? <0.1?



Best di-lepton measurement.

# All-Jets Channel

ME assisted Template Method,  $0.94\text{fb}^{-1}$  (in situ JES calibration)

a priori JES constraint

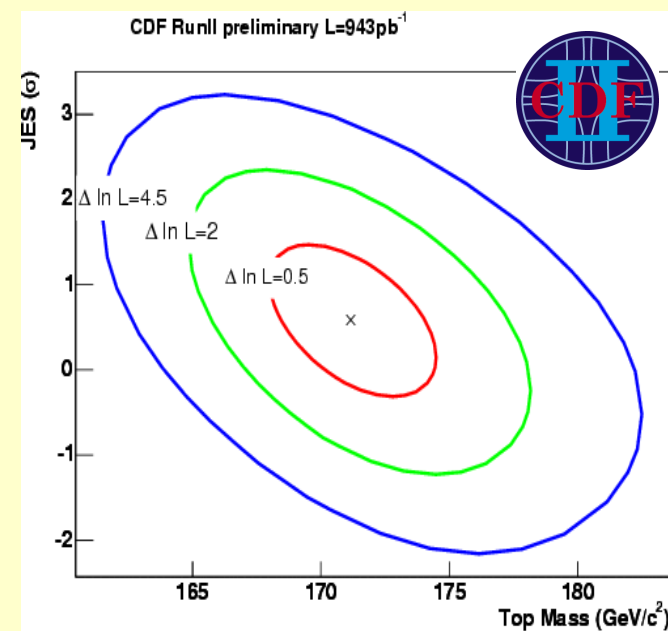
$$L = L_{1\text{ tag}}(m_t, \text{JES}) \times L_{2\text{ tag}}(m_t, \text{JES}) \times \exp\left(\frac{-(\text{JES} - \text{JES}_{\text{exp}})^2}{2}\right)$$

$$M_{\text{top}} = 171.1 \pm 3.7 (\text{stat.} + \text{JES}) \pm 2.1 (\text{syst.}) \text{ GeV}/c^2$$

JES	Stat	b-JES	Residual	Relative	Absolute	OOC
GeV/c <sup>2</sup>	2.4	0.4	0.7	0.2	0.5	0.5

expect to improve

- Dominant systematic uncertainties:
  - gluon FSR,
  - background modeling
  - generator
 }  $O(\sim 1\text{GeV}/c^2)$  each



Best all-jets measurement.

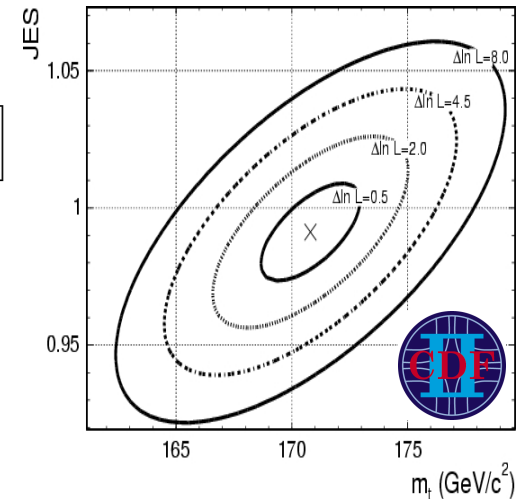
# JES Uncertainties (Lepton-Jets)

## Matrix Element Method, $0.96\text{pb}^{-1}$ (in situ JES calibration)

$$L(M_{\text{top}}, \text{JES}, C_s) \propto \prod_{i=1}^{\text{events}} \left[ C_s P_{t\bar{t}}^{(i)}(M_{\text{top}}, \text{JES}) + (1 - C_s) P_{\text{bck}}^{(i)}(\text{JES}) \right]$$

$$M_{\text{top}} = 170.8 \pm 2.2 (\text{stat.} + \text{JES}) \pm 1.4 (\text{syst.}) \text{ GeV}/c^2$$

JES	Stat	b-JES	Residual
GeV/c <sup>2</sup>	1.5	0.6	0.4



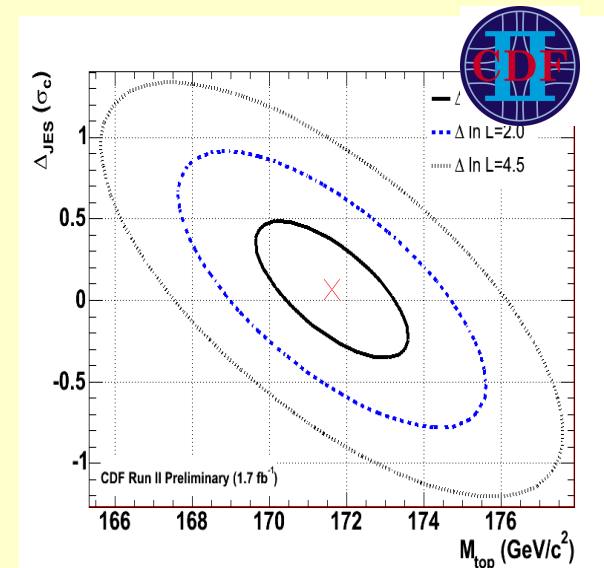
## Template Method, $1.7\text{fb}^{-1}$ (in situ JES calibration)

a priori JES constraint

$$L = L_{1 \text{ tag}}(m_t, \Delta_{\text{JES}}) \times L_{2 \text{ tag}}(m_t, \Delta_{\text{JES}}) \times \exp\left(\frac{-\Delta_{\text{JES}}^2}{2\sigma_c^2}\right)$$

$$M_{\text{top}} = 171.6 \pm 2.1 (\text{stat.} + \text{JES}) \pm 1.1 (\text{syst.}) \text{ GeV}/c^2$$

JES	Stat	b-JES	Residual	
GeV/c <sup>2</sup>	1.3	0.6	0.6	dominating systematics



- ISR/FSR modeling  $O(\sim 0.5\text{GeV}/c^2)$

**Best single measurement.**



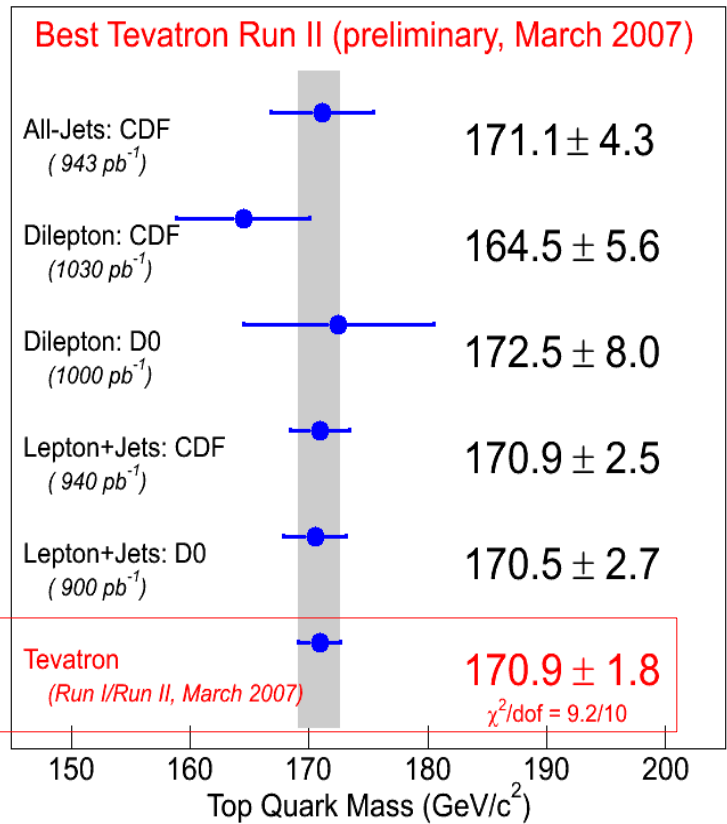
# Precision vs. Consistency

## Tevatron combination (March '07)

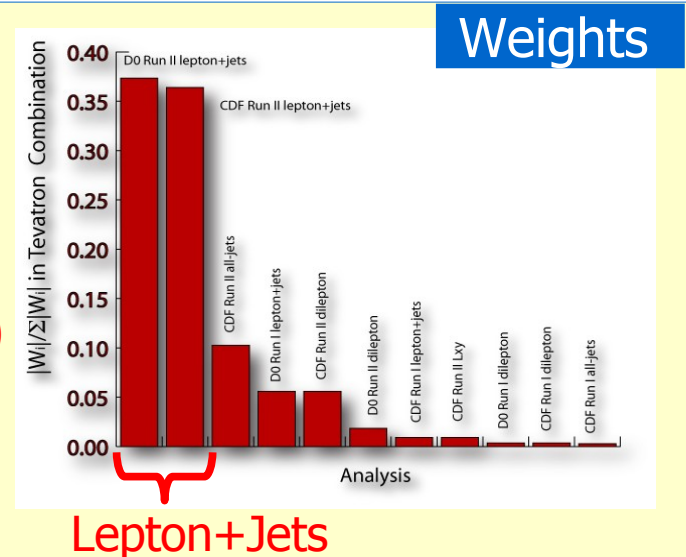
Parameter	Value (GeV/c <sup>2</sup> )	Correlations
all-jets	172.2 ± 4.1	1.00
lep-jets	171.2 ± 1.9	0.21 1.00
di-lep	163.5 ± 4.5	0.15 0.30 1.00

$p$  (di-lep/all-jets) = 7%  
 $p$  (lep-jets/all-jets) = 75%  
 $p$  (di-lep/lep-jets) = 12%

2.4%  
1.1%  
2.8%  
1.1%



- Can we **trust** increased precision? Are we **biased** by unknown systematics (e.g. color reconnection)?
- Need higher precision in non-golden channels with different hadronic activity to verify  
 → **reduction of  $\Delta_{JES}$  essential** (e.g. di-lepton channel)
- Alternate less JES sensitive methods important  
 - lepton  $p_T$  | decay length technique (appendix)



# Outlook



- Confidence through a consistent picture of many top mass measurements at Tevatron

Combined CDF&D0 result (March '07): **1.1%**

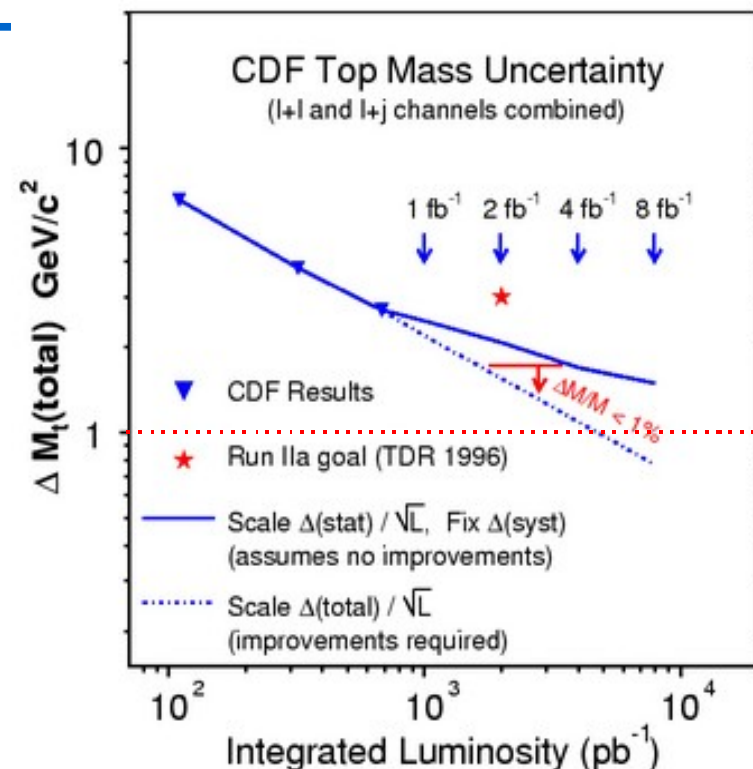
$$M_{\text{top}} = 170.9 \pm 1.8 \text{ GeV}/c^2$$

- Lessons from Run-II: Improvements are based on

- High b-tagging efficiency
- Improved analysis techniques
- In-situ W-jj calibration of the JES

- Claiming high precision requires mutual verification in all channels.
- We are therefore awaiting how future measurements will benefit from reduced JES uncertainties through better calorimeter simulation.
- Limiting factor at the end of Run-II expected to be ISR/FSR (=theoretical).
- Goal:  $\Delta M_{\text{top}} < 1 \text{ GeV}/c^2$  at the end of Run-II (=5-10 years LHC!!!)

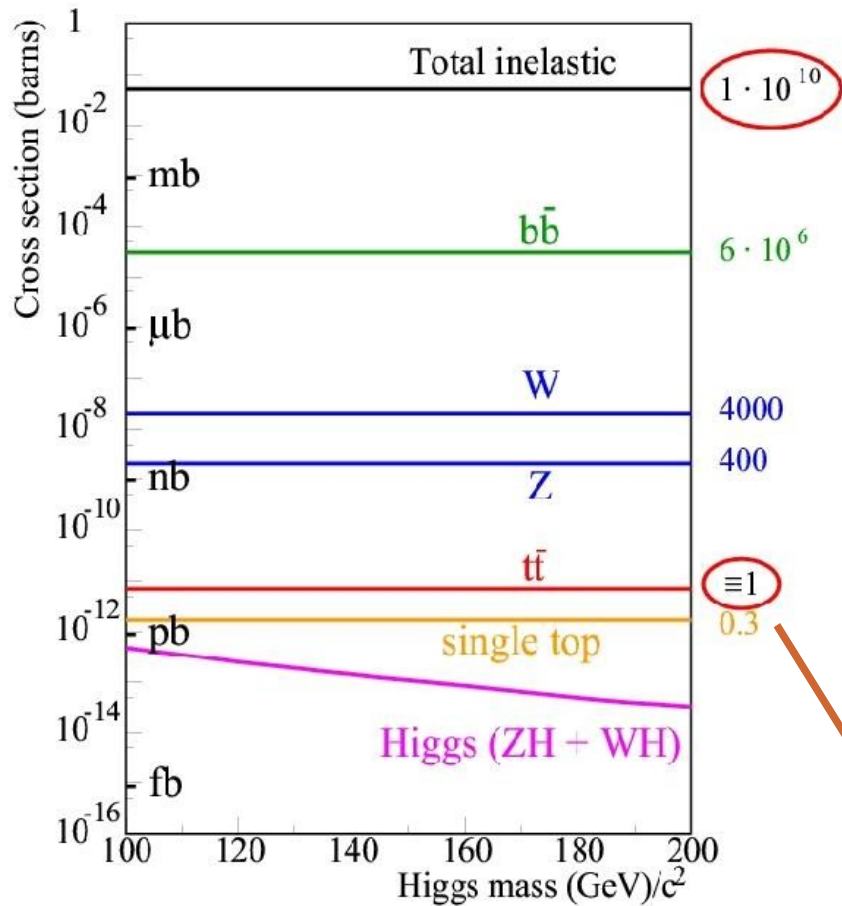
**Tevatron might be the lasting legacy for the top quark mass!**



# Backup Slides

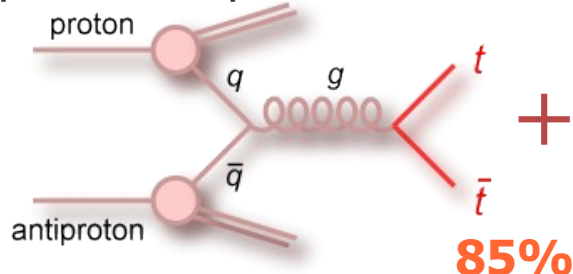


# Top Quark Production

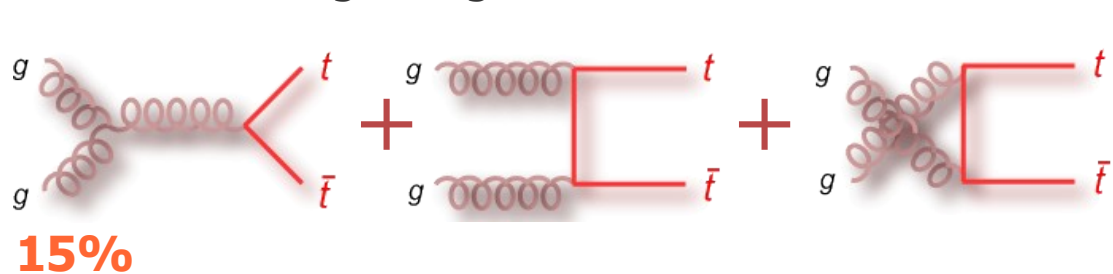


- Top quarks are mainly produced in pairs via quark/antiquark annihilation, and gluon/gluon fusion:  
 $\sigma_{t\bar{t}}(1.96\text{TeV}) = 6.1\text{pb}$
- Single top production:  
 $\sigma_{t\text{-channel}}(1.96\text{TeV}) = 1.98\text{pb}$   
 $\sigma_{s\text{-channel}}(1.96\text{TeV}) = 0.88\text{pb}$   
 ...ignored in mass analyses
- 1 top quark pair each  $10^{10}$  inelastic collisions ...  
 ... a needle in a haystack

quark/anti-quark annihilation



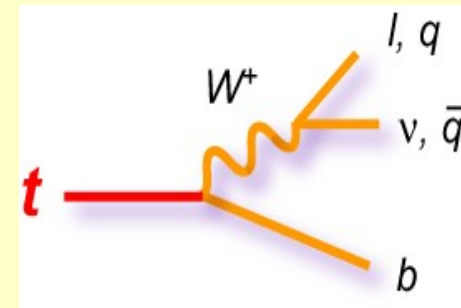
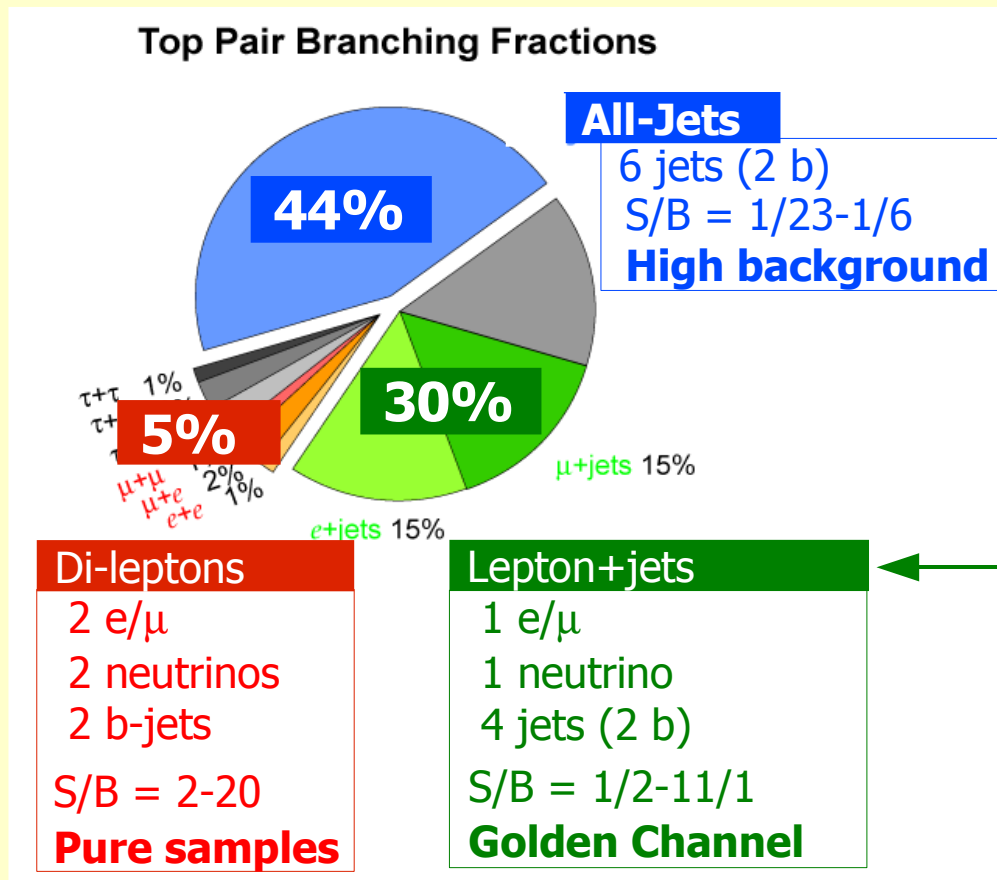
gluon/gluon fusion



# Top Quark Signatures

- SM top quark decays weakly before hadronization  
→ Can measure its properties directly: Mass, Spin, Charge ...
- BR ( $t \rightarrow Wb$ ) = 99.9% (CKM matrix)

- W decay determines experimental signature:



most precise results obtained in this channel

# Challenges of Top Quark Physics

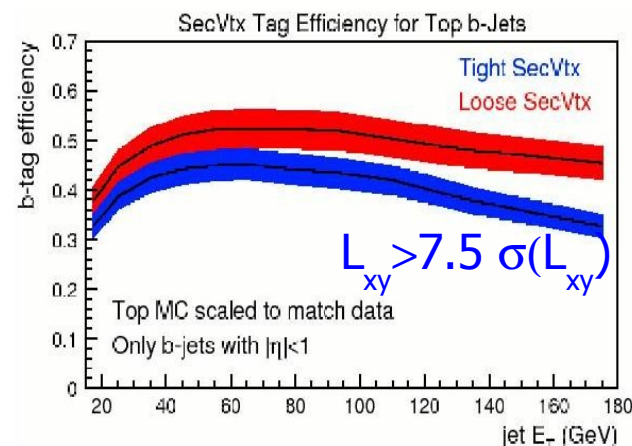


Requires full detector capabilities:

- Clean identification of electrons and muons  
→ charged leptons from W decay
- Undetected ("missing") energy  
→ neutrino reconstruction
- Secondary vertex tagging  
→ quark flavor (b or light)
- Calorimeter clusters ("jets")  
→ quark reconstruction

...crucial for reduction of background and jet-quark combinatorics

- $t\bar{t}$  tagging efficiency  $\sim 55\%$
- $t\bar{t}$  fake rate  $\sim 0.5\%$



fraction of tagged b jets vs. jet transverse energy

## Determination of the jet energy scale (JES)

- Correction of jet energies for detector effects, hadronization, multiple interactions, ...  
→ momenta of hadronic top decay products!
- JES currently known at  $\sim 3\%$  level → dominant uncertainty in all top quark mass measurements!

More details in 2<sup>nd</sup> part of talk

# Measurement Strategies (1)

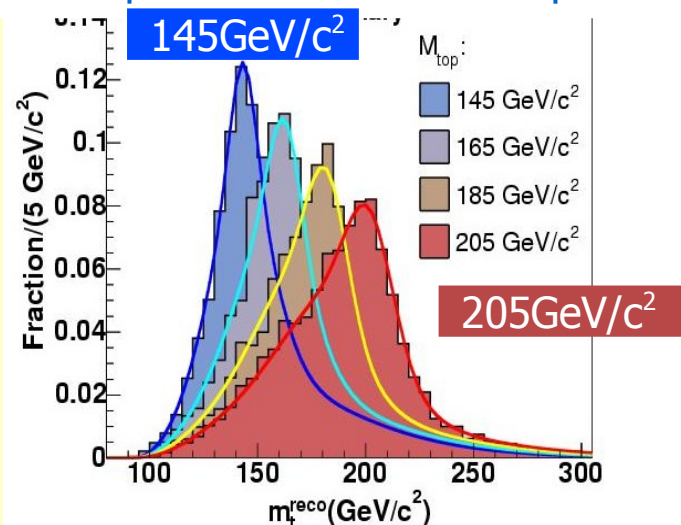
## Template Method (TM):

- Classical Run-I strategy
- Calculate one observable per event correlated with  $M_{top}$ .
- Compare simulated distributions for signal+ background with varying  $M_{top}$  with data to obtain  $M_{top}$ .

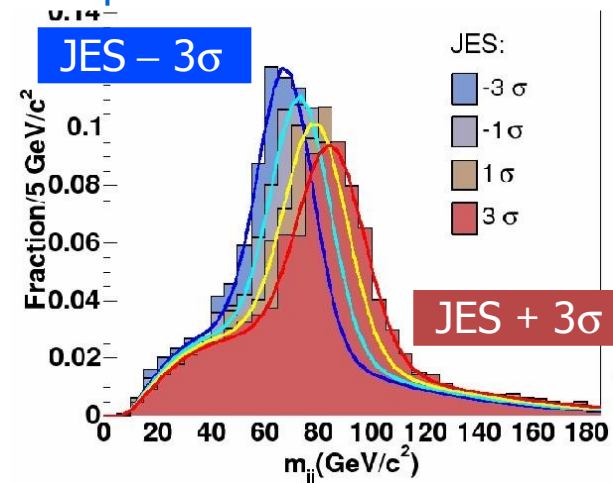
+ computationally simple

– limited kinematic information, just one number per event

Example: “reconstructed” top mass



Example: “reconstructed” W mass

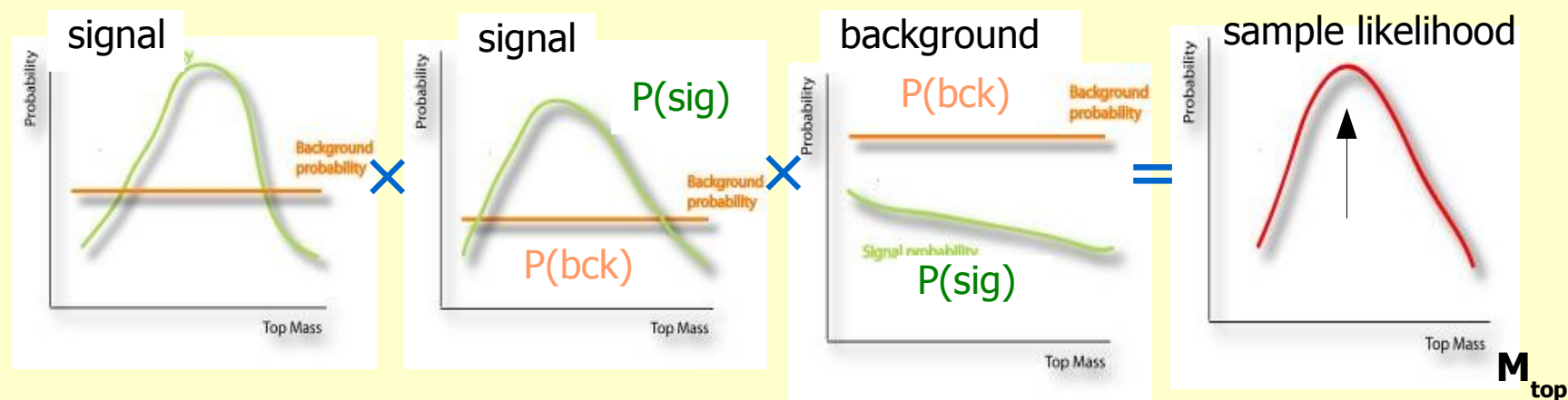


- Important extensions developed in Run-II, e.g. use of a 2<sup>nd</sup> variable for JES calibration.

# Measurement Strategies (2)

## Matrix Element Method (ME):

- Calculate a per-event probability density curve (from matrix element calculations) for signal and background as function of  $M_{\text{top}}$ .
- Multiply probabilities to extract most likely  $M_{\text{top}}$  for the whole data sample.



- + per-event probability curve enhances statistical power
- extremely CPU intensive numerical integrations

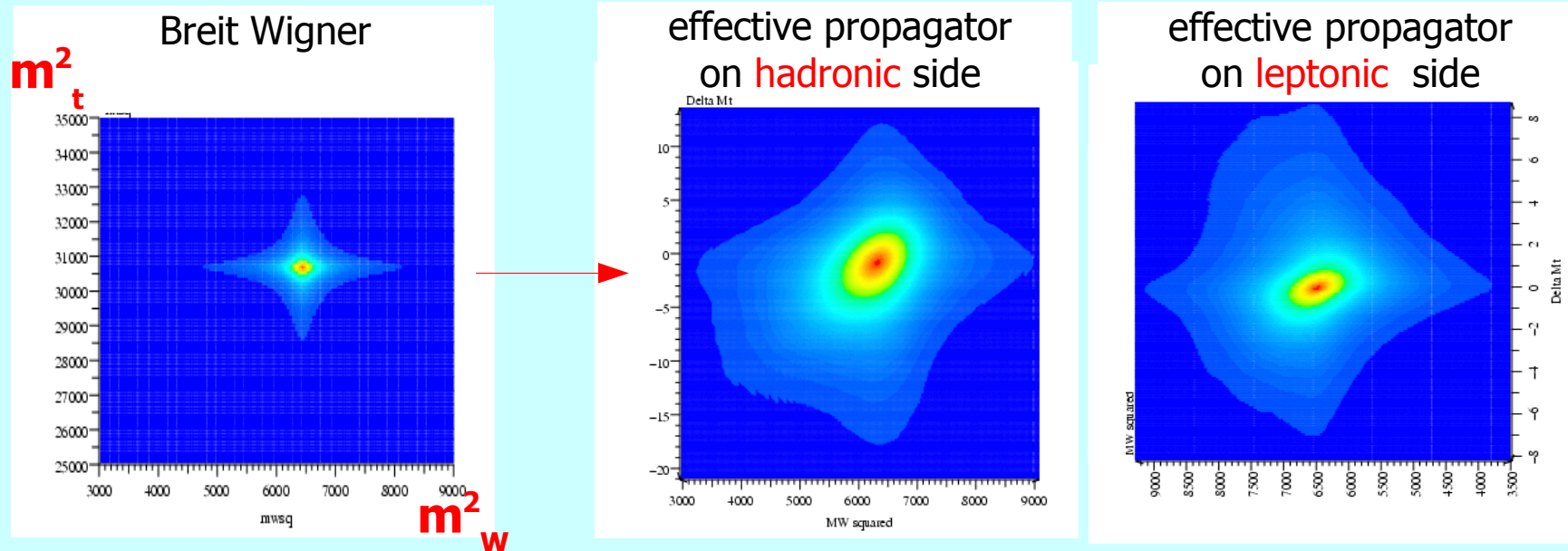
- ME Method extended using 2-dimensional likelihoods ( $M_{\text{top}}$ , JES)
- Additional event weighting using S/B discriminants, b-tagging information etc.



# Integration

- Integration over full phase space in 22 dimensions intractable, make simplifying assumptions:
  - quark angles / charged lepton momentum are perfectly measured
  - quark / charged lepton / neutrino masses are known
- Seven integration variables remaining:
  - $m_W^2$  (had),  $m_t^2$  (had),  $m_W^2$  (lep),  $m_t^2$  (lep),  $\log(p_1/p_2)$  (light quarks),  $p_x(\bar{t}t)$ ,  $p_y(\bar{t}t)$

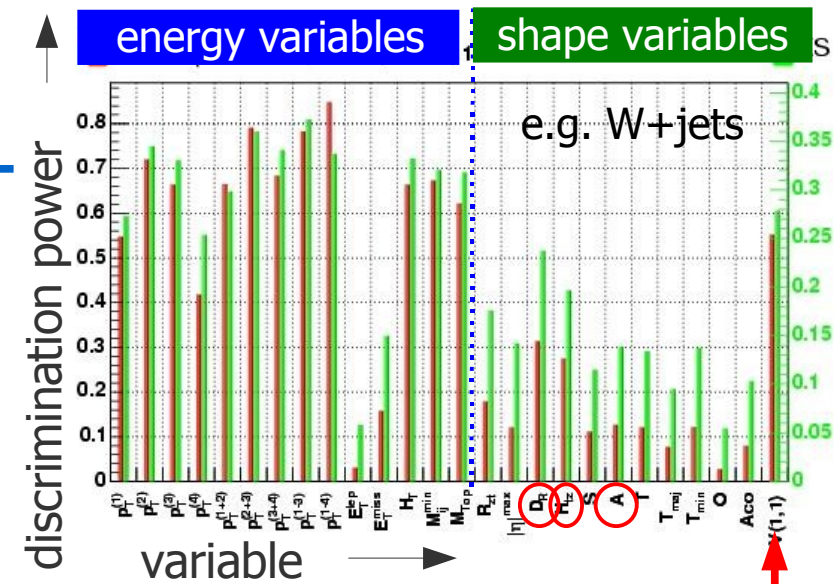
- Effective propagators are used when integrating over mass variables  
 → corrects for mismatch between ME, MC and integration assumptions



# S/B Discriminant

Many candidates to choose from:

- **Energy variables** (e.g. jet transverse energy sum) higher S/B discrimination but also largely correlated with  $m_t$ /JES
- **Shape variables** (e.g. aplanarity) lower S/B but smaller  $m_t$ /JES dependence



- Linear combination of variables  
→  $m_t$  / JES systematics mutually cancel

$$A = 1.5 Q_1 \text{ (aplanarity)}$$

$$Q_1 < Q_2 < Q_3 \text{ EV of } T_{\alpha\beta} = \sum_i p_\alpha^{(i)} p_\beta^{(i)} / (p^{(i)})^2$$

$$D_R = \min(\Delta R_{ij}) \times p_T^{(\min)} / E_T^{\text{lep}}$$

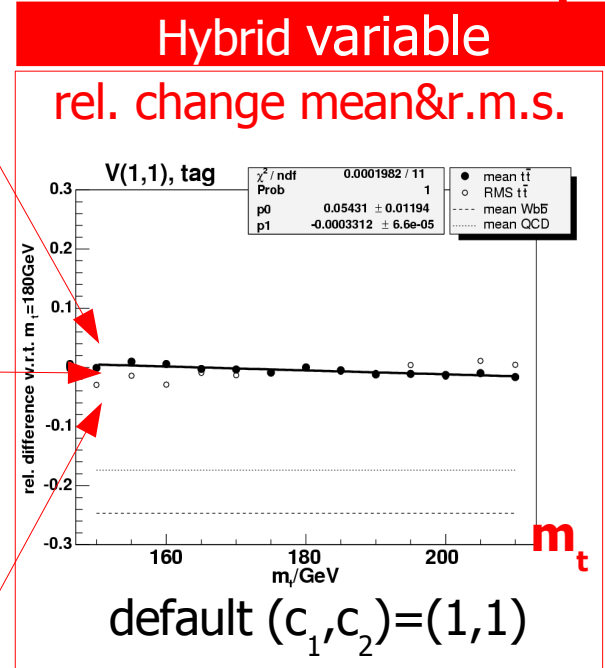
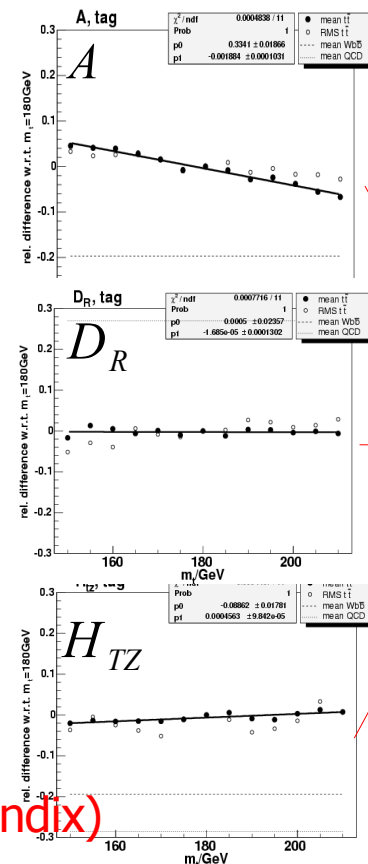
$p_T^{(\min)}$ : smaller  $p_T$  of the min. separation pair

$$H_{TZ} = \sum_{i=2..4} p_T^{(i)} / \left( \sum_{i=1..4} p_z^{(i)} + p_z^{(\text{lep})} + p_z^{(\nu)} \right)$$

$p_z^{(\nu)}$ : smallest of neutrino  $p_z$  solutions

$$V = (\hat{c}_1 A + \hat{c}_2 D_R + \hat{c}_3 H_{TZ}) \times N$$

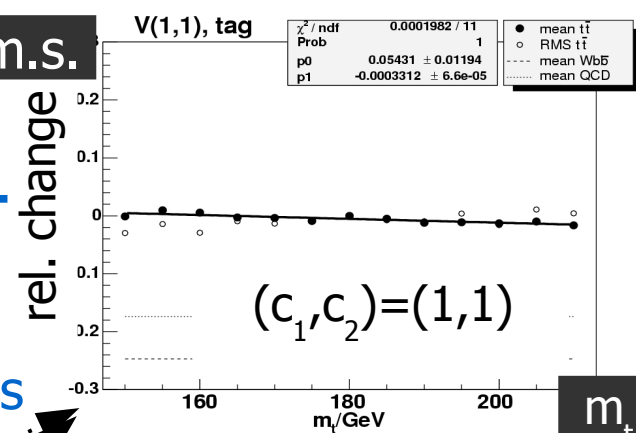
...systematic fine tuning of coefficients (appendix)



# Hybrid Variable

- Fine tuning of two independent coefficients
- Study relative changes w.r.t. reference distribution
- S/B discrimination quantified by divergence measures

mean & r.m.s.

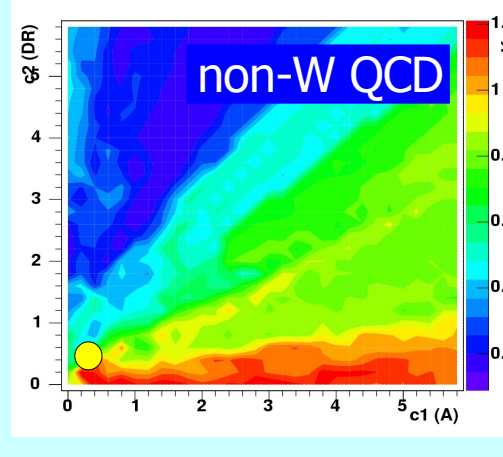
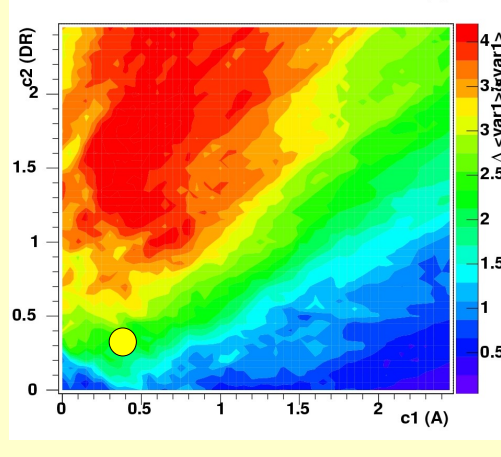
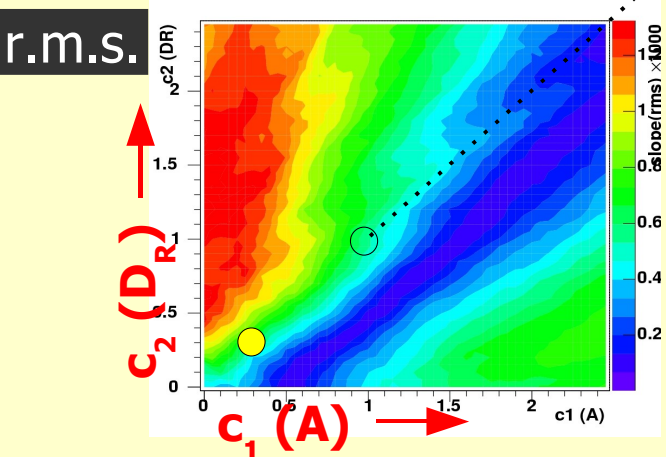
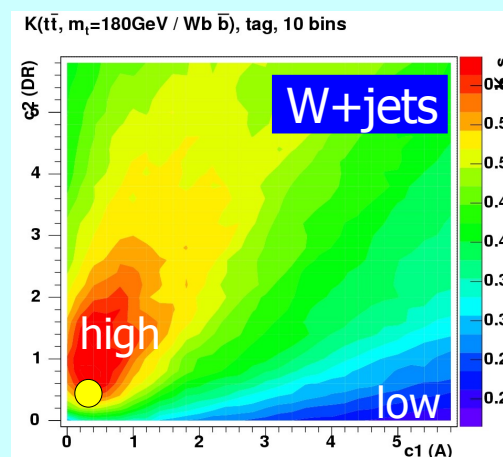
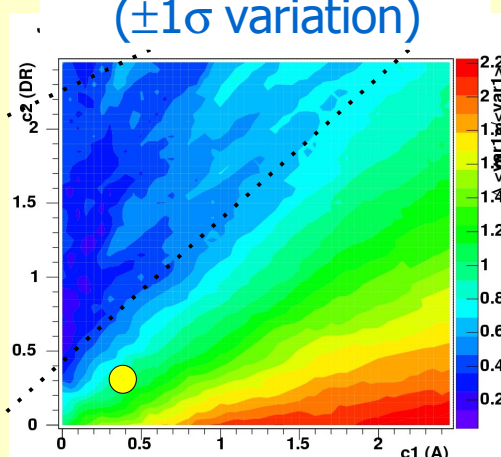
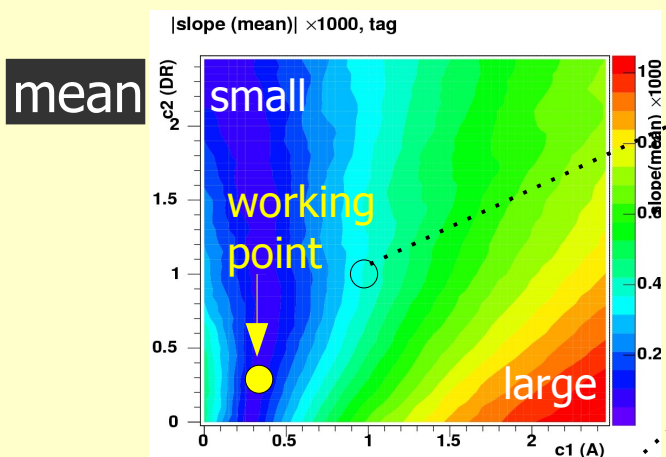


$$V = (\hat{c}_1 A + \hat{c}_2 D_R + \hat{c}_3 H_{TZ}) \times N$$

$m_t$  dependence [0.1%]

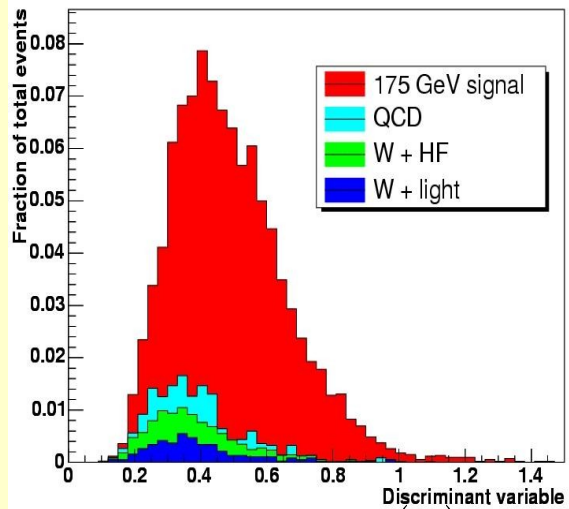
JES dependence [%]  
( $\pm 1\sigma$  variation)

S/B discrimination

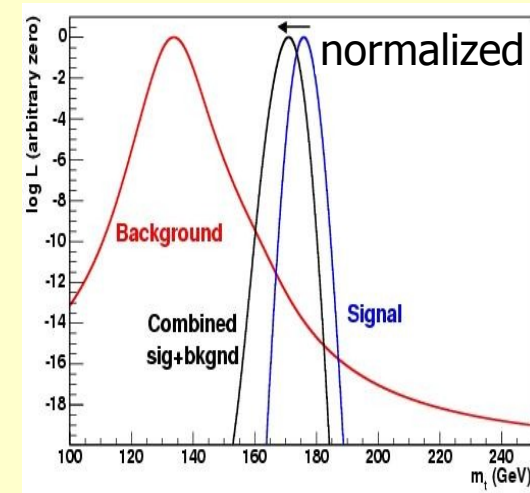


$m_t$

# Background Treatment



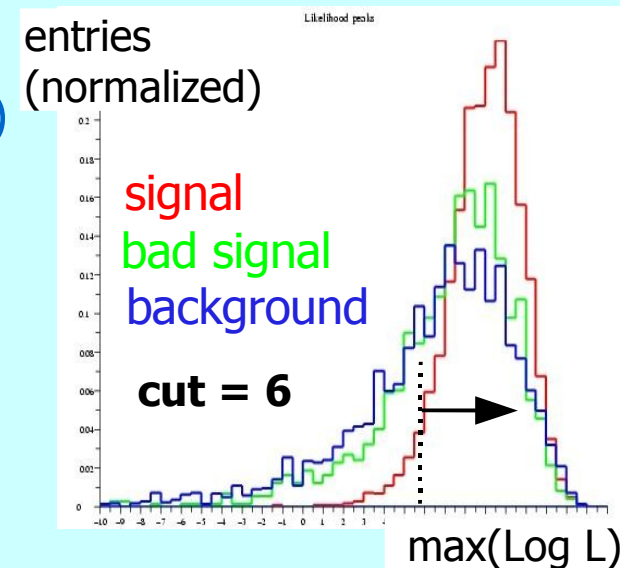
- Adding background shifts signal likelihood curve
- Subtract average log background weighted by background probability



$$f_{bg}(q) = \frac{B(q)}{B(q) + S(q)} \longrightarrow \log(L_{tot}) = \sum_i \log L_{sig,i} - f_{bg}(q_i) \langle L_{bg} \rangle$$

- Additional likelihood cut applied to clean up background and bad signal (ISR/FSR,  $W \rightarrow \tau\nu$ ...)
- Improves bias and resolution
- Number of candidates: 179  $\rightarrow$  149

Type of event	1-tag	>1-tag
Good signal	94.7%	94.1%
Bad signal	73.7%	80.2%
Background	63.1%	57.5%



Systematic source	Systematic uncertainty (GeV)
Residual JES	0.28
PDFs	0.46
ISR	$0.75 \pm 0.36$
FSR	$0.67 \pm 0.40$
MC generator	$0.44 \pm 0.43$
Gluon fraction	0.05
Background: fraction	0.20
Background: composition	0.39
Background: average shape	0.29
Background: $Q^2$	0.30
Calibration	0.14
b-JES	0.23
b-tag $E_T$ dependence	0.02
Permutation weighting	0.06
Multiple interactions	0.05
Lepton $P_T$	0.05
Total	1.39

- Total systematic:  
 $\Delta M_{\text{top}}(\text{syst.}) = 1.4 \text{ GeV}/c^2$
- Largest contribution from modeling of the initial and final state gluon radiation:  
 $\Delta M_{\text{top}}(\text{ISR+FSR}) = 1.0 \text{ GeV}/c^2$
- Statistical component:  
 $\Delta M_{\text{top}}(\text{stat.}+\text{JES})$   
 $= 2.3 \text{ GeV}/c^2$   
 $= 1.6(\text{stat.}) + 1.7(\text{JES}) \text{ GeV}/c^2$ .
- Residual JES uncertainty:  
 $\Delta M_{\text{top}}(\text{JES}_{\text{res}}) = 0.3 \text{ GeV}/c^2$ .  
 ( $\eta/p_t$  dependence of jet corrections)

# Systematics

## Lepton+Jets (ME 370 pb<sup>-1</sup>)



(status 03/07/2007)

Uncertainties [GeV/c <sup>2</sup> ]	Di-Lept (ME 1030 pb <sup>-1</sup> )	(ME 955 pb <sup>-1</sup> )	ll-Jets (TM 940 pb <sup>-1</sup> )
Statistical	3.9	1.6	2.8
<b>JES</b>	<b>3.5</b>	<b>1.5</b>	<b>2.4</b>
Residual JES		0.4	0.7
b-JES		0.6	0.4
ISR/FSR	0.4	1.1	1.2
PDF	0.8	0.1	0.5
Generator	0.9	0.2	1.0
MC statistics	0.7	0.2	0.4
Background model	0.2		0.9
Sample composition	0.7		0.1
Lepton p <sub>T</sub>	0.1	0.2	
b-tag p <sub>T</sub> dep.		0.3	
Multiple interactions	0.2	0.1	
Method	0.6		0.2
Total systematics (excluding JES)	1.7	1.4	2.1

physics model



Source of Uncertainty	b-Tagging Analysis
-----------------------	--------------------

Statistical uncertainty and jet energy scale +4.1 -4.5

**JES only 3.5**

*Physics modeling:*

Signal modeling	±0.46
Background modeling	±0.40
PDF uncertainty	+0.16 -0.39
b fragmentation	±0.56
b/c semileptonic decays	±0.05

*Detector modeling:*

JES p <sub>T</sub> dependence	±0.19
b response (h/e)	+0.63 -1.43
Trigger	+0.08 -0.13
b tagging	±0.24

*Method:*

Signal fraction	±0.15
QCD contamination	±0.29
MC calibration	±0.48

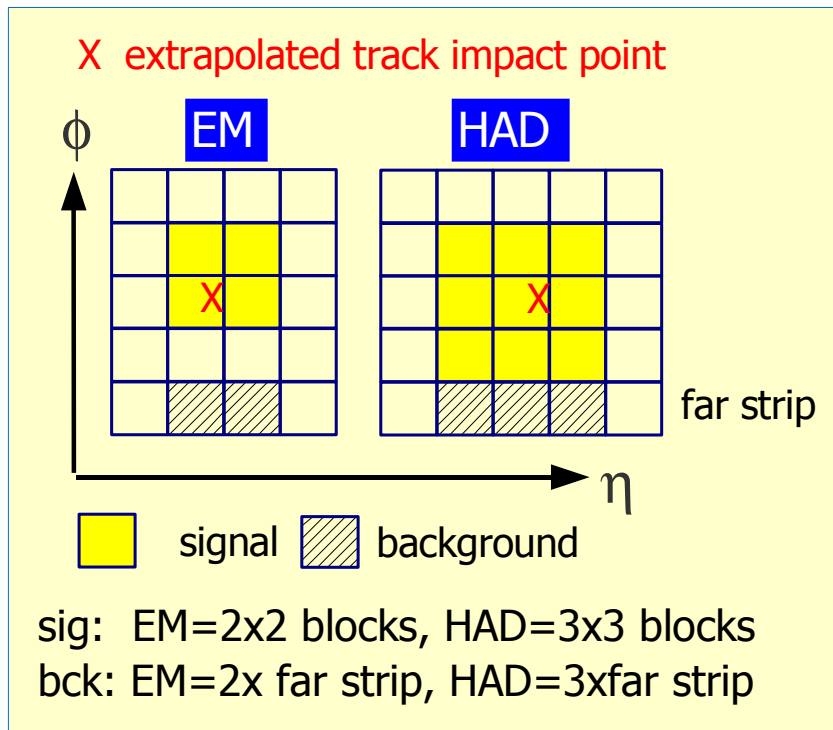
Total systematic uncertainty +1.2 -1.8

Total uncertainty +4.3 -4.9

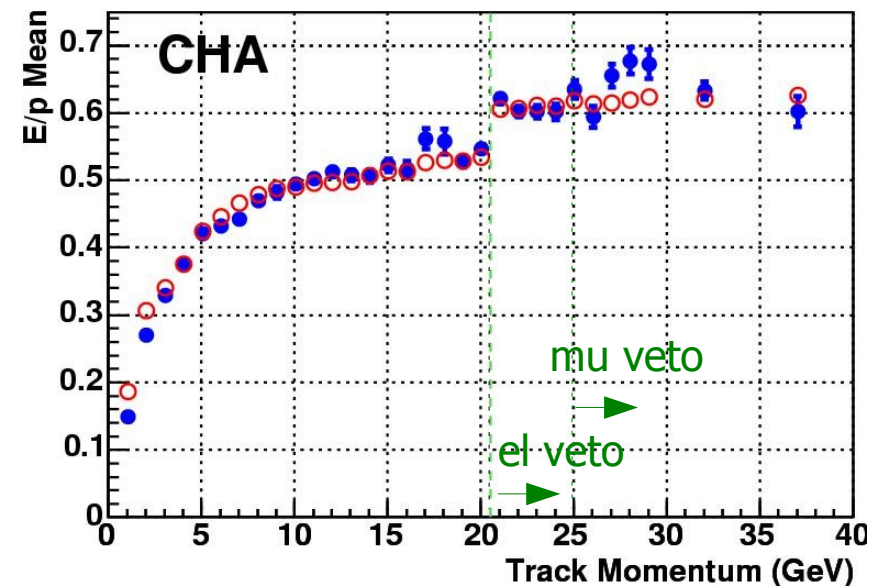
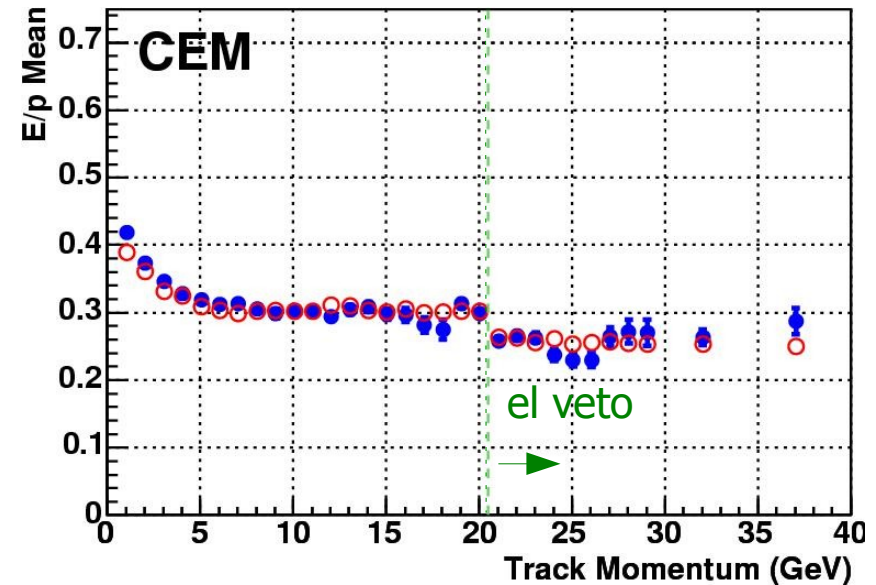
- Non-JES systematics mainly dominated by physics model:
  - amount of FSR gluon radiation, hadronization model,...

... will limit or knowledge of M<sub>top</sub> in future!

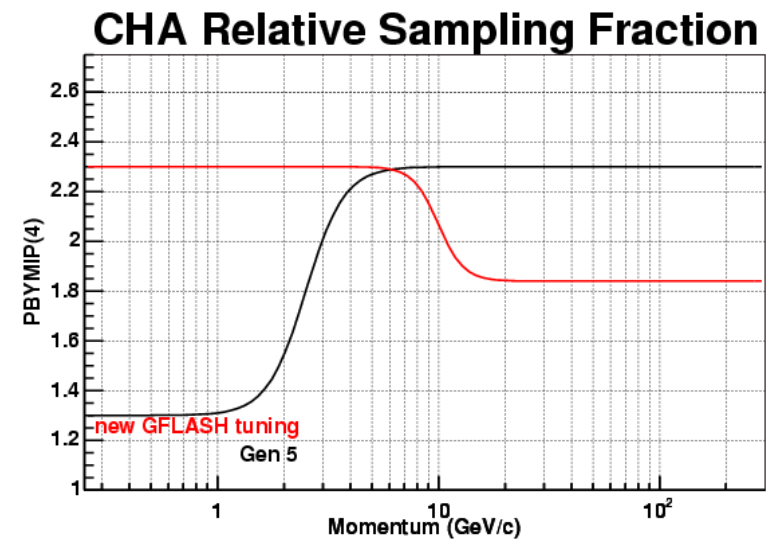
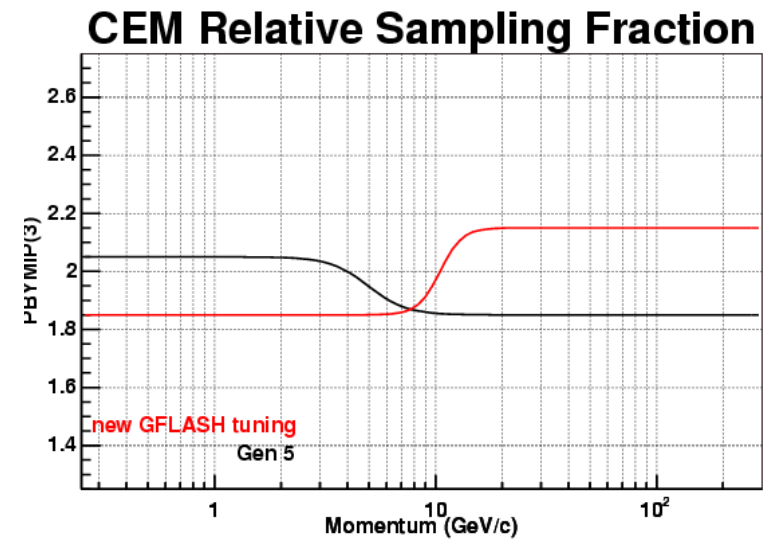
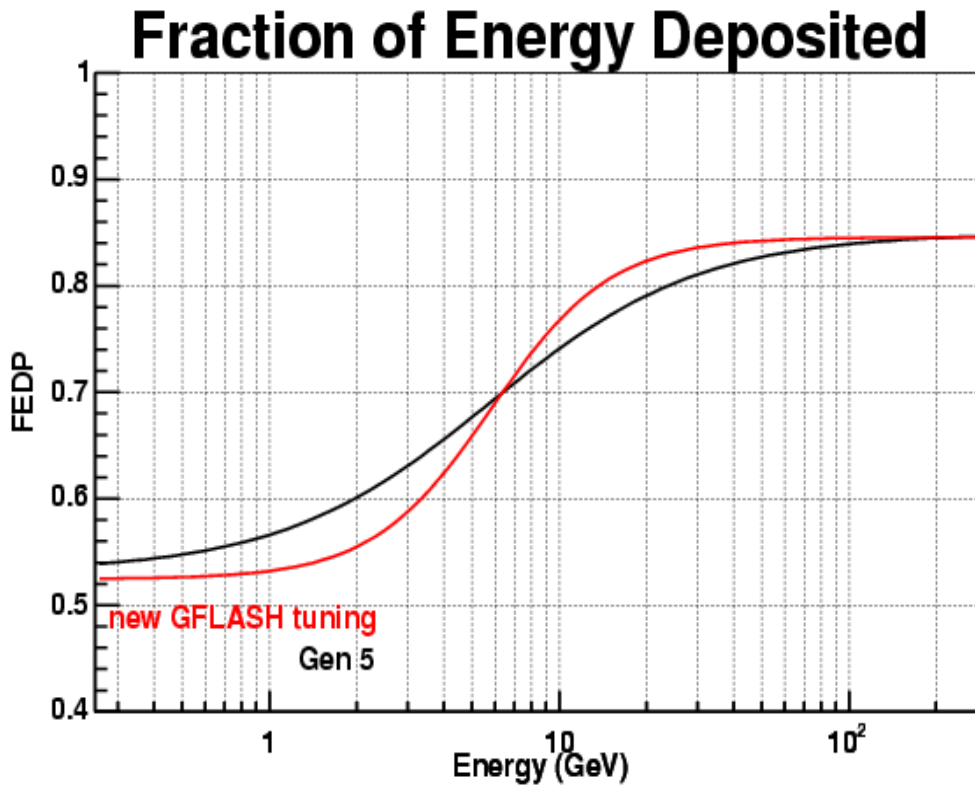
# Absolute CEM and CHA Response



- These are not primary tune observables but serve as cross checks
- Responses dependent on shower start, shapes are more complicated than TOT and MIP
- Reasonable agreement



# Parametrization (Central)

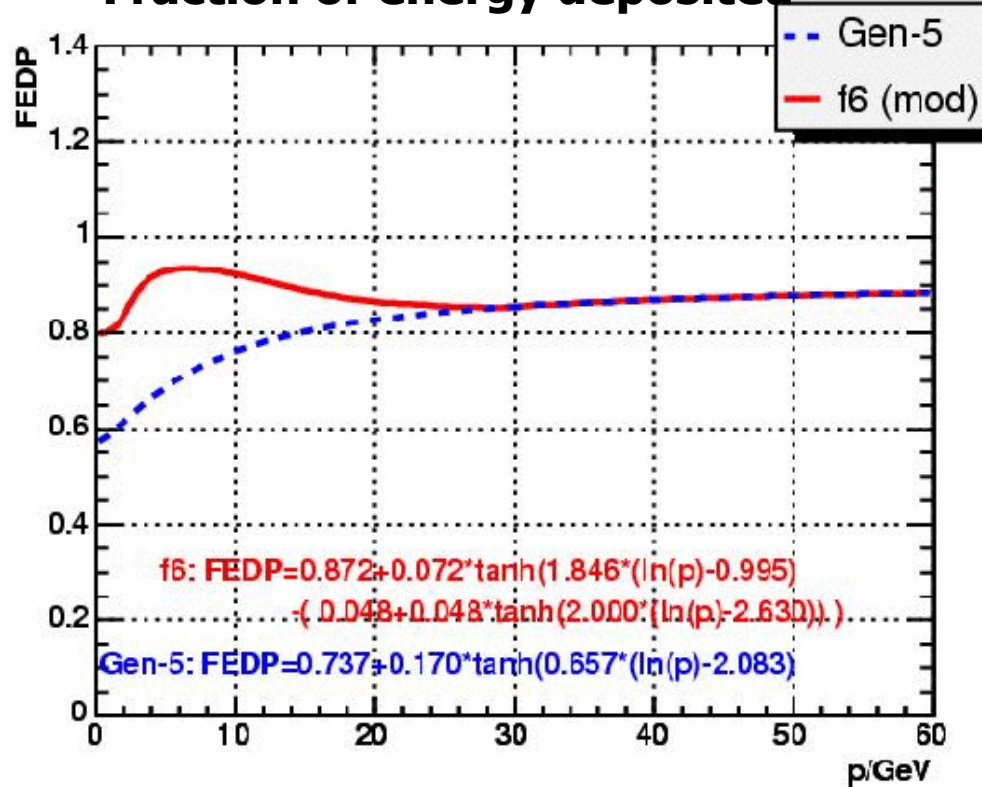


- Smooth parametrization connecting in-situ tuning and test beam tuning result.

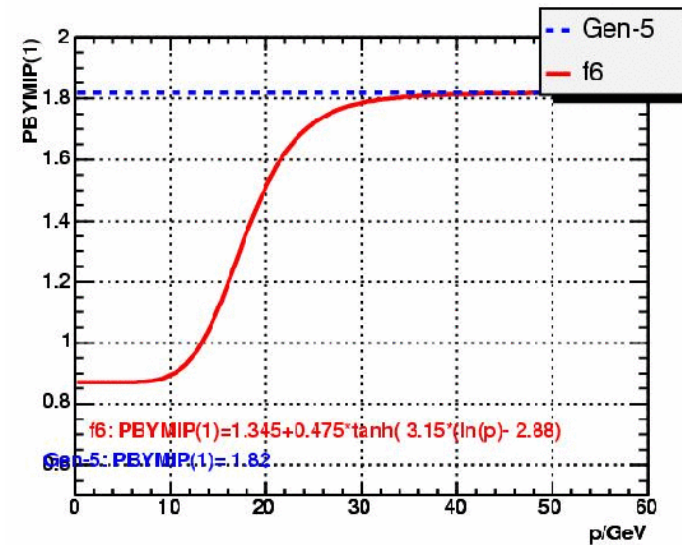


# Parametrization (Plug)

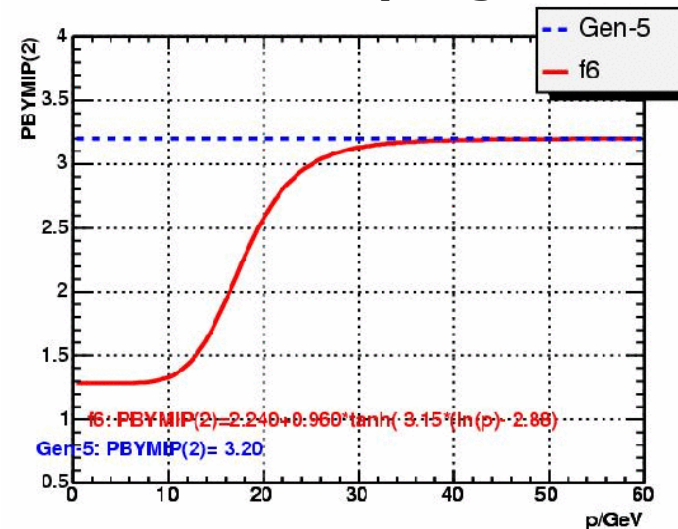
## Fraction of energy deposited



## PEM Relative Sampling fraction



## PHA Relative Sampling fraction

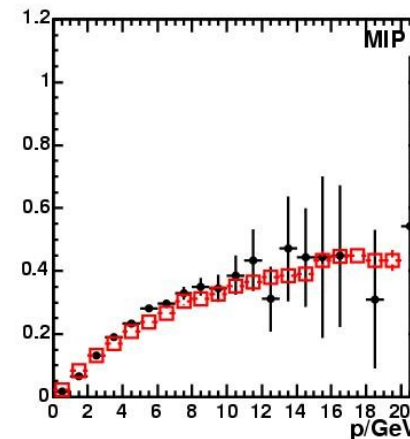
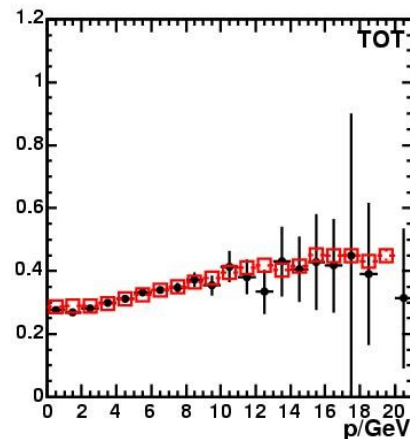
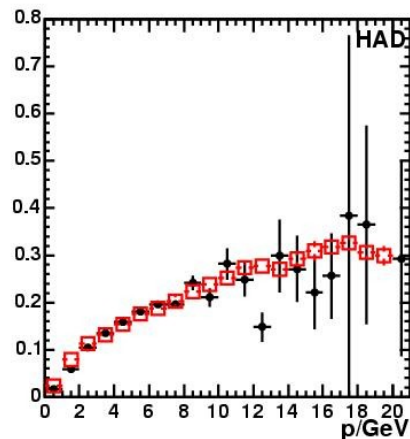
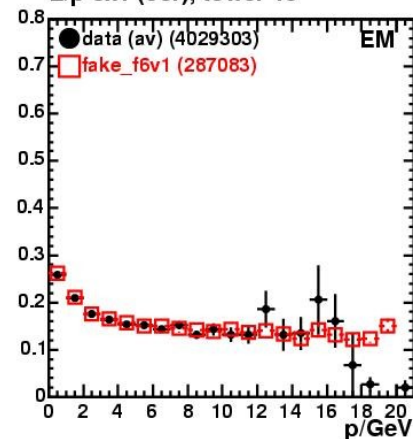


- Smooth parametrization connecting in-situ tuning and test beam tuning result.

# Absolute Response Tuning (Crack)

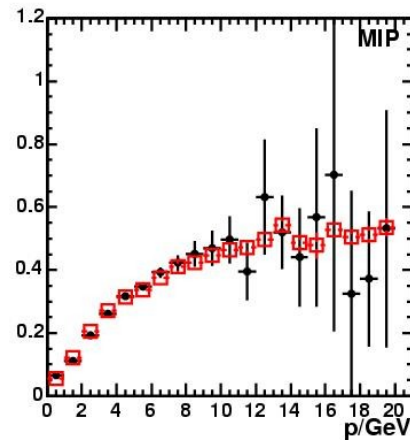
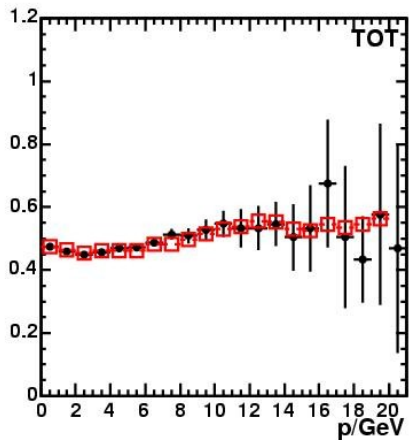
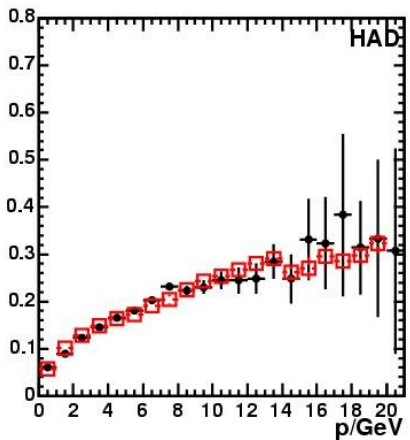
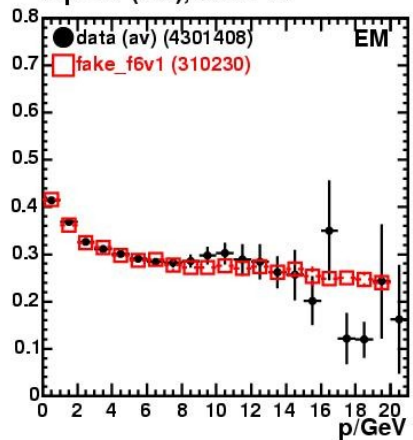
## ■ Tower 10

E/p 3x1 (cor), tower 10



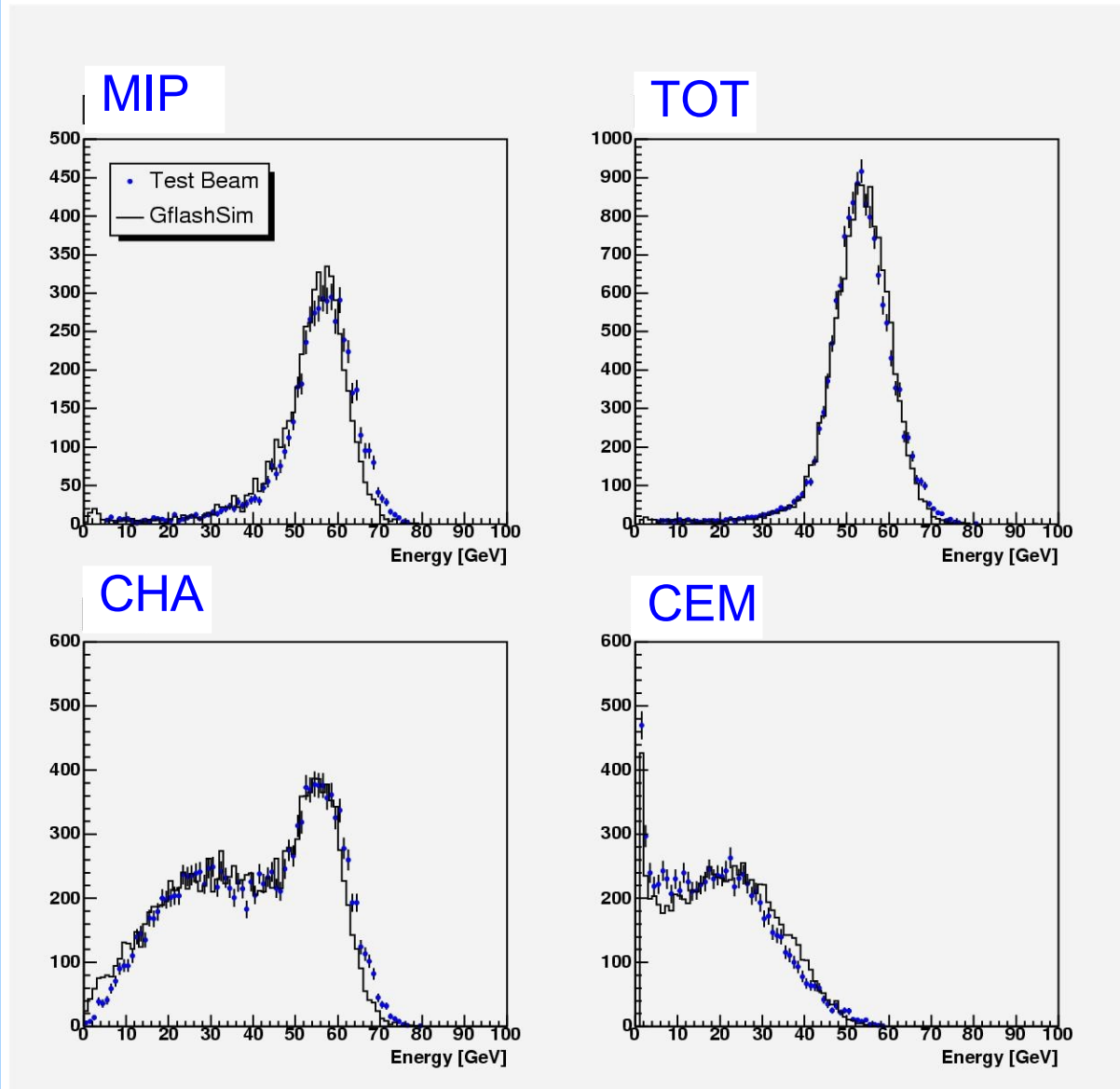
## ■ Tower 11

E/p 3x1 (cor), tower 11



sig: EM=3x1 strip, HAD=3x1 strip  
 bck: 1.5 x both side towers

# Comparison with 57 GeV Test Beam Data



## Gaussian Fits of the MIP and Total

### MIP

57 GeV testbeam  $57.2668 \pm 6.3638$   
f4 tune MC  $56.1179 \pm 5.6968$   
percent difference -2.0%

### TOT

57 GeV testbeam  $53.4797 \pm 6.2428$   
f4 tune MC  $53.6959 \pm 6.3393$   
percent difference +0.4%

- Reassure latest tuning using pure pion response from 57 GeV test beam.
- Reasonable agreement of E/p shapes between MC and data.

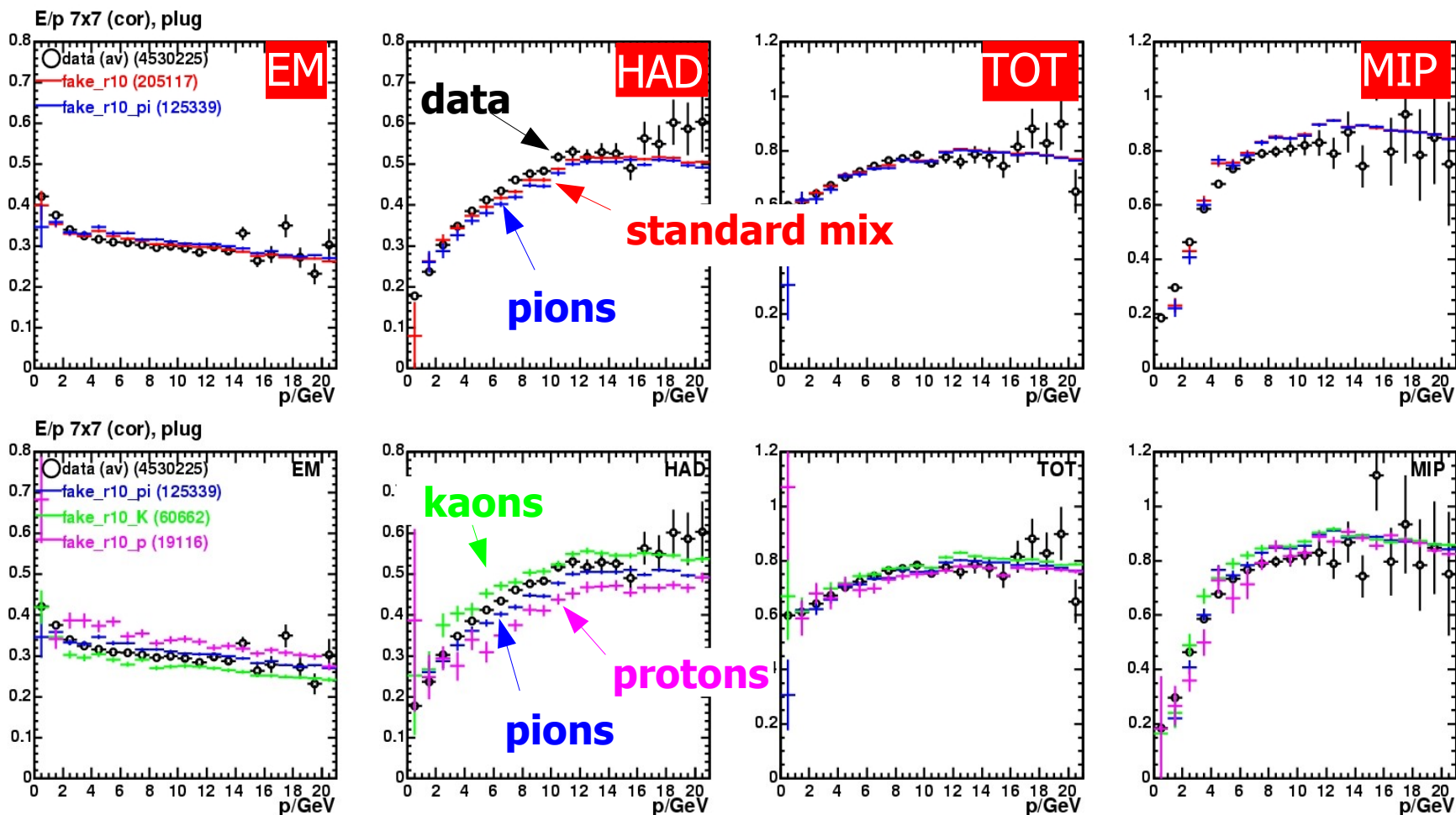
# Tuning Uncertainties



- E/p analysis
  - For TOT and MIP we consider Gaussians so we are insensitive to background contamination (e.g.: high p muons or electrons).
  - Treatment of uncorrelated background ensures that we can compare E/p from different event activity.
  - CES partially suppresses correlated background in Central.
  - Not sure about correlated background sources in the Plug (we don't use PES) – at least we are using a reasonable MC tool (Pythia) to model background.
  - Differences due to momentum spectrum has proven to be negligible.
- Lateral profile dependence
  - Profile mismatch can cause leakage effects .
  - After tuning this effect should be under control.
- Flavor dependence
  - MC mixture used at low p: minimum bias composition  
at high p: pions/kaons/protons = .6/.3/.1
  - very weak flavor dependence for primary variable TOT
  - moderate effect for MIP response (CHA, PHA sampling fractions)
  - larger effect for EM (CEM, PEM sampling fractions)
  - negligible effect for hadronic E/p profiles due to normalization

# Flavor Dependence

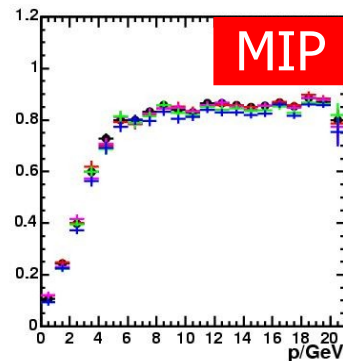
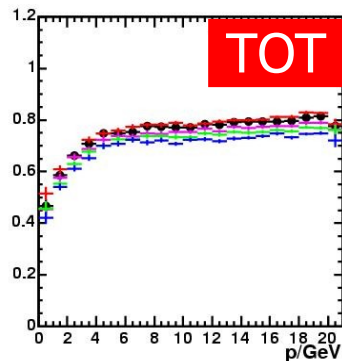
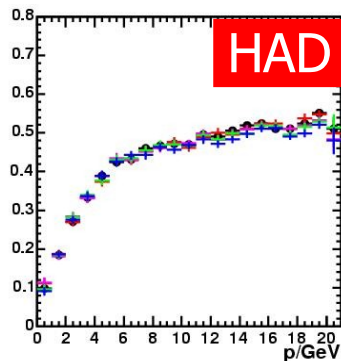
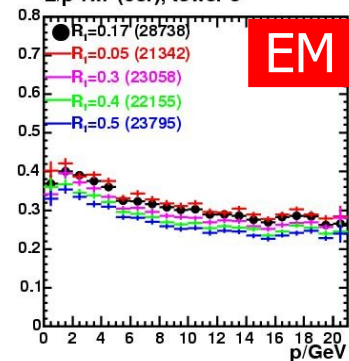
- Extreme scenario: consider individual flavors (FAKEEV flavor/anti-flavor = 50%/50%)  
NB: Minbias spectrum dominates low p.



- GFLASH treats pion/kaon/proton showers equally! Flavor dependence is pure effect of different typical shower starts given by GEANT cross sections!
- Little /moderate effect in TOT/ MIP due to almost complete coverage of shower shapes.

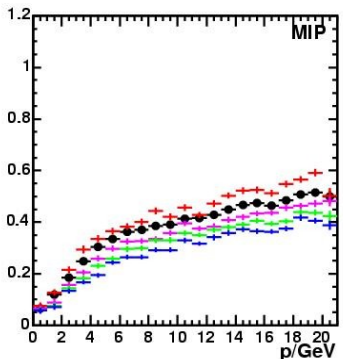
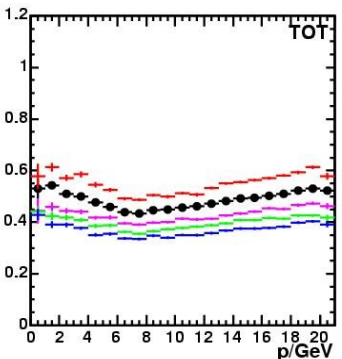
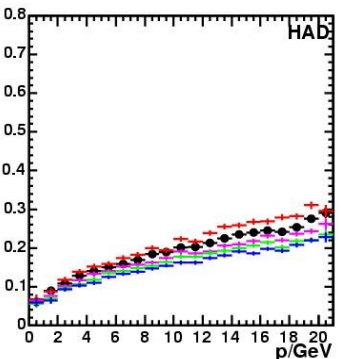
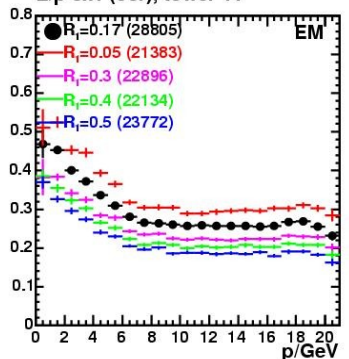
# Lateral Profile Dependence

E/p 7x7 (cor), tower 6



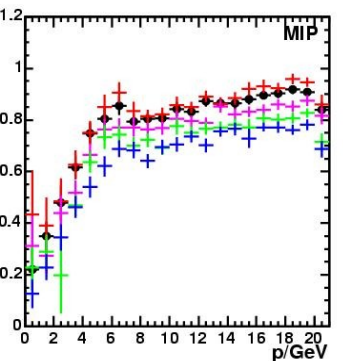
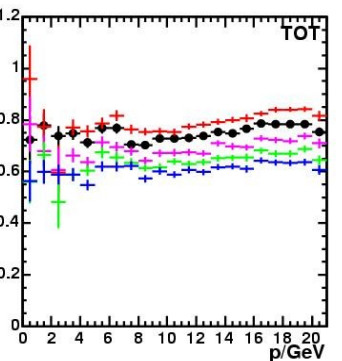
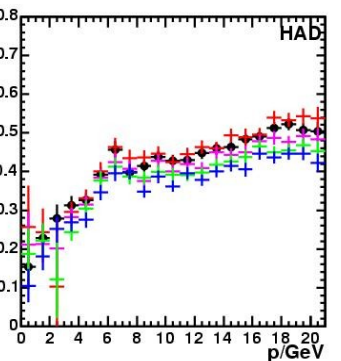
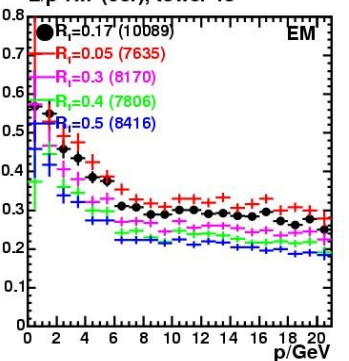
tower 6

E/p 3x1 (cor), tower 11



tower 11

E/p 7x7 (cor), tower 13

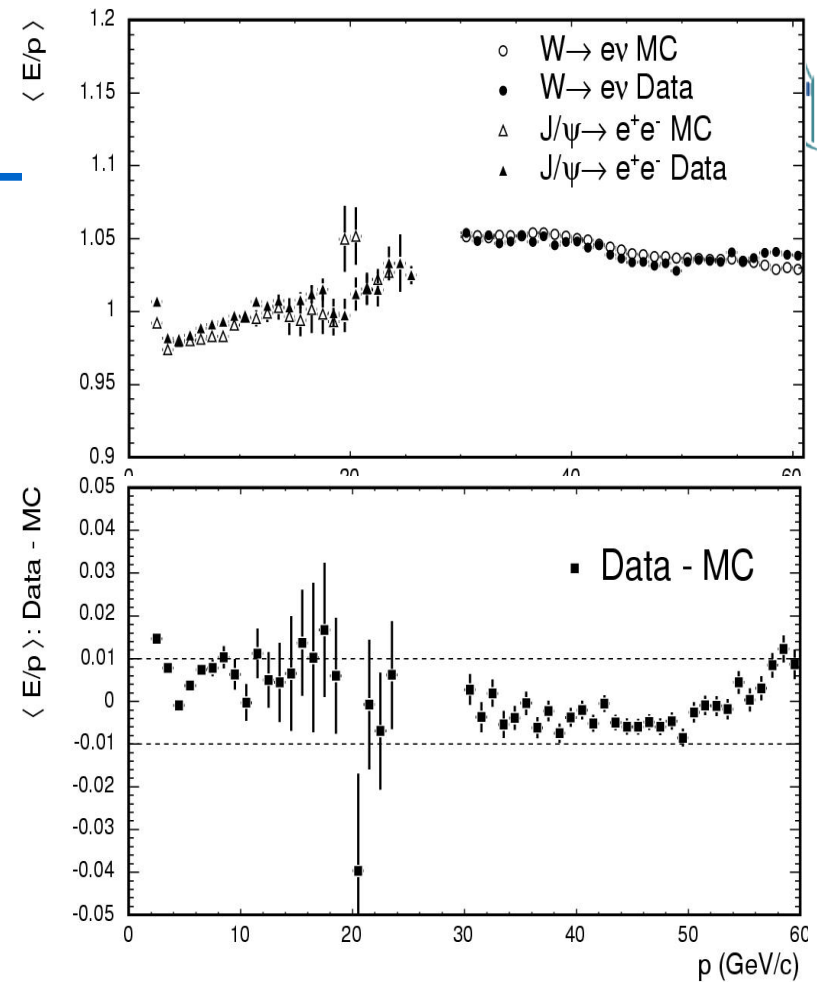
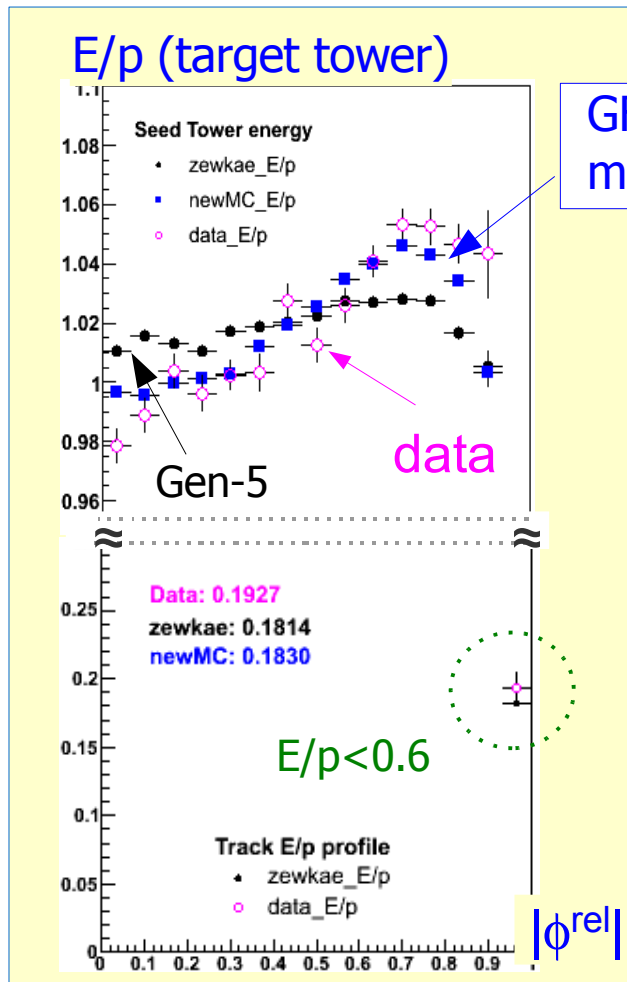


tower 13

- Effect of varying the lateral profile core parameter  $R_1$  from 0.05 to 0.50.  
 $R_1$  values used in Gen-5: 0.490 ( $p < 5\text{GeV}$ ), 0.015 ( $p > 5\text{GeV}$ )

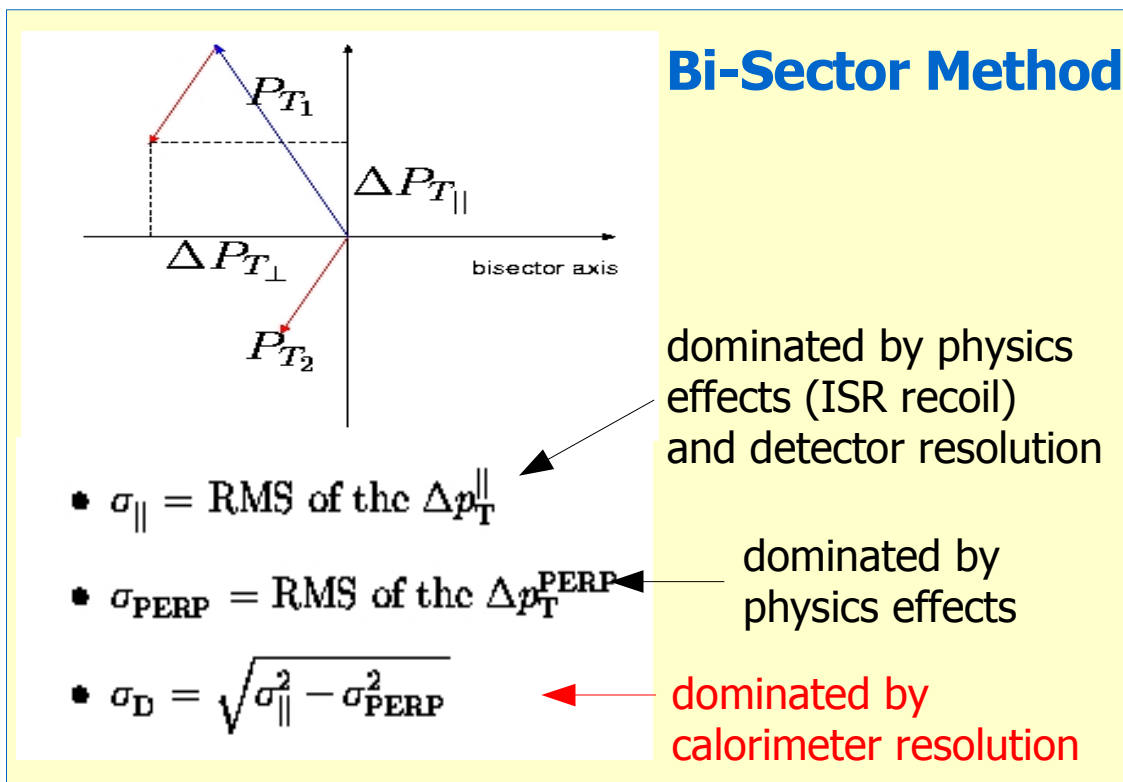
# Electron Response

- Electromagnetic scale is tuned in-situ using electrons from  $J/\psi$  (low  $p$ ) or  $W$  (high  $p$ ) decay
- MC – data discrepancy ...
  - e pointing to inner  $0.9 \times 0.9$  of target tower: 0.5%
  - e pointing to  $\phi$  cracks (WLS, steel bar): **1.6%**

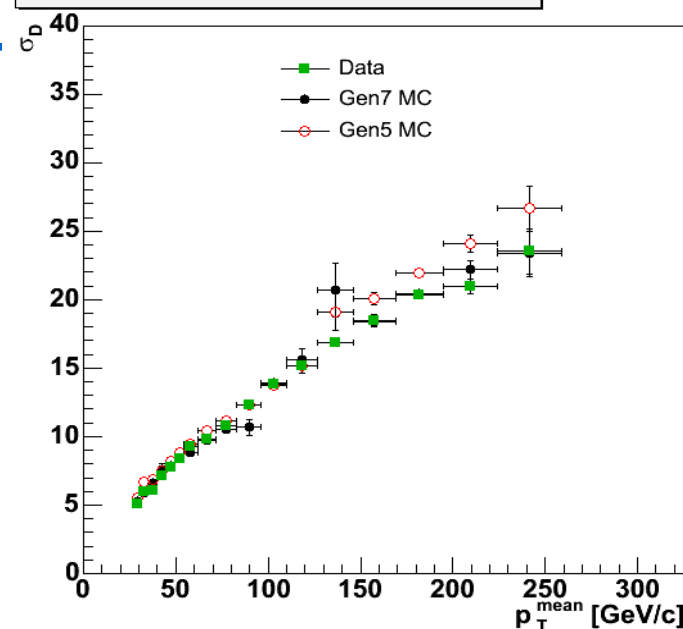


- Response along  $\phi$  is monitored using electron pairs from  $Z^0$  decays in a mass window around  $Z^0$  mass. One leg in Central target tower, the other leg probes  $\phi$  profile.
- New map correction in phi plus MC scaling by 0.5%  $\rightarrow$   $\phi$  profile has significantly improved.

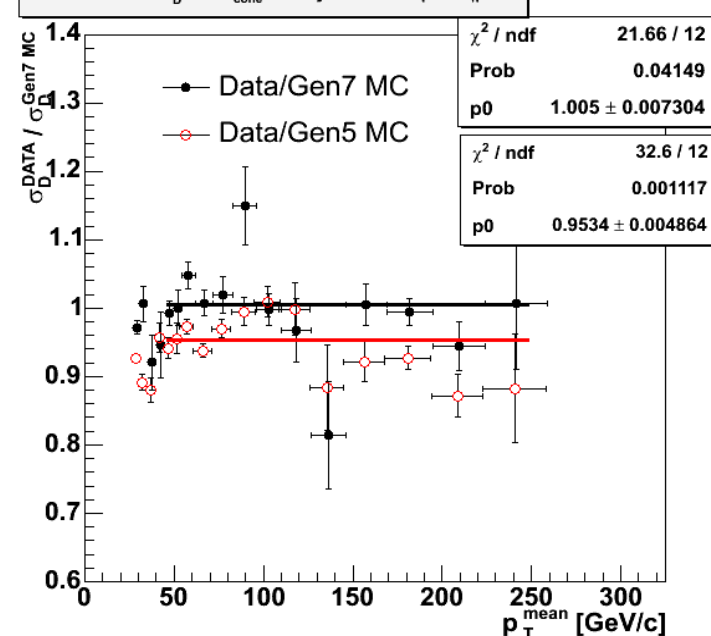
# Jet Energy Resolution



$\sigma_D$  for  $R_{\text{cone}} = 0.7$  jets in  $1.1 < |\text{Det } \eta| < 1.6$



Ratio Data/MC  $\sigma_D$  for  $R_{\text{cone}} = 0.7$  jets in  $1.1 < |\text{Det } \eta| < 1.6$



- Simulated and measured resolution agree better in certain detector regions.