



Precision Top Mass Measurement



Lina Galtieri (LBNL and FNAL)
on behalf of CDF and DØ collaborations

Motivation

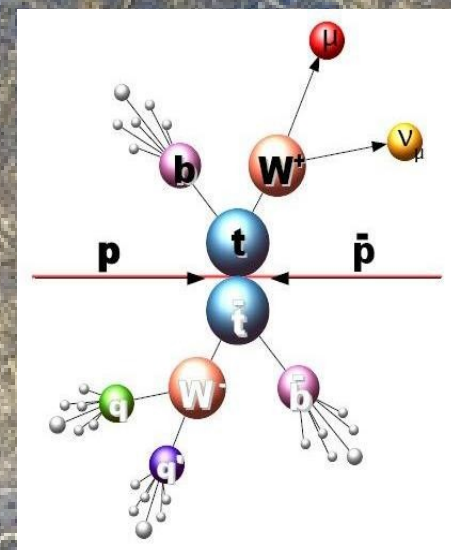
How to: Direct Measurement

Analysis Methods

Results

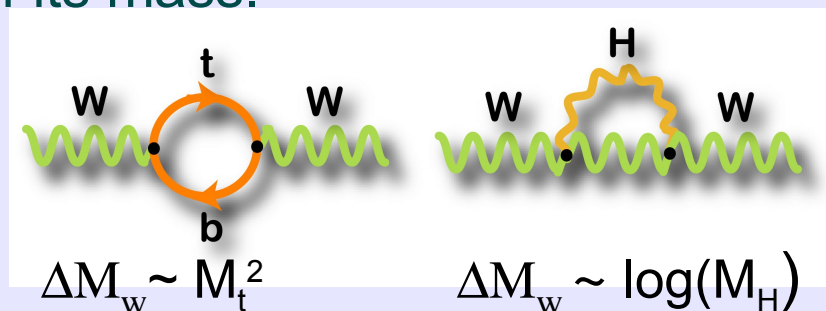
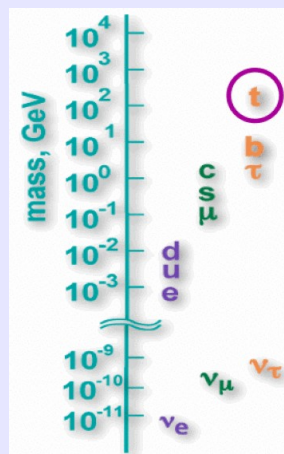
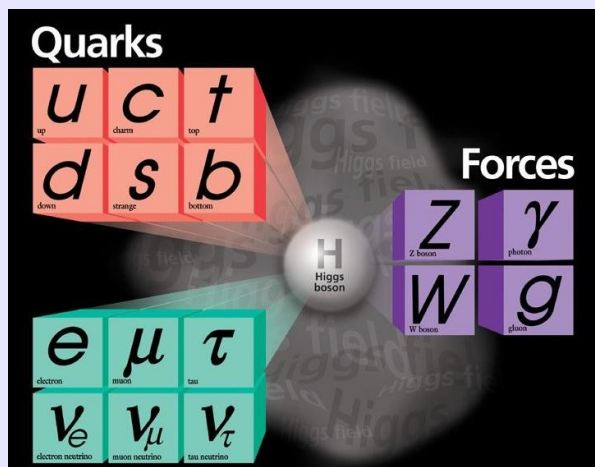
Standard Model Higgs Implication

Conclusions

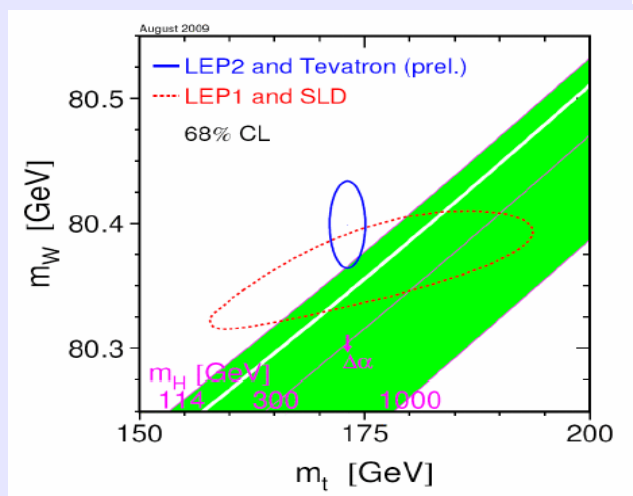


Motivation

Within the Standard Model the top quark holds a special place because it is the heaviest quark and its Yukawa coupling $g_t \sim 1$. Many models need a precise value of its mass.



- Quantum loop corrections to many EWK observables are sensitive to the top mass
- The W mass is highly correlated to M_{top} and M_H in EWK theory



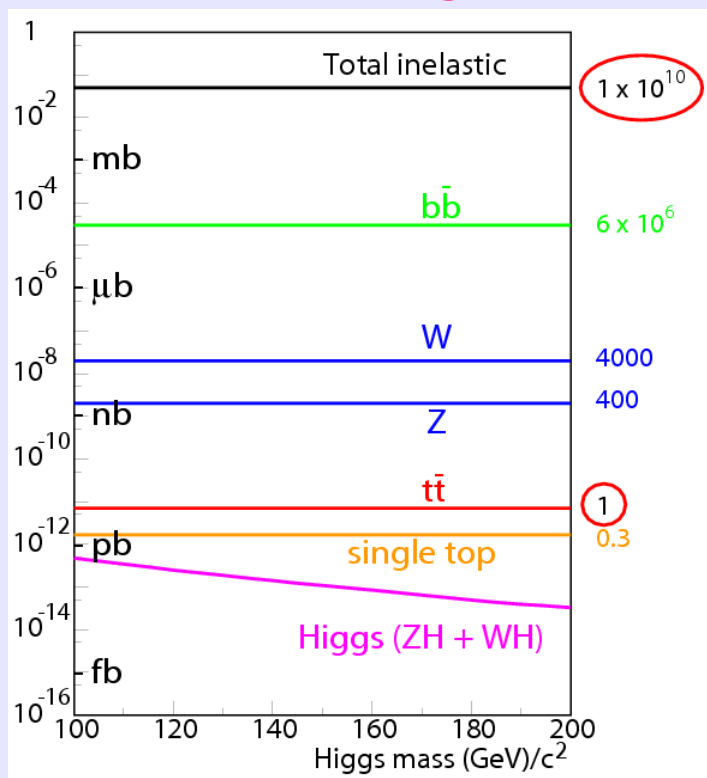
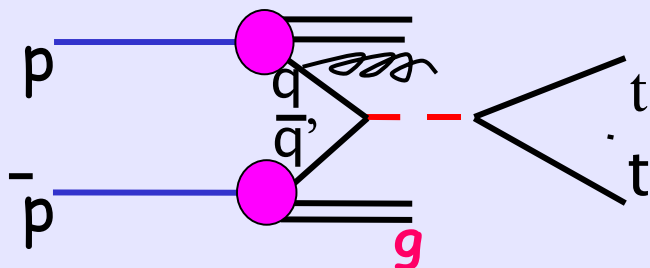
Precision measurements of the top and W mass measurements provide a better constraint to the Higgs mass than the combination of many EWK observable



Top Production and Decay



$t\bar{t}$ Production at the Tevatron:

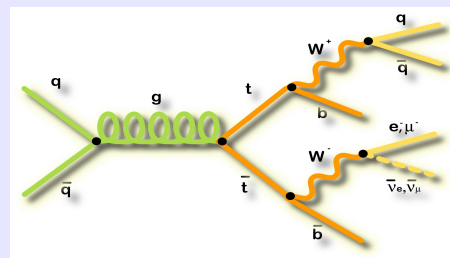


Top is heavy: decays very fast!

$$t\bar{t} \rightarrow W^+ b W^- \bar{b}$$

$$\Gamma(t \rightarrow Wb) \sim 1.5 \text{ GeV}, \tau \sim 4 \times 10^{-25} \text{ sec}$$

No hadronization: measure quark properties (mass etc.) directly



~85%



~15%

Major backgrounds:

Total inelastic $\sigma = 10^{10}$ times larger!

- QCD multijet
- W and Z +jets production,

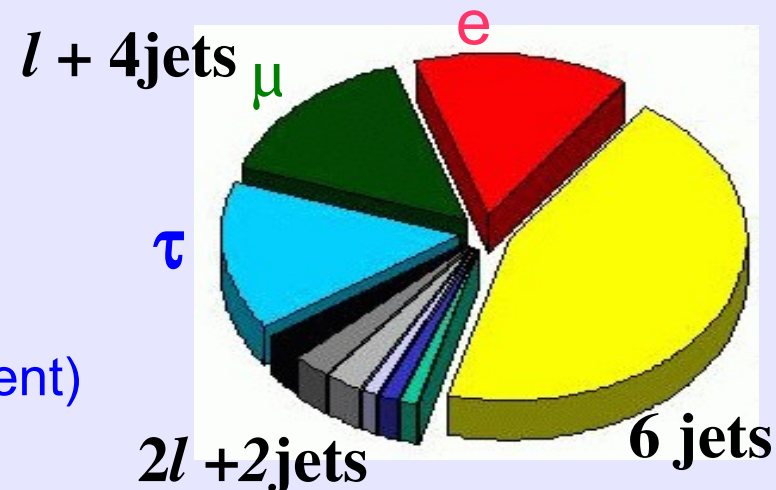


Top Quark Topologies



Reconstruct top events $t\bar{t} \rightarrow W^- b W^+ b$

- Many channels, depending on W's decays
- Experimental Challenges
 - reduce QCD, other backgrounds (b-tagging)
 - jet energy measurements systematics
 - measure jets and not partons (method dependent)

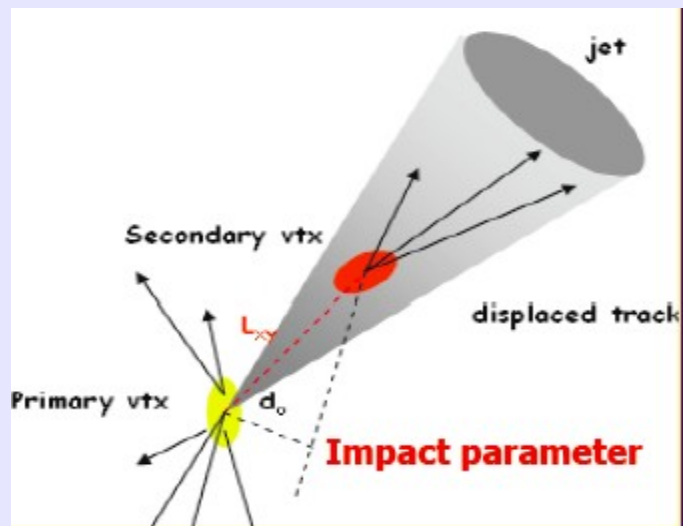


Sample	Di-lepton (e,μ)	Lepton+jets (e,μ)	All Hadronic NN selection
BR	6.4%	30%	44%
Signature	2 lept+2ν+2jets	1 Lept+1ν+4jets	6 jets
Major Back.	DY, W/Z+jets	QCD, W/Z+jets	QCD multi-jets
0-b-tags S/B	1:1	1:4	1:20
1-b-tags S/B	4:1	4:1	1:5
2-b-tags S/B	20:1	20:1	1:1
Events in 1 fb ⁻¹ (≥ 1 b-tag)	25	180	150 (2 b-tags)

τ decays not included

the MET has info about ν kinematics

Challenge(1): tagging of b-jets

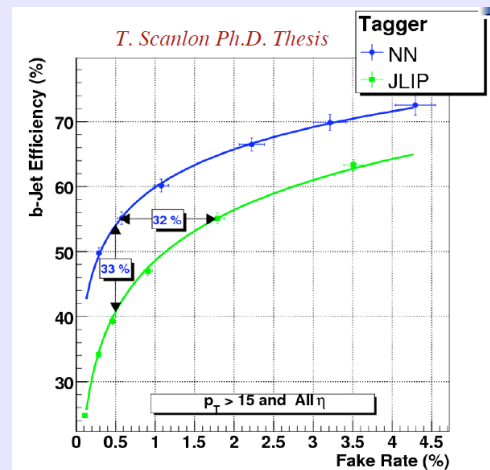


Reduction of background is obtained by identifying jets from b-quarks.

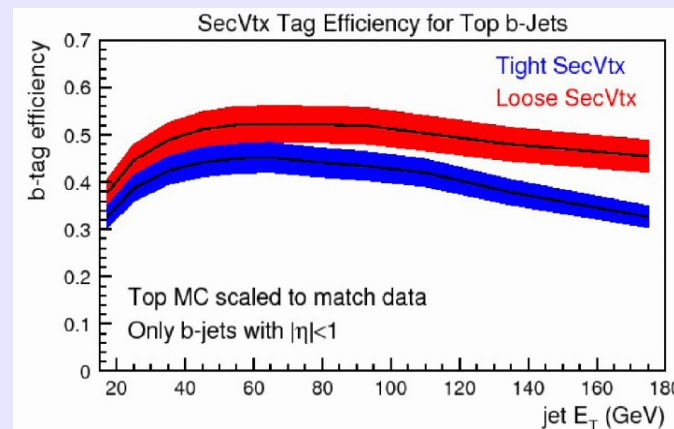
Two methods:

- secondary vertex tagging most efficient
- semileptonic decays of B hadrons in jets

Secondary vertex b-tagging



B-tag algo.
Optimized by
a NN
discriminant



Effic. per top event = $(60 \pm 3)\%$
Mistag rate = $(0.48 \pm 0.04)\%$

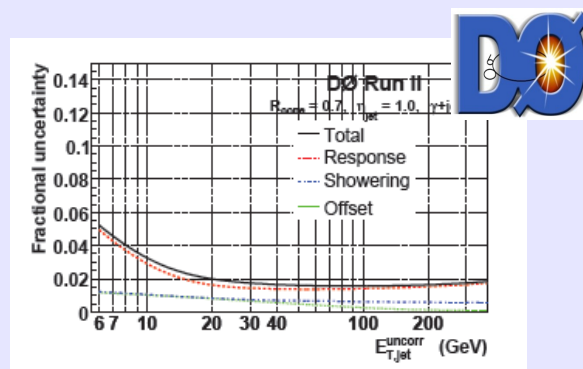
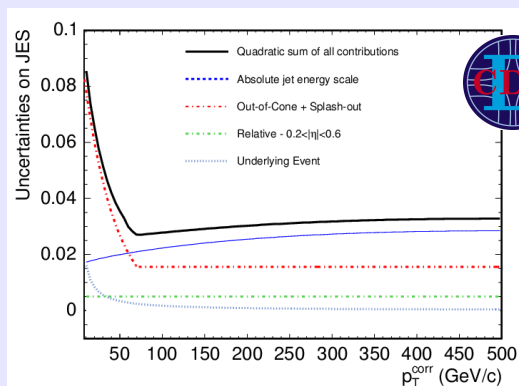


Challenge(2): Jet Reconstruction

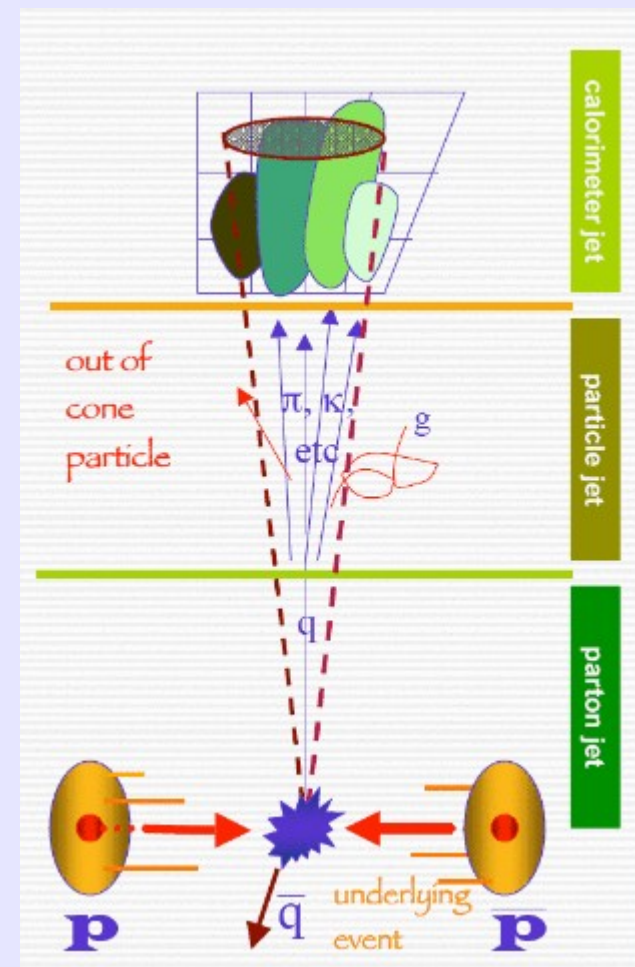


Top mass measurement needs parton information, we measure jets

- Use calorimeter information to correct the jets to the particle level .
- JES (jet energy scale) is the major source of the top mass uncertainty



- JES “in situ” calibration in $t\bar{t}$ events
 - Use $W \rightarrow jj$ constraint to measured W mass
 - A systematic is now a statistical uncertainty
 - Can be used for $l+jets$ and all had. topology



Use cone algorithm



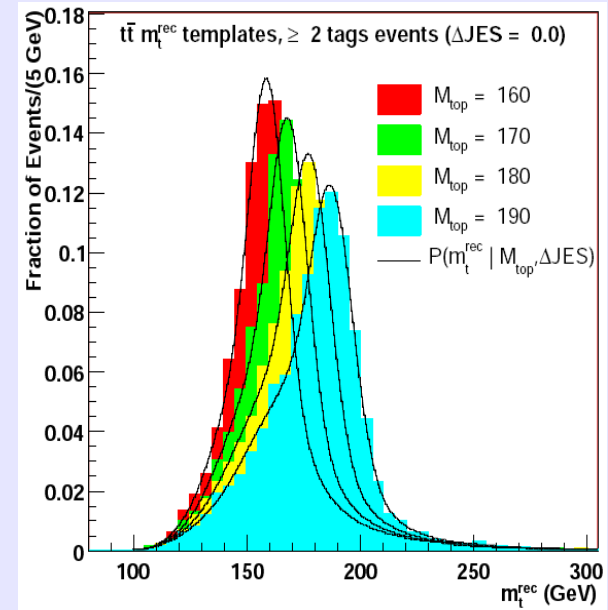
Mass Measurement Methods



Many approaches have been used.

- **Template method**

- Choose an observable x , that is sensitive to m_t
- Predict the distribution of x as a function of m_t using Monte Carlo (templates)
- For each event evaluate a likelihood for each m_t value
- Maximize the likelihood for the entire sample.



Systematics are somewhat different for different methods.

- **Matrix Element Method (ME)**

Uses all information from the event, integrating over the least known variables.

“In situ” calibration of JES is used for topologies with $W \rightarrow jj$



Top Mass Measurement: ME



- For each event evaluate a likelihood as a function of the top mass and Δ_{JES} related to the jet momenta uncertainty.
- All possible jet permutations are included with weights = w_i (24 for 1+jets)

$$L(\vec{y} \mid m_t, \Delta_{\text{JES}}) = \frac{1}{N(m_t)} \frac{1}{A(m_t, \Delta_{\text{JES}})} \sum_{i=1}^{24} w_i L_i(\vec{y} \mid m_t, \Delta_{\text{JES}})$$

measured quantities

normalization

acceptance

24 Permutations

$$L_i(\vec{y} \mid m_t, \Delta_{\text{JES}}) = \int \frac{f(z_1)f(z_2)}{FF} \text{TF}(\vec{y} \mid \vec{x}, \Delta_{\text{JES}}) |M(m_t, \vec{x})|^2 d\Phi(\vec{x})$$

Incoming partons

Transfer functions

parton level quantities

- Integrate over phase space ($d\Phi$) and Matrix Element (M) for $t\bar{t}$ production and decay. Integration is over parton level quantities (32). Make some assumptions, integrate over the least known variables. Subtract background.

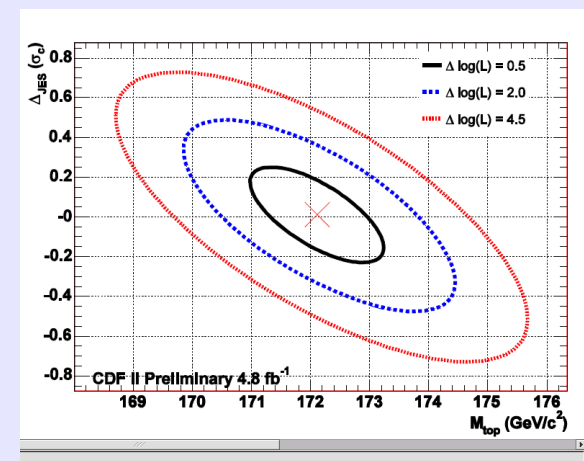
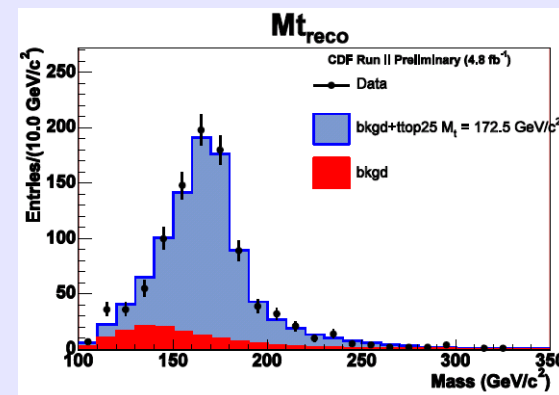


CDF Lepton+jets: Templates



NEW

- 4.8 fb⁻¹ of data are used.
- 986 events selected
 P_T lepton (e, μ) > 20 GeV, MET > 20 GeV,
4 jets with P_T > 20 GeV, 1 b-tags
Jet 4 P_T > 12 GeV for ≥ 2 b-tags
- Background estimated at 169 ± 57 events
- Uses 3D Template: M_t^{reco} , $M_t^{\text{reco}(2)}$, M_W
 M^{reco} : top mass reconstructed by constrained fit
 $M^{\text{reco}(2)}$: second best solution
- JES calibration “in situ” : constrain M_{jj} to M_W



$$M_{\text{top}} = 172.2 \pm 0.9 \text{ (stat.)} \pm 0.8 \text{ (JES)} \pm 1.0 \text{ (syst)} = 172.2 \pm 1.5 \text{ GeV}$$



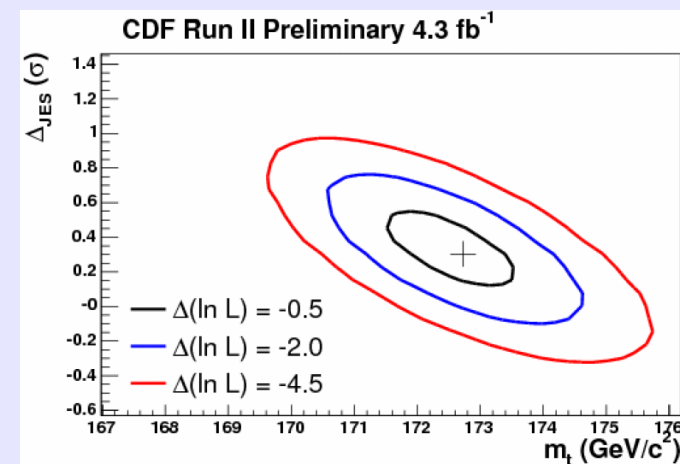
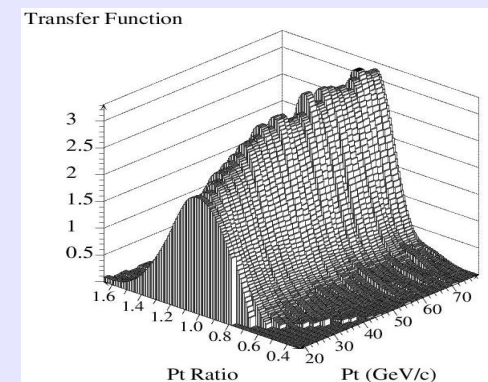
CDF: Lepton+jets, ME



- 4.3 fb⁻¹ of data are used. 738 events selected
 P_T lepton (e,m) > 20 GeV, MET > 20 GeV
4 jets with P_T > 20 GeV, ≥ 1 b-tag
Background estimated at 173 ± 50 events
- P_T transfer functions built as a function of η and jet mass for light and b-jets
- “In situ” JES calibration is performed

A Quasi-Montecarlo integration is used, that allows integration over 19 variables

- Use NN discriminant to weigh background contribution
- Major systematics are: MC generator(0.5), b-jets JES(0.4), residual JES(0.5), CR (0.4)



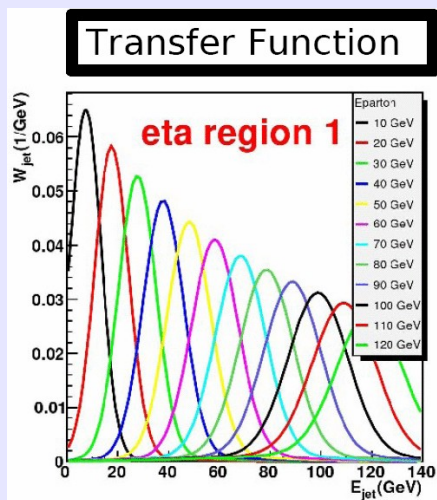
$$M_{\text{top}} = 172.6 \pm 0.9 \text{ (stat.)} \pm 0.7 \text{ (JES)} \pm 1.1 \text{ (syst)} = 172.6 \pm 1.6 \text{ GeV}$$



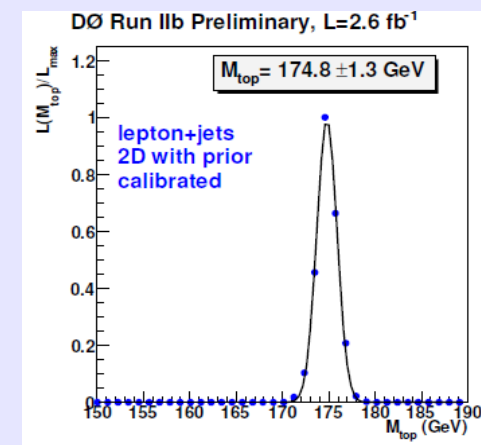
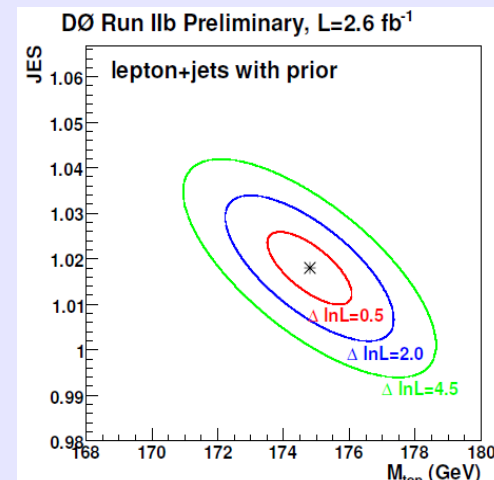
DØ lepton+jets: ME



- Uses the ME method on two separate samples
- Event selection similar to CDF. NN optimized b-tagging used to improve efficiency, reduce mistag
- Transfer functions are generated from Monte Carlo for light, heavy jets in 4 different η regions, leptons.



- Matrix Element for signal uses $qq \rightarrow t \bar{t}$ only.
- Background ME from VECBOS
- “In situ” calibration of JES using a prior



RunIIa 1.0 fb^{-1}

$M_{top} = 171.5 \pm 1.4 \text{ (stat.)} \pm 1.8 \text{ (syst) GeV}$

RunIIb 2.6 fb^{-1}

$M_{top} = 174.8 \pm 1.0 \text{ (stat.)} \pm 1.6 \text{ (syst) GeV}$

Combined

$M_{top} = 173.8 \pm 0.8 \text{ (stat.)} \pm 1.6 \text{ (syst)} = 173.8 \pm 1.8 \text{ GeV}$



DØ top-antitop Mass Difference



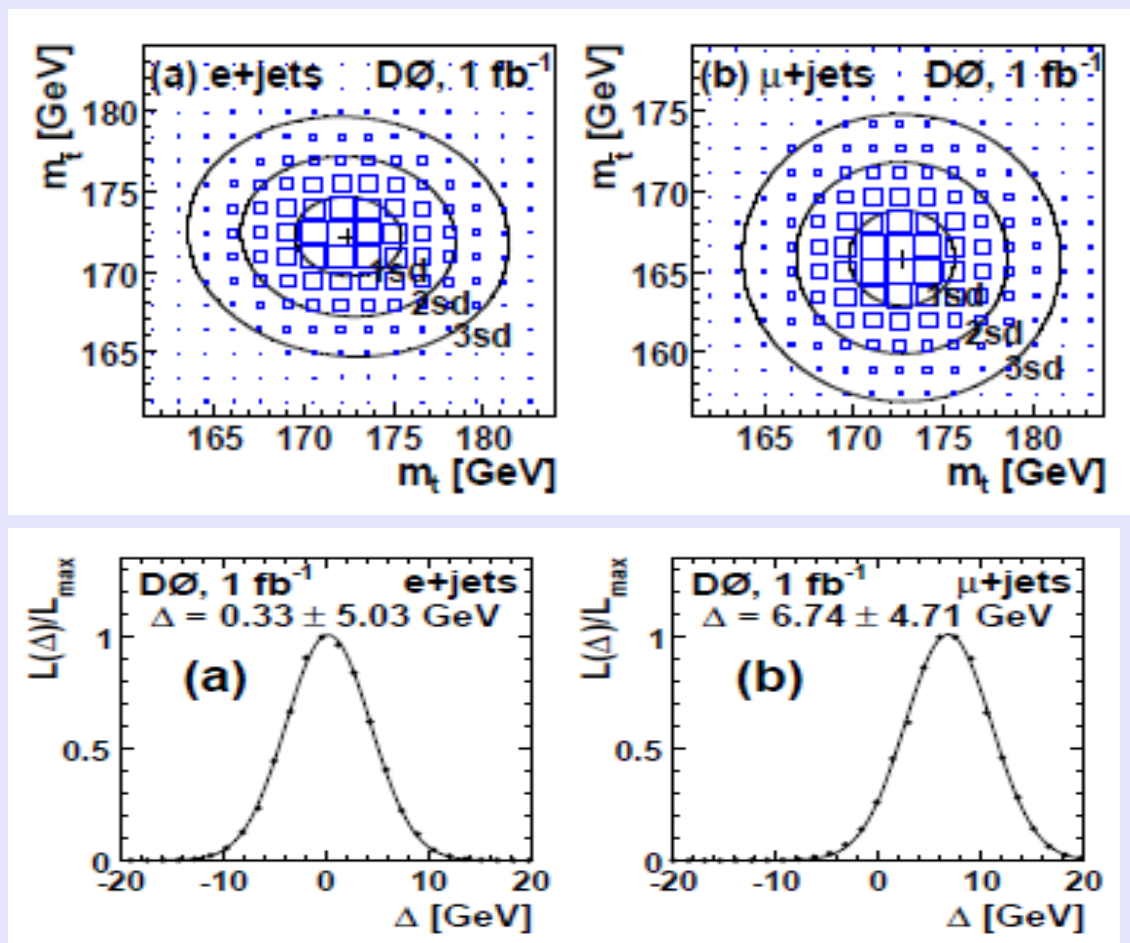
Test of CPT invariance: particle and antiparticles have the same mass

Test never done on a quark.
Top quark is unique because it decays before hadronizing

- Use ME analysis
- Samples with m_t and $m_{t\text{bar}}$ set to different values
- Likelihood as a function of Δm_t
- Analyse e and μ samples separately

Combined Result:

$$\Delta m_t = 3.8 \pm 3.4(\text{stat}) \pm 1.2(\text{syst}) = 3.8 \pm 3.7 \text{ GeV}$$





DØ di-leptons +jets



Event selection

2 leptons: ee, eμ, μμ, etrk, μtrk
large MET, 2 jets

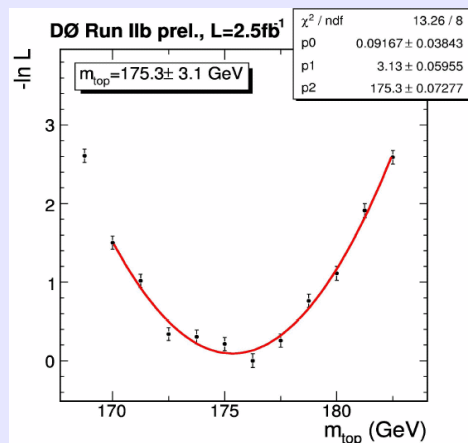
Background: Z+jets, WW, W+jets

ME: eμ only

run2a 1.1fb⁻¹,
run2b 2.5 fb⁻¹

- transfer functions
- integration
- final likelihood

$$M_{\text{top}} = 174.8 \pm 3.3(\text{stat}) \pm 2.6(\text{syst}) \text{ GeV}$$



Combined average

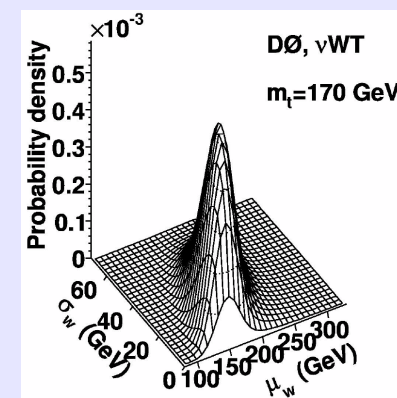
$$M_{\text{top}} = 174.7 \pm 2.9(\text{stat.}) \pm 2.4(\text{syst.}) = 174.7 \pm 3.8 \text{ GeV}$$

Template method: run2a (1 fb⁻¹)

data: ee, μμ, e-track, μ-track

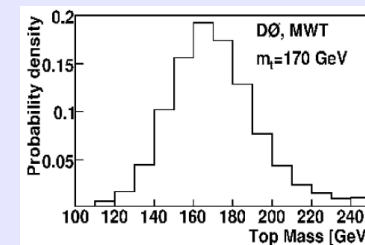
Neutrino weighting:

- sample η of ν's
- compare MET_{reco} to MET_{obs}: get weight w
- 2D templates: weight-vs-Δσ(w)



Matrix weighting

use measured MET
construct 1D weight



Combine results

$$M_{\text{top}} = 174.7 \pm 4.4(\text{stat}) \pm 2.0(\text{syst}) \text{ GeV}$$



CDF di-leptons



NEW 4.8 fb⁻¹ Template Method

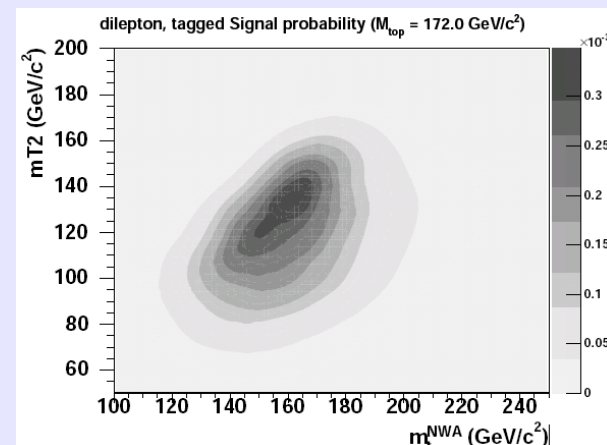
2D templates: NWA-vs-mT2

NWA: m_t from neutrino weighting algorithm

m_{T2} : m_t transverse mass from assumptions on
 m_t and the 2ν P_T values

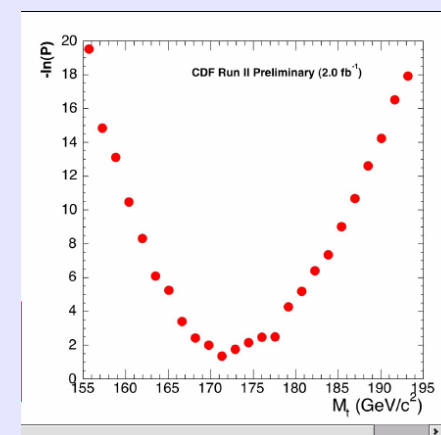
Lester, Summers, PLB, 463, 99(99); Barr, Stephens G29, 2343(03)

$$M_{\text{top}} = 170.6 \pm 2.2 \text{ (stat.)} \pm 3.1 \text{ (syst)} = 170.6 \pm 3.8 \text{ GeV}$$



1.9 fb⁻¹ Matrix Element Integration

- integrate over the 2 unknown ν
- improve event selection with a NN optimized on mass resolution
- obtain 20% improvements despite lower S/B
- overall result with 1.9 fb⁻¹ similar to TMT above



$$M_{\text{top}} = 171.2 \pm 2.7 \text{ (stat.)} \pm 2.9 \text{ (syst)} = 171.2 \pm 4.0 \text{ GeV}$$



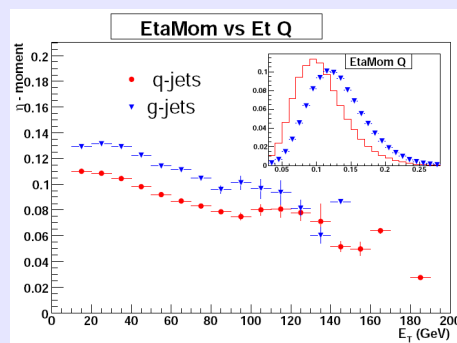
CDF: ALL HADRONIC Channel



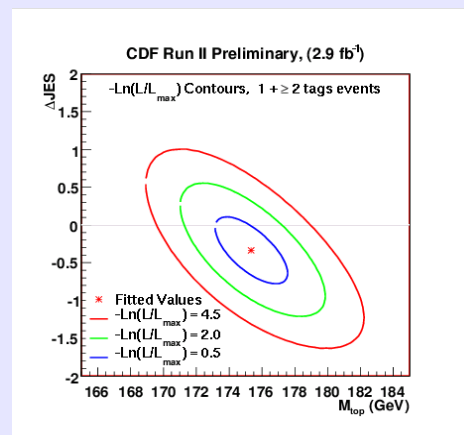
Template method (2.9 fb⁻¹)

- Event selection:
 - 6-8 jets $P_T > 15$ GeV
 - ≥ 1 b-tagged jet
 - no leptons, small MET
- Background suppression
 - S/B $\sim 10^{-3}$ after trigger
 - use NN (13 variables)
 - S/B = 1:4 (1 b-tag), 1:1 (2 b-tags)
- Analysis Strategy
 - use jet shapes: distinguish quark from gluon
 - “in situ” JES calibration
- Major Systematics
 - jet uncertainties = 1.7 GeV

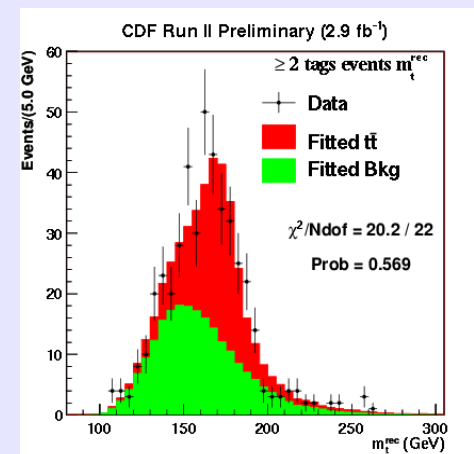
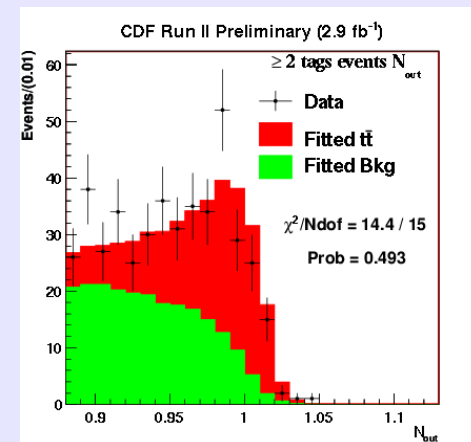
jet shapes



2-D likelihood, ≥ 1 b-tags



≥ 2 b-tags required
441 events



$$M_{\text{top}} = 174.8 \pm 1.7(\text{stat.}) \pm 1.6(\text{JES}) \pm_{1.0}^{1.2}(\text{syst}) \text{ GeV} = 174.8 \pm 2.7 \text{ GeV}$$



Top Mass Summary



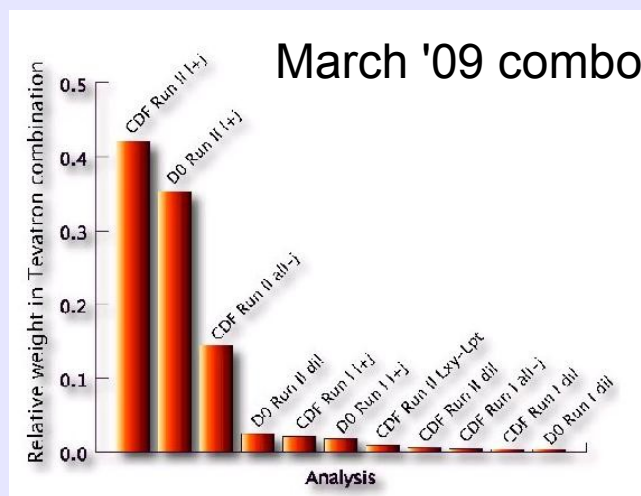
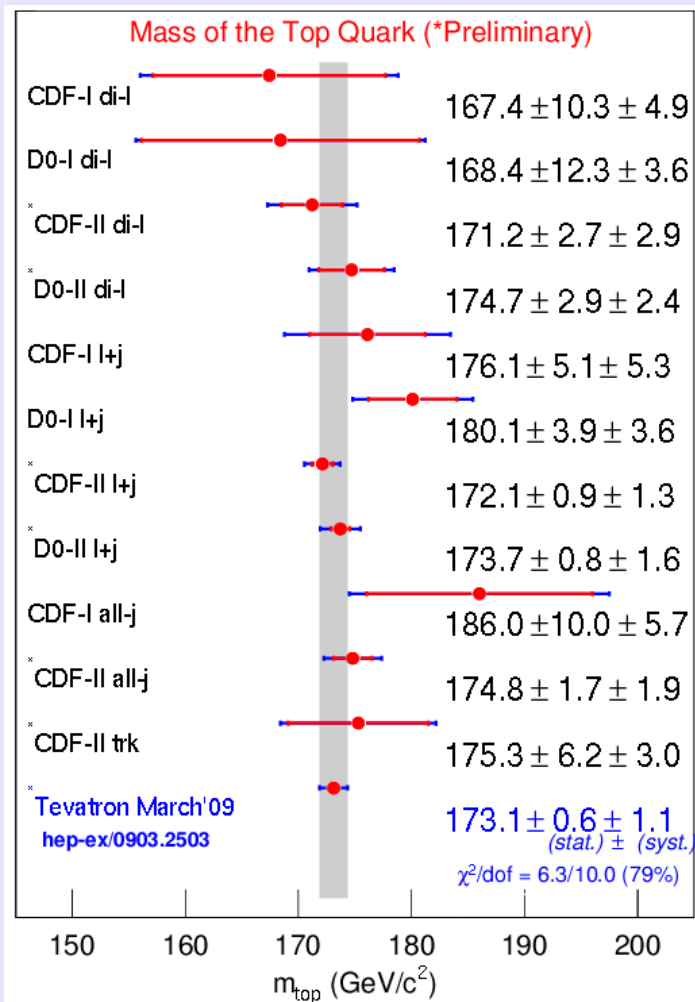
New measurements at this Conference

CDF I+jets Templates

$$M_{\text{top}} = 172.2 \pm 0.9(\text{stat.}) \pm 1.3(\text{syst.}) = 172.2 \pm 1.5 \text{ GeV}$$

CDF dilepton Templates

$$M_{\text{top}} = 171.2 \pm 2.2(\text{stat.}) \pm 3.1(\text{syst.}) = 171.2 \pm 3.8 \text{ GeV}$$



$$M_t = 173.1 \pm 1.3 \text{ GeV}$$

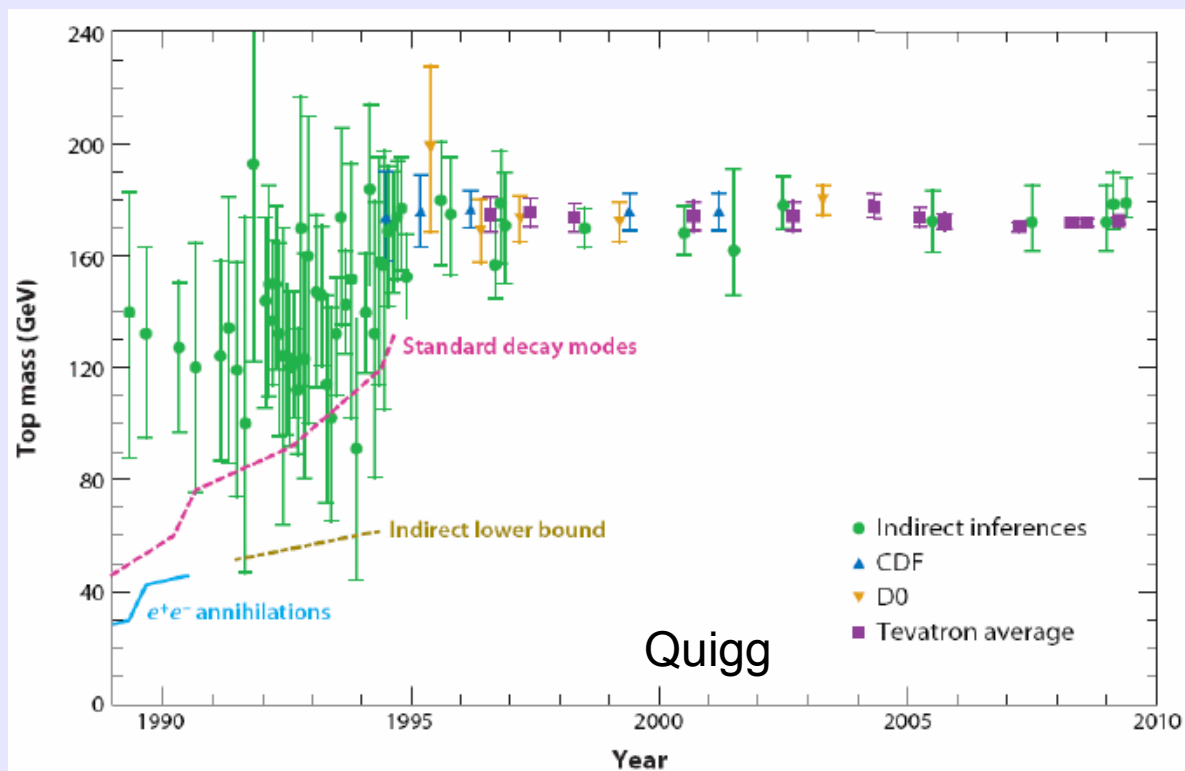


History of the top mass



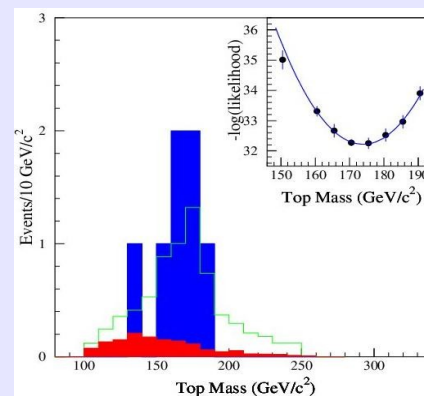
Measurement uncertainty on M_T has improved since 1994, but mass value has not changed much

$$M_{\text{top}} = 173.1 \pm 1.3 \text{ GeV}$$



First measurement

7 events (1.4 background)
CDF, PRD **50**, 2966 (1994)



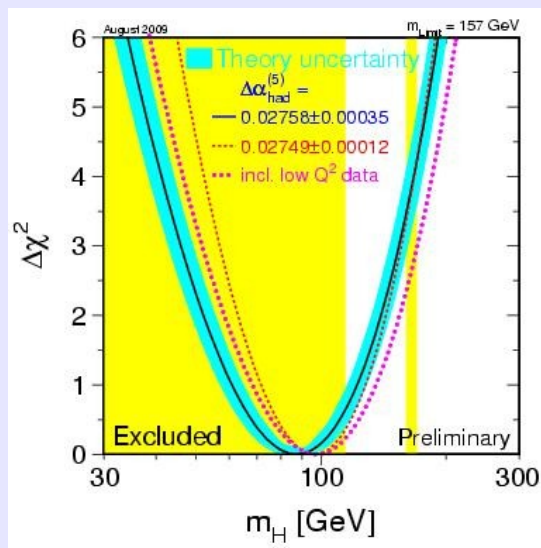
$$M_{\text{top}} = 174 \pm 10^{+13}_{-12} \text{ GeV}$$



Higgs Mass Constraint



Winter Conferences 2009 EWK Fit, gives $M_H < 186 \text{ GeV}/c^2$



Winter 2009 best Fit

$$M_H = 87^{+35}_{-26} \text{ GeV}/c^2$$

and

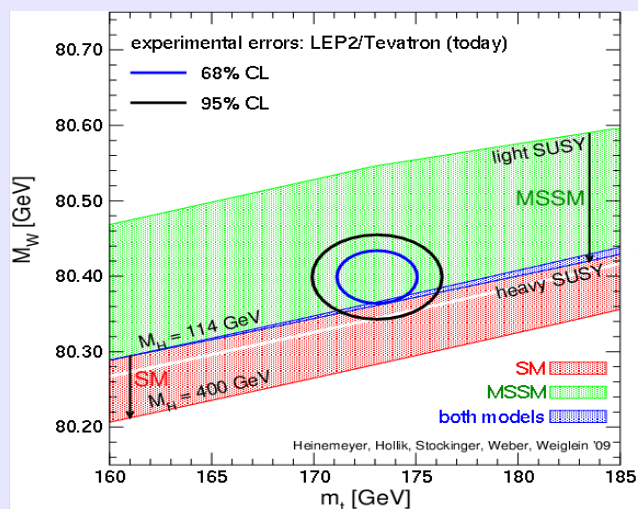
$$M_H < 157 \text{ GeV}/c^2 \text{ at 95\% CL}$$

Direct limit:

$$M_H > 114 \text{ GeV at 95\% CL}$$

Adding the direct limit

$$M_H < 186 \text{ GeV}/c^2 \text{ at 95\% CL}$$





Conclusions

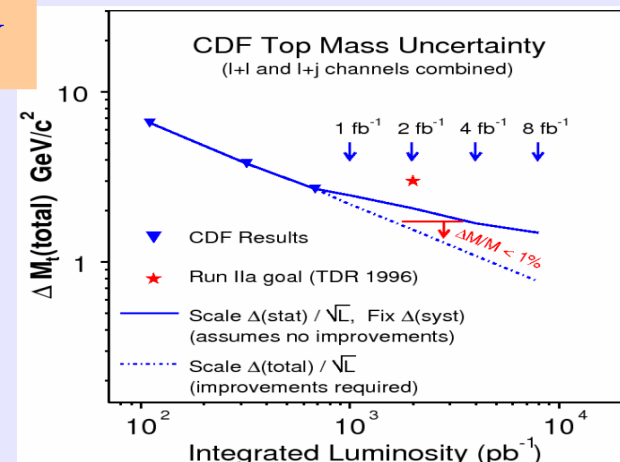


$$M_{\text{top}} = 173.1 \pm 0.6(\text{stat}) \pm 1.1(\text{syst}) = 173.1 \pm 1.3 \text{ GeV}$$

- CDF and DØ have performed many measurements of the top mass, bringing its precision down to 0.75%
- DØ has measured the top-antitop mass difference, consistent with CPT invariance

$$\Delta m_t = 3.8 \pm 3.7 \text{ GeV}$$

- At this point systematic uncertainties dominate over the statistical ones
- Additional data can help reduce some of the systematic uncertainties (JES). Major terms:
 - generator (0.5 GeV)
 - Jet Energy uncertainty (1.0 GeV)
 - b-jets Energy scale (0.4 GeV)



Example systematic uncertainties

Systematic source (Lepton+jets, ME)	Systematic uncertainty (GeV/c^2)
MC generator	0.5
Background	0.5
Residual JES	0.5
b-jet JES	0.4
Colour reconnection	0.4
ISR and FSR	0.3
Lepton P_T uncertainty	0.2
PDFs	0.2
Method calibration	0.2
Multiple hadron interactions	0.1
Total	1.1



BACKUP SLIDES



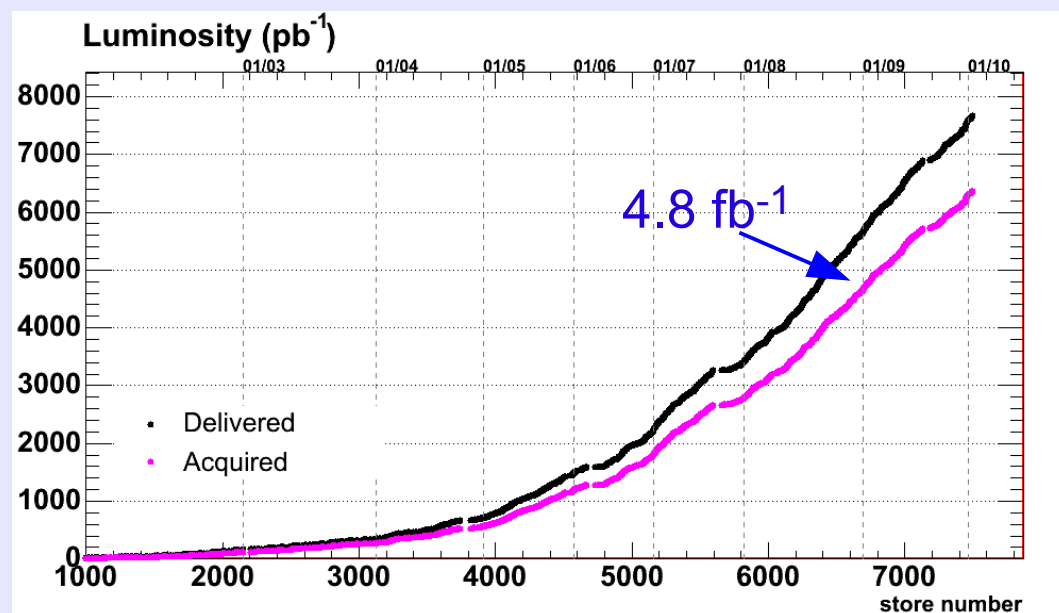
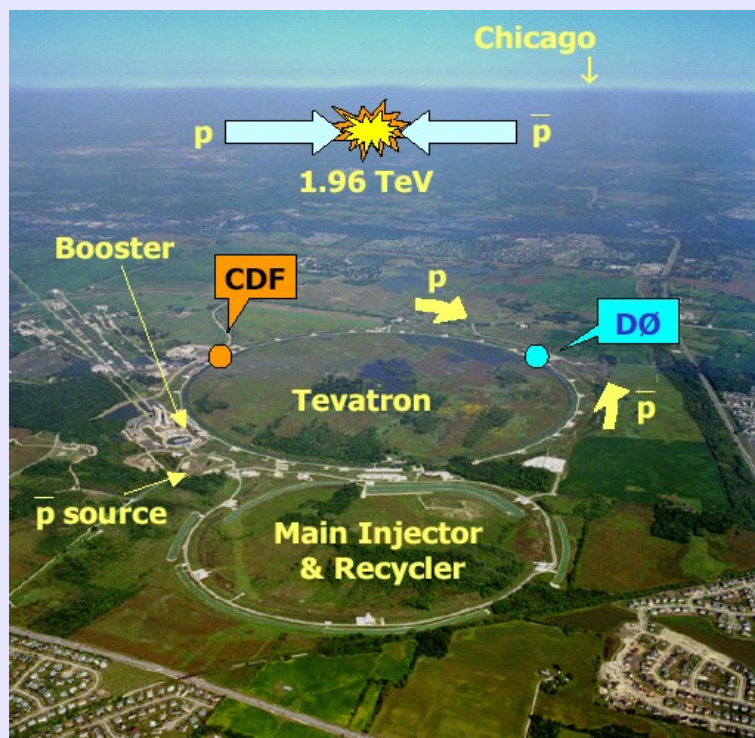
MORE INFO



The Tevatron



Direct measurements are the most precise and can only be done at hadron colliders, at present. The Tevatron now, LHC in the future



Pbar-p at 1.96 TeV since 2001
Record luminosity: $3.6 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
January 20, 2009

Expected to run through 2011:
integrated luminosity up to 12 fb^{-1}

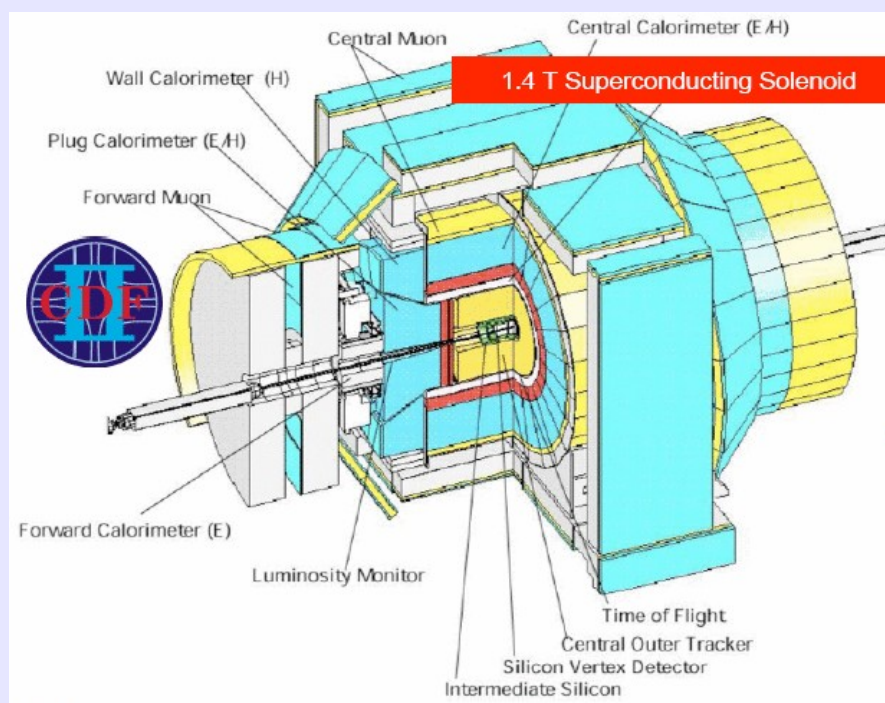
Results on top studies use up to 4.8 fb^{-1}



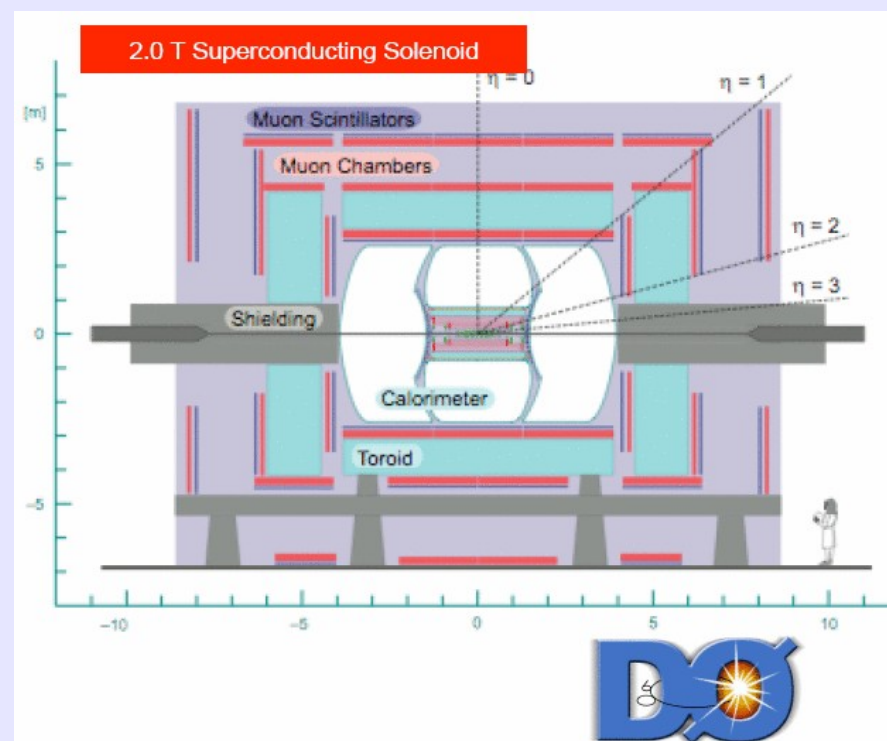
Detectors for $t \rightarrow W+b$ studies



Precision top mass measurement requires:
Accurate tracking system with Silicon Detectors
Good calorimetry to measure jet momenta.
Efficient b-tagging capabilities



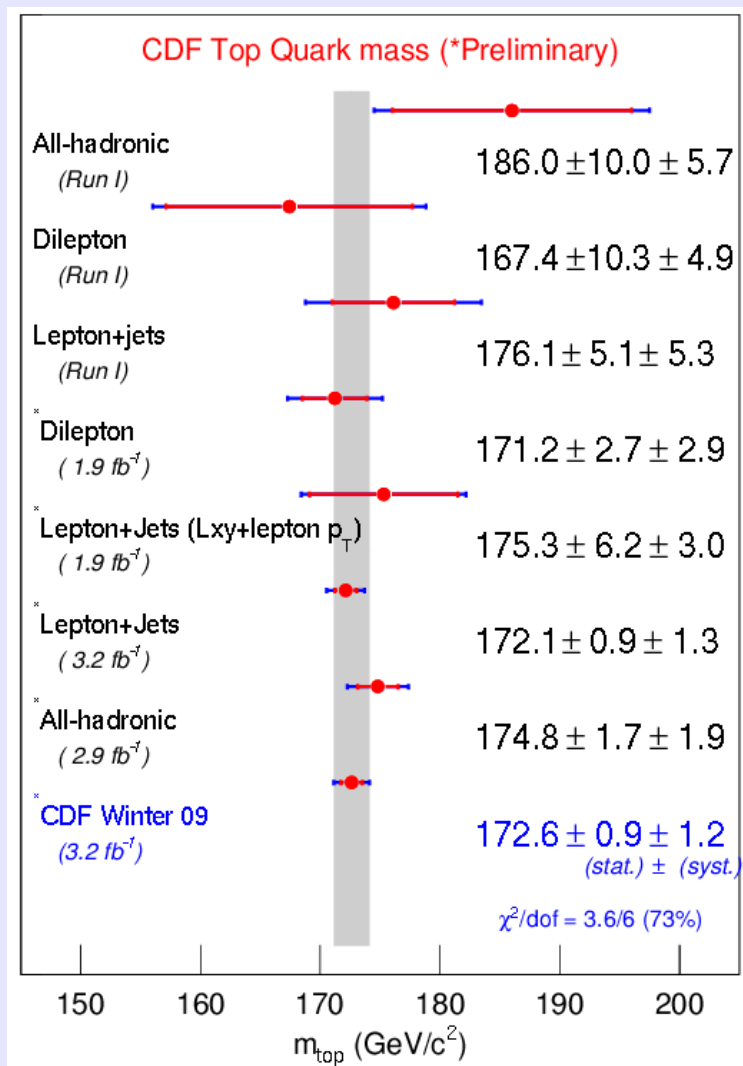
Excellent tracking system



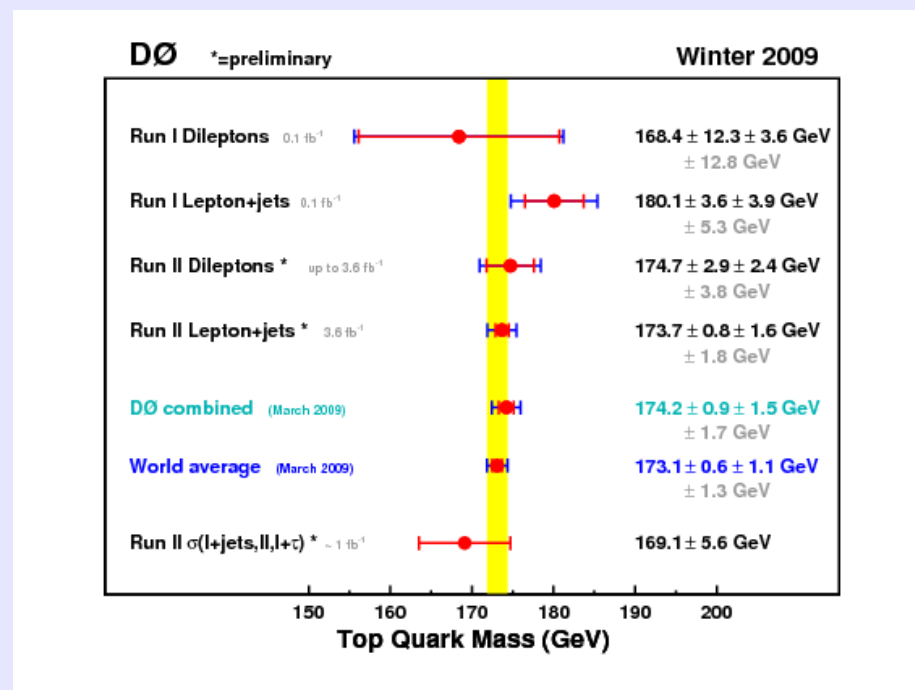
Excellent muon coverage



CDF and D0 averages



$M_t = 172.6 \pm 1.5 \text{ GeV}$



$M_t = 174.2 \pm 1.7 \text{ GeV}$